

Luminosities and mass-loss rates of Local Group AGB stars and Red Supergiants[★]

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ABSTRACT

Context. Mass loss is one of the fundamental properties of asymptotic giant branch (AGB) stars, and through the enrichment of the interstellar medium, AGB stars are key players in the life cycle of dust and gas in the universe. However, a quantitative understanding of the mass-loss process is still largely lacking.

Aims. To investigate mass loss and luminosity in a large sample of evolved stars in several Local Group galaxies with a variety of metallicities and star-formation histories: the Small and Large Magellanic Cloud, and the Fornax, Carina, and Sculptor dwarf spheroidal galaxies (dSphs).

Methods. Dust radiative transfer models are presented for 225 carbon stars and 171 oxygen-rich evolved stars in several Local Group galaxies for which spectra from the Infrared Spectrograph on *Spitzer* are available. The spectra are complemented with available optical and infrared photometry to construct spectral energy distributions. A minimisation procedure is used to determine luminosity and mass-loss rate (MLR). Pulsation periods are derived for a large fraction of the sample based on a re-analysis of existing data.

Results. New deep *K*-band photometry from the VMC survey and multi-epoch data from IRAC (at 4.5 μ m) and AllWISE and NEOWISE have allowed us to derive pulsation periods longer than 1000 days for some of the most heavily obscured and reddened objects. We derive (dust) MLRs and luminosities for the entire sample. The estimated MLRs can differ significantly from estimates for the same objects in the literature due to differences in adopted optical constants (up to factors of several) and details in the radiative transfer modelling. Updated parameters for the super-AGB candidate MSX SMC 055 (IRAS 00483–7347) are presented. Its current mass is estimated to be $8.5 \pm 1.6 M_{\odot}$, suggesting an initial mass well above $8 M_{\odot}$ in agreement with estimates based on its large Rubidium abundance. Using synthetic photometry, we present and discuss color-color and color-magnitude diagrams which can be expected from the James Webb Space Telescope.

Key words. circumstellar matter – infrared: stars – stars: AGB and post-AGB – stars: mass loss – Magellanic Clouds

1. Introduction

Almost all stars with initial masses in the range $\sim 0.9\text{--}8 M_{\odot}$ will pass through the asymptotic giant branch (AGB) phase, which is the final stage of active nuclear burning before they become post-AGB objects, planetary nebulae and finally white dwarfs. Stars above this mass range will pass through the red supergiant (RSG) phase before they may end as supernovae. In both cases, mass loss dominates the final evolutionary stages of the star.

The *Infrared Astronomical Satellite* (IRAS) and the *Infrared Space Observatory* (ISO) have greatly improved our understanding of these final evolutionary stages for stars in the Galaxy, but uncertainties in distances prevent accurate luminosities and mass-loss rates (MLRs). Sources at known distances, as in the Large and Small Magellanic Clouds (LMC and SMC), or nearby dwarf spheroidal galaxies (dSphs), reduce this problem and also enable the study of the effect of metallicity on the MLR. Surveys of the MCs with the *Spitzer Space Telescope* (Werner et al.

2004) have added to this legacy with data from IRAC (Fazio et al. 2004) and MIPS (Rieke et al. 2004): the *Spitzer* Survey of the SMC (S³MC; Bolatto et al. 2007) and the full-galaxy catalogs from *Surveying the Agents of Galactic Evolution* program for the LMC (Meixner et al. 2006) and SMC (Gordon et al. 2011).

Groenewegen et al. (2007) previously modelled the spectral energy distributions (SEDs) and spectra taken with the Infrared Spectrograph (IRS; Houck et al. 2004) on board *Spitzer* for a sample of 60 carbon (C) stars. Groenewegen et al. (2009, hereafter G09) extended this to 101 C stars and 86 oxygen-rich AGB stars and RSGs (hereafter referred to as M stars for simplicity) in the MCs.

The cryogenic phase of the *Spitzer* mission is over and the data taken with the IRS spectrograph are publicly available, e.g. through the CASSIS website (Lebouteiller et al. 2011)¹. In this paper we investigate a sample of AGB stars and RSGs in the MCs that is almost double in size compared to that considered by G09, including 19 C stars in four dSphs: Fornax, Carina, Leo I, and Sculptor (Matsuura et al. 2007, Sloan et al. 2012).

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[★] Tables A.1, A.2, B.1, B.1, and ?? are available in electronic form at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsweb.u-strasbg.fr/cgi-bin/qcat?J/A+A/>. Figures ?? and ?? are available in the on-line edition of A&A.

¹ Combined Atlas of *Spitzer*/IRS sources, available at <http://cassis.sirtf.com>.

Considerable work is ongoing to model large numbers of AGB stars in the MCs using the available photometry, by fitting the SEDs of individual stars with a radiative transfer model. Gullieuszk et al. (2012) presented results on 374 AGB candidates in a 1.42 square degree area² in the LMC observed as part of the VISTA Magellanic Cloud Survey (VMC; Cioni et al. 2011). Riebel et al. (2012) derived MLRs for a sample of $\sim 30\,000$ AGB stars and RSGs in the LMC, by fitting up to 12 bands of photometry to the precomputed Grid of Red Supergiant and Asymptotic Giant Branch Models (GRAMS; Srinivasan et al. 2011 for the C-rich grid; Sargent et al. 2011 for the O-rich grid). Srinivasan et al. (2016) used a similar approach for the SMC. Boyer et al. (2012) took a hybrid approach by first determining the dust MLR using the GRAMS models for 65 stars in 5 classes of AGB stars and RSGs. They then determined relations between the dust MLR and photometric excess at $8\,\mu\text{m}$ and used these to estimate the dust MLR for a total of about 25 000 AGB stars and RSGs in the LMC and about 7500 in the SMC.

To only consider stars with IRS spectra naturally limits the number of stars for which mass-loss rates and luminosities may be determined, but the spectra provide some important advantages compared to just a photometric sample. First, molecular absorption bands and dust emission features in the spectra allow confident identifications of C-rich versus O-rich stars (as described succinctly by Kraemer et al. 2002). Spectroscopic classifications are not perfect, primarily because some sources exhibit C-rich and O-rich characteristics simultaneously, but they do help break the degeneracies where the two classes overlap in color-color space (for the bluest and reddest sources). Second, the spectra better constrain mineralogical properties of the dust such as grain size and shape, crystallinity, and chemistry. And, because the spectra provide more information on a source than the photometry can, they also better constrain the radiative transfer models fitted to the data. The lessons learned from the smaller spectroscopic sample can then be applied to models of the much larger photometric samples.

Section 2 describes the sample of AGB stars and RSGs with IRS spectra and the spectral data. Section 3 describes the ancillary photometry and the periods derived from those data. Section 4 presents the radiative transfer model and the properties of the dust species considered. Section 5 presents the results and compares them to previous efforts (e.g. G09). Section 6 discusses the relation between stellar evolution and mass loss.

2. The sample of infrared spectra

2.1. Spectra

Several groups have obtained *Spitzer* IRS data of evolved stars in the LMC and SMC. Table 1 lists the programs considered here. The last program listed provided data on a sample of 19 C stars in the Carina, Fornax, Leo I, and Sculptor dSphs.

Most of the spectra considered here were obtained with the low-resolution modules of the IRS: Short-Low (SL), which covers the 5.1–14.2 μm range, and Long-Low (LL), which covers 14.0–37.0 μm . Both modules have a resolution ($\lambda/\Delta\lambda$) of ~ 60 –100. For some of the fainter sources, spectra were obtained using only SL. Program 40650 (Gruendl et al. 2008) observed several deeply embedded carbon-rich sources with SL and the two modules with higher spectral resolution, Short-High (SH) and Long-

High (LH). They referred to these sources as extremely red objects (EROs), and we have done the same.

All observations utilized the standard IRS nodding mode, which produces spectra of the source in two positions in each slit. Each module has two apertures, which produce spectra in two orders, along with a short “bonus” order, which produces a short piece of the first-order spectrum when the source is in the second-order aperture. Thus, to generate a full low-resolution IRS spectrum, eight separate pointings of the telescope are required, and these produce 12 spectral segments which must be combined.

The detailed nature of the observations varied substantially among the samples considered here. Some observers were careful to match the integration times and number of integration cycles in each aperture of a given module; others prioritized reduced observing time over flexibility in background subtraction. Whenever possible, we differenced images by aperture in SL, using the image with the source in one aperture as the background for the image when the source is in the other aperture. For LL, we generally used the image with the source in one nod as the background for an image with the source in the other nod in the same aperture. However, when forced to deviate from this default due to background gradients, other sources in the image, or the design of the observation, we shifted to whatever background had the least structure.

Difference images still contain pixels which cannot be calibrated (rogue pixels), which we replaced using the IMCLEAN algorithm (see Sloan & Ludovici (2012) for more details).

Spectra were extracted from images using two methods: tapered-column and optimal extraction. The former sums the spectra within a range of fractional pixels close to the spectral trace. The algorithms available with the SMART and CUPID packages are functionally equivalent;³ we used CUPID. Optimal extraction fits a measured point-spread function (PSF) to the image at each wavelength to minimize the noise. We used the algorithm available in SMART (see Lebouteiller et al. 2010 for details) but ran it offline.

For tapered-column extraction, spectra were extracted from individual images and then coadded. For optimal extraction, we coadded the images first to improve our ability to properly locate faint sources, then extracted.

The tapered-column extractions are preferred in only a few cases. If the source is extended, optimal extraction produces artifacts due to the impossibility of fitting a PSF. For bright sources, the gain in signal/noise ratio (SNR) with the optimal extraction is negligible, and for the highest SNR cases, artifacts due to limits in our understanding of the PSF can be seen. We used optimal extraction in most cases; it can improve the SNR by a factor of nearly two. Only when the spectra produced different structure did we rely on the tapered-column extraction.⁴ Most of the spectra considered here are publicly available from the CASIS website, which provides both tapered-column and optimal extractions and guidance as to which is preferred in individual cases.

Spectra observed with SH and LH were extracted using full-slit extraction, which is also available in SMART. Only the EROs from Program 40650 (Gruendl et al. 2008) are affected.

² An area corresponding to a single “tile” observed by VISTA, out of a planned 180 square degrees for the final VMC survey covering SMC, LMC, Bridge and Stream.

³ The Spectroscopy Modeling Analysis and Reduction Tool (Higdon et al. 2004), and the Customizable User Pipeline for IRS Data, available from the SSC.

⁴ Tapered-column extraction was kept for the following sources: MSX LMC 787, IRAS 04374, IRAS 05568, MH 6 and W61-6-24

Table 1. Spectroscopic *Spitzer* programs considered in this paper.

Program ID	Principal Investigator	Reference paper	Notes
200	J. R. Houck	Sloan et al. (2008)	Evolved stars in the LMC and SMC
1094	F. Kemper		AGB evolution in the LMC (and Galaxy)
3277	M. P. Egan	Sloan et al. (2006), Kraemer et al. (2016)	Infrared-bright sample in the SMC
3426	J. H. Kastner	Buchanan et al. (2006)	Infrared-bright sample in the LMC
3505	P. R. Wood	Zijlstra et al. (2006), Lagadec et al. (2007)	AGB stars in the LMC and SMC
3591	F. Kemper	Leisenring et al. (2008)	Evolved O-rich stars in the LMC
30155	J. R. Houck		Sources with crystalline silicates in the SMC
30788	R. Sahai	Sloan et al. (2014)	Embedded carbon stars and post-AGB objects in the LMC
40159	A. Tielens	Kemper et al. (2010), Woods et al. (2011)	Filling color-color and color-mag. space in the LMC
40650	L. W. Looney	Gruendl et al. (2008)	YSOs (and some deeply embedded carbon stars) in the LMC
50167	G. Clayton		RSGs in the LMC and SMC
50240	G. C. Sloan		Filling color-color and color-mag. space in the SMC
50338	M. Matsuura	Matsuura et al. (2014)	Carbon-rich post-AGB candidates in the LMC
20357	A. Zijlstra	Sloan et al. (2012)	Carbon stars in other Local Group dwarf galaxies

Another difference between observations was the requested accuracy of the peak-up algorithm used to center the source in the spectroscopic slit. Some of the spectra did not utilize the highest accuracy, and as a result these were more likely to suffer from partial truncation of the source by the slit edges. Given the narrow size of the SL slit (3.6'') compared to the typical pointing accuracy of ~0.4'', any of the SL data could be affected. Sloan & Ludovici (2012) found that for most observations, multiplying a spectral segment by a scalar would solve this pointing-induced throughput problem to within ~2%.

Throughput problems generally result in small discontinuities between spectral segments. We assumed that all corrections should be up, to the best-centered spectral segment.

We calibrated the spectra using HR 6348 (K0 III) as a standard star, supplemented with HD 173511 (K5 III) for LL data taken after the change in detector settings for that instrument (starting with IRS Campaign 45). Sloan et al. (2015) describe how the truth spectra for these sources were constructed, tested, and cross-calibrated with other systems.

2.2. Considering the sample

Not all programs considered here observed AGB stars and RSGs exclusively. As with G09, targets were selected from these programs by examining the IRS spectra, collecting additional photometry (see below), consulting SIMBAD and the papers describing these programs, and considering the results of the radiative transfer modelling (see Sec. 4).

Our classification leads to a sample with 225 C stars and 171 M stars, with the M stars including 10 objects in the foreground of the LMC and one in front of the SMC. Our C stars include R CrB stars and post-AGB objects which other groups place in separate categories. For example, we count 160 stars in the LMC and 46 in the SMC, while Sloan et al. (2016) count 144 and 40, respectively. The classifications from the SAGE Team include 145 C stars in the LMC and 39 in the SMC (Jones et al. 2017b; Ruffle et al. 2015). We have classified one unusual object, 2MASS J00445256–7318258 (j004452) as a C star, due to the deep C₂H₂ absorption band centered at 13.7 μ m. Ruffle et al. (2015) classify it as O-rich due to the presence of strong crystalline emission features at 23, 28, and 33 μ m. Kraemer et al. (2017; They refer to the object as MSX SMC 049.) confirmed its optical C-rich spectrum, noted its dual C/O chemistry in the mid-infrared, and suggested that it may be a post-AGB object.

3. Ancillary data

Tables A.1 and A.2 in the Appendix list basic information for the C and M stars respectively, including name, position, an abbreviated identifier used in subsequent tables and figures, the pulsation period, pulsation (semi-)amplitude and filter (see details in Section 3.2 below), and remarks. These tables and some of the figures use the following classifiers for the oxygen-rich stars: FG=Foreground; SG=Supergiant; MA=M-type AGB-star.

3.1. Photometry

For all stars additional broadband photometry ranging from the optical to the mid-IR was collected from the literature, primarily using VizieR⁵ and the NASA/IPAC Infrared Science Archive⁶, using the coordinates given in Tables A.1 and A.2.

In the optical we collected *UBVI* data from Zaritsky et al. (2002, 2004) for the Magellanic Clouds (MCs), *UBVR* data from Massey (2002) for the MCs, *BVRI* data from Oestreich et al. (1997) for RSGs in the LMC, *OGLE-III VI* mean magnitudes from Udalski et al. (2008a,b), *EROS BR* mean magnitudes from Kim et al. (2014) and Spano et al. (2011), *MACHO BR* mean magnitudes from Fraser et al. (2008), and *VRI* data from Wood, Bessell & Fox (1983, hereafter WBF).

Near-infrared photometry comes from DENIS *IJK* data from Cioni et al. (2000) and their third data release (The DENIS consortium 2005), the all-sky *JHK* release of 2MASS (Skrutskie et al. 2006), the extended mission long-exposure release (2MASS-6X, Cutri et al. 2006), *JHK* data from the IRSF survey (Kato et al. 2007), *JHK* data from the LMC near-infrared synoptic survey (Macri et al. 2015), SAAO *JHKL* data from Whitelock et al. (1989, 2003), and CASPIR *JHKL* data specifically taken for the IRS observations (Sloan et al. 2006, 2008, Groenewegen et al. 2007), and from Wood et al. (1992), and Wood (1998). VMC data (Cioni et al. 2011) were used for selected very red sources, mostly to try to determine their pulsation periods (Sec. 3.2).

Mid-infrared data include *IRAS* data from the Point Source Catalog and the Faint Source Catalog (Moshir et al. 1989; Loup et al. 1997; only data of the highest quality flag were considered), photometry at 3.6, 4.5, 5.8, 8.0 and 24 μ m from the SAGE survey of the LMC (Meixner et al. 2006; two epochs), the S³MC sur-

⁵ <http://vizier.u-strasbg.fr/viz-bin/VizieR>

⁶ <http://irsa.ipac.caltech.edu/>

vey of the SMC, (Bolatto et al. 2007), and the SAGE-SMC catalog (Gordon et al. 2011; also two epochs). For selected very red sources we also used *Spitzer* photometric data from Gruendl et al. (2008) and Whitney et al. (2008). We also used data from the *Wide-field Infrared Survey Explorer* (WISE; Wright et al. 2010), specifically from the *AllWISE* catalog (Cutri et al. 2013), as well as data from the *Akari* Point-Source Catalogue (up to 5 filters between 3 and 24 μm) and Infrared Camera catalog (IRC; 9 and 11 μm) (Ishihara et al. 2010, Ita et al. 2010, Kato et al. 2012).

Far-infrared data were obtained from the *Akari* Far-Infrared Surveyor (FIS, with four filters between 65 and 160 μm ; Yamamura et al. 2010), MIPS 70 μm data from the SAGE survey, and the Heritage survey, which included photometry from *Herschel* at 70, 100, 250, 350, and 500 μm (Meixner et al. 2013). Reliable data beyond 60 μm were available for only about a dozen C stars and a half dozen O stars, mostly SAGE data at 70 μm . Additionally, MIPS-SED spectra (van Loon et al. 2010a,b) were used for four sources⁷.

The literature considered is not exhaustive, but it does include all recent survey data available in the near- and mid-IR, where these stars emit most of their energy. When fitting radiative transfer models, all data were considered as individual measurements with their reported errors. No attempt was made to combine or average multiple observations in a given photometric band, or in similar bands from different telescopes. Variability is an important characteristic of AGB stars and can influence the constructed SED and the fitting. Fortunately, in the optical where the amplitude of variability is largest, mean magnitudes are available from the OGLE, MACHO and EROS surveys, with small errors on the mean magnitude.

In most cases, spectra from the IRS and the infrared photometry agreed. In the 48 cases where they did not ($\sim 12\%$ of the sample), the spectra were scaled to the available photometry in wavelengths covered by the spectrum. In half of those cases, the correction was less than 25%, and in 14 cases it was larger than a factor of 2.

3.2. Pulsation periods

An extensive effort was made to obtain pulsation periods for the sample. The most important data sources are the OGLE, EROS and MACHO photometric surveys. Although periods have been published for LPVs from these surveys, we downloaded the original data and derived periods independently using the publicly available code *Period04* (Lenz & Breger 2005). OGLE-III *I*-band data are available through the OGLE Catalog of Variable Stars.⁸ The EROS-2 data for more than 150 000 stars that were used by Kim et al. (2014) are available online,⁹ and the data for the few stars that were missing were kindly provided by Dr. Jean-Baptiste Marquette (private communication). The correspondence between EROS-2 identifier and coordinates is provided by a separate database, but is also available through SIMBAD and VizieR. MACHO data are also online.¹⁰ In this case any association listed in SIMBAD and VizieR between our sources and the MACHO counterpart was only taken as guidance, and we independently searched for all MACHO targets within 2.5'' of our targets.

⁷ With our designations: wohg64, bmbb75, msxlm349, and iras05329.

⁸ <ftp://ftp.astrouw.edu.pl/ogle/ogle3/OIII-CVS/>

⁹ <http://stardb.yonsei.ac.kr/>

¹⁰ <http://macho.nci.org.au/>

Other sources of optical data were also considered, specifically the Catalina Sky Survey (CSS, Drake et al. 2014),¹¹ ASAS-3 data (Pojmanski 2002)¹², and data from the Optical Monitor Camera (OMC) onboard *INTEGRAL* (Mas-Hesse et al. 2011).¹³

Many of the redder sources have traditionally been monitored in the near-infrared (e.g. Wood 1998, Whitelock et al. 2003), and these data have also been used, either taking directly the quoted periods and amplitudes or in some cases combining the data and rederiving the periods. For red stars with no previous period determination or where the available infrared data were sparse, the VMC database (Cioni et al. 2011) was consulted. In the *K*-band the VMC observations typically have 10–15 data points spread over a relatively short timespan (6–12 months), but when combined with other data, even if from a single epoch, a reliable and unique period could be derived in many cases (Groenewegen et al. in prep.)

To analyze the variability of the more embedded sources, we have utilized the data from *WISE* differently than described in the previous section, where the focus was on assembling photometric data to be fitted with radiative transfer models. To investigate variability, we have followed Sloan et al. (2016) and used the *AllWISE Multiepoch Photometry Table* and the *NEOWISE-R Single Exposure (L1b) Source Table* (from the NEOWISE reactivation mission; Mainzer et al. 2014) but with some changes to their method. We did not average together data taken within a few days of each other. We considered data up to and including the June 2017 release, which gives two more years of data than were considered before. We also focused just on the W2 filter at 4.6 μm , as it is brighter than W1 for the reddest sources.

When data were available, we combined the W2 data with IRAC 4.5 μm data from the *SAGE-VAR* catalog (Riebel et al. 2015), which adds 4 epochs obtained during the warm *Spitzer* mission on the Bar of the LMC and the core of the SMC with the original epochs obtained during the *SAGE* and *SAGE-SMC* surveys. The effective wavelengths of the W2 and IRAC 4.5 filters are similar, but for the reddest sources for which these data were used, the difference can be of the order of a few tenths of a magnitude. To shift the W2 at 4.6 μm to 4.5 μm , we did not use the color corrections derived by Sloan et al. (2016). Instead, we used the radiative transfer models fitted to the photometry to determine the proper adjustment from the WISE to the IRAC filter.

Tables A.1 and A.2 in the Appendix list the adopted pulsation period, the amplitude (in the mathematical sense, sometimes referred to as the semi-amplitude, or in other words, half the peak-to-peak amplitude), the filter, and the reference to the data used.

The sample includes about 180 stars with periods listed by OGLE. In 85% (88%) of the cases the period we derive from the OGLE data agrees within 5% (10%) with the first of three possible periods listed by OGLE. In an additional 6% of the cases our adopted pulsation period corresponds to the second period listed by OGLE. There are also a few cases where the period we find is about double that of the first OGLE period. The final periods listed in the tables also include the analysis from EROS and MACHO data when available.

As mentioned above, Sloan et al. (2016) used *AllWISE* and *NEOWISE* data to derive previously unknown periods for five C stars (their Fig. 20). For three stars we quote periods here based on *K*-band data from the VMC survey and the literature

¹¹ http://nunuku.caltech.edu/cgi-bin/getcssconedb_release_img.cgi

¹² <http://www.astrouw.edu.pl/asas/?page=aasc&catsrc=asas3>

¹³ https://sdc.cab.inta-csic.es/omc/secure/form_busqueda.jsp

(Groenewegen et al. in prep), that agree to within 3% with the periods found by Sloan et al. For the other two stars, we independently derived the periods based on the W2 filter (combining it with [4.5] data for one object). Despite the differences in our approaches, the periods agree within 1%.

4. The model

The models are based on the “More of DUSTY” (MoD) code (Groenewegen 2012) which uses a slightly updated and modified version of the *DUSTY* dust radiative transfer (RT) code (Ivezic et al. 1999) as a subroutine within a minimization algorithm.

4.1. Running the radiative transfer code

The RT code determines the best-fitting dust optical depth, luminosity, temperature at the inner radius, T_c , and index of the density distribution, $\rho \sim r^{-p}$ by fitting photometric data and spectra for a given model atmosphere and dust composition. (The code can also consider visibility data and 1D intensity profiles, but these data are not available for the sample considered here.) Each of the four free parameters may be fixed or fitted in the RT code, see Section 4.3.

The outer radius in the models is set to a value where the dust temperature reaches about 20 K. This implies values of $(4 - 22) \cdot 10^3$ times the inner radius, which correspond to outer radii of less than $\sim 25''$ in all cases. However, depending on wavelength, the emission comes from a much smaller region. As a test, the SED was calculated for one of the reddest sources with a large default outer radius of $13\,000 R_{in}$, and then re-run with progressively smaller outer radii. At $70\,\mu\text{m}$ the flux is reduced by 5% when decreasing the outer radius to $2\,000 R_{in}$, corresponding to about $2''$. In comparison the FWHM of the MIPS $70\,\mu\text{m}$ band is $18''$. Emission at shorter wavelengths comes from an even more compact region, e.g. $\lesssim 1''$ at $24\,\mu\text{m}$. Generally, the PSFs of the combinations of instrument and filter of the datasets listed in Sec. 3 match the physical size of the emitting region at the distance of the MCs quite well. The exception is the WISE 4 filter at $22\,\mu\text{m}$ with a PSF of $12''$, which is much larger than the size of the emitting region and makes background subtraction more important. In fact, this is the data point that has been excluded most frequently from the SEDs, in 25 of the 370 sources for which it was available.

We masked those portions of the IRS spectra with poor S/N or those affected by background subtraction problems and did not include them in the minimization procedure. In addition, spectral regions dominated by strong molecular features that are not included in the simple model atmospheres are also excluded for the C stars, i.e. the regions $5.0\text{--}6.2\,\mu\text{m}$ (CO + C₃, e.g. Jørgensen et al. 2000), $6.6\text{--}8.5\,\mu\text{m}$ and $13.5\text{--}13.9\,\mu\text{m}$ (C₂H₂, e.g. Matsuura et al. 2006). No regions were excluded in the fitting of the O-rich stars.

The photospheric models for C stars come from Aringer et al. (2009)¹⁴, while the M stars are modelled by a MARCS stellar photosphere model (Gustafsson et al. 2008)¹⁵. For the C stars, the models assume 1/3 solar metallicity for the LMC and 1/10 for the SMC and other Local Group galaxies. For M stars, the corresponding values are -0.5 and -0.75 dex. The model atmospheres also depend on $\log g$, mass, and C/O ratio (for the C-stars). The SED fitting is not sensitive to these values, and we

adopted fixed values $\log g = 0.0$ or $+0.5$, 1 or $2 M_{\odot}$, and C/O = 1.4.

To determine luminosities from the RT output, distances of 50 kpc to the LMC and 61 kpc to the SMC are adopted, while for the other Local Group galaxies the distances adopted by Sloan et al. (2012) are kept: 84.7 kpc for Sculptor, 104.7 kpc for Carina, 140.6 kpc for Fornax, and 259.4 kpc for Leo I.

The model results have been corrected for a typical $A_V = 0.15$ mag for all Magellanic stars, 0.06 mag for Sculptor, 0.08 mag for Carina and Fornax, and 0.09 mag for Leo I. We adopted the reddening law of Cardelli et al. (1989) for other wavelengths. The exact value has little impact on the results, as it corresponds to $\lesssim 0.02$ mag of extinction in the near-IR.

4.2. Dust grain properties

The dust around the C stars is assumed to be a combination of amorphous carbon (AMC), silicon carbide (SiC), and magnesium sulfide (MgS). The optical constants are taken from Zubko et al. (1996, the ACAR species, denoted “zubko” in Table B.1) for AMC, Pitman et al. (2008, denoted “Pitm” in Table B.1) for SiC, and Hofmeister et al. (2003, denoted “Hofm” in Table B.1) for MgS.

Models were run mostly for a single grain size $0.15\,\mu\text{m}$, although some models were also explored with $a = 0.10$ and $0.30\,\mu\text{m}$. The current modelling does not allow us to determine the grain size (or even grain size distribution). Nanni et al. (2016) recently found that the near- and mid-IR colors of SMC C-stars can be described better with grains of size $\lesssim 0.12\,\mu\text{m}$ than with grains $\gtrsim 0.2\,\mu\text{m}$.

The models by G09 did not consider MgS, and the 22–39 μm wavelength range was specifically excluded in their fitting. Also, the absorption and scattering coefficients were calculated in the small-particle limit for spherical grains. Here, MgS is included in the fitting, but spherical grains are known not to match the observed profile of MgS (Hony et al. 2002). The absorption and scattering coefficients for MgS have been calculated using a distribution of form factors (Mutschke et al. 2009) close to the classical CDE (continuous distribution of ellipsoids; see Min et al. 2006). This distribution fits the observed shape of the $30\,\mu\text{m}$ feature reasonably well.

The identification of MgS as the carrier of the $30\,\mu\text{m}$ feature by Goebel & Moseley (1985) has come under some scrutiny in the past few years. The primary issue is that the strength of the $30\,\mu\text{m}$ feature in some post-AGB objects would violate abundance limits if the grains were solid MgS (Zhang et al. 2009). However, if MgS forms a layer on a pre-existing core, it will produce the observed feature without requiring too much Mg or S. Sloan et al. (2014) reviewed the spectroscopic evidence supporting the case for layered grains, addressed other concerns about MgS as the carrier of the $30\,\mu\text{m}$ feature, and concluded that it remains the best candidate.

The absorption and scattering coefficients for SiC and AMC are calculated using a distribution of hollow spheres (DHS, Min et al. 2003). In DHS, the optical properties are averaged over a uniform distribution in volume fraction between 0 and f_{max} of a vacuum core, where the material volume is kept constant, in order to simulate the fluffiness of real grains. G09 found that $f_{\text{max}} = 0.7$ fitted the data well, and we use that value here.

AMC, SiC and MgS are then mixed in proportions in order to fit the data, i.e. the strength of the SiC and MgS feature. This method assumes that the mixture is uniform throughout the envelope and that the grains are in thermal contact.

¹⁴ <http://stev.oapd.inaf.it/synphot/Cstars/>

¹⁵ <http://marcs.astro.uu.se/>

For M stars the dust chemistry is richer than that for C stars. We considered several species, but found that we could model the observed data with four dust components: amorphous silicates (olivine or MgFeSiO_4 ; Dorschner et al. 1995; denoted “Oliv” in Table B.2), amorphous alumina (Begemann et al. 1997; denoted “AlOx”), metallic iron (Pollack et al. 1994; denoted “Fe”), and crystalline forsterite ($\text{Mg}_{1.9}\text{Fe}_{0.1}\text{SiO}_4$; Fabian et al. 2001, denoted “Forst”).

The absorption and scattering coefficients are calculated using DHS with $f_{\text{max}} = 0.7$, and for grain sizes 0.1, 0.2 and 0.5 μm , compared to a more traditional value of $\sim 0.1 \mu\text{m}$. For some Galactic targets, large grains have proven necessary when near-IR visibility data are available, because they provide an additional scattering component. Examples include IRC +10 216 and OH 26.5, which were fitted with MoD code by Groenewegen et al. (2012) and Groenewegen (2012), respectively. Recently, Norris et al. (2012), Scicluna et al. (2015), and Ohnaka et al. (2016) found evidence for grains in the range 0.3–0.5 μm , and 0.1–1 μm grains are advocated to drive the outflow around oxygen-rich stars (Höfner 2008, Bladh & Höfner 2012).

4.3. Finding the best model

The MoD code determines the best-fitting luminosity, dust optical depth, temperature at the inner radius, and index of the density distribution. Groenewegen (2012) describes how to identify the best-fitting model by minimising a χ^2 parameter.

The luminosity is fitted in all cases. Whether the other three parameters have been fitted or fixed is indicated in Tables B.1 and B.2. In about 8% of the objects, the data show no evidence of a dust excess, and the dust optical depth is fixed to a small value. In about one-third of the C-stars and half of the O-stars, the dust optical depth is the only additional free parameter. When not fitted, T_c is fixed to the typical condensation temperature (1200 K for C-stars and 1000 K for O-stars in most cases) and p is fixed to 2, i.e. the density law for a constant outflow velocity and MLR.

Increasing the number of free parameters will always decrease the reduced χ^2 of the model. To avoid overfitting and penalizing the addition of free parameters, MoD also calculates the Bayesian information criterion (BIC; Schwarz 1978; see also Groenewegen 2012). The best-fitting model is the one with the lowest BIC value.

Some of the parameters that are determined are external to MoD, as they are available on a discrete grid only. For example, the model atmospheres (both MARCS and Aringer et al. 2009) are available on a grid with 100 K spacing. In addition, the grain absorption and scattering properties are pre-calculated for a discrete number of grain sizes and dust compositions. For C stars, we considered AMC, SiC and MgS in ratios 100 : x : y , where x and y are integer multiples of 5. We treated O-rich stars with a similar grid for silicates, alumina, metallic iron and forsterite.

MoD is then run over the grid of effective temperatures (for a typical dust composition) to find the best-fitting model atmosphere. Then the model atmosphere is fixed to that effective temperature, and the model is run over the grid of grain sizes and dust compositions to find the best dust model. The input and output of the models (parameters, reduced χ^2 , BIC) are stored, so that the lowest BIC (the best-fitting model) may be found, and errors estimated for the parameters.

5. Results

Tables B.1 and B.2 in the Appendix list the parameters of the models which best fit the observed data for the C stars and M

stars, respectively. Figures ?? and ?? in the Appendix show the best-fitting model to the SED and IRS spectra for these two groups. The tables include the luminosity and MLR, calculated assuming an expansion velocity v_{exp} of 10 km s^{-1} and a gas-to-dust ratio of 200. Observations of CO line widths suggest that the outflow velocity may depend on luminosity and metallicity (e.g. van Loon et al. 2000, Lagadec et al. 2010, Groenewegen et al. 2016; Goldman et al. 2017). The gas-to-dust ratio in the circumstellar outflows is expected to scale with the initial metallicity for O rich sources, but this is not clear for C rich sources, which fuse carbon in their interiors. In both cases, though, the nature of that dependence is uncertain, and we hold both velocity and gas-to-dust ratio constant to aid comparison. The MLRs are proportional to both quantities and can be scaled as desired.

The fitting routine also provides uncertainties for the MLR, dust temperature at the inner radius, and luminosity. These are typically small, of order 1%, and are not reported. The realistic 1σ errors are larger, and can be estimated from a comparison of model runs with different parameters and different realizations of the photometric data. They are typically 10% in luminosity, 25% in MLR and 50 K in T_c , and have been estimated from the spread in the parameters in all models that have a χ^2 less than twice the value of the best-fitting model. The difference between the small fitting error and the realistic error is likely due to the difficult treatment of source variability in the fitting. Currently, multiple measurements at a given wavelength have been assigned their respective photometric errors. However, the source variability, especially in Miras and long-period variables is usually much larger than the photometric uncertainty. The fitting will lead to a larger best-fit χ^2 than if the same source were only fitted with, say, a single K -band photometric point.

5.1. Color relations

Some of the analysis presented by G09 can be improved here thanks to the larger sample size. Figure 1 shows a synthetic color-color diagram (CCD) generated from the best-fitting models. Plotting $[5.8] - [8.0]$ vs. $[8.0] - [24]$ is effective at distinguishing M from C stars (Kastner et al. 2008, G09). The larger sample only reinforces this conclusion. Following this result, we also constructed CCDs with similar colors generated by using *WISE* and *Akari* data. For *WISE* data, $W2 - W3$ vs. $W3 - W4$ has the most discriminatory power, and for *Akari*, it is $N4 - S7$ vs. $S7 - L24$. Both CCDs show behavior similar to the *Spitzer*-based CCD, but they do not separate the M and C stars quite as well.

Each of the top panels in Fig. 1 also includes two lines that separate M and C stars, with a break at $[5.8] - [8.0] = 0.8 \text{ mag}$. To the blue, the M stars are those with $[5.8] - [8.0] < 0.125 ([8] - [24]) + 0.150$. To the red, they follow $[5.8] - [8.0] < 0.463 ([8] - [24]) - 0.121$. Over 95% of the stars classified as C stars appear above this line. Ten stars classified as C stars, however, stray into the M-star territory.

Two of the strays are red, with $[8.0] - [24.0]$ at 1.9 mag (in the LMC) and 2.3 mag (in the SMC). The red SMC object, IRAS 00350, is classified by Sloan et al. (2014) as a C-rich post-AGB object and is evolving to the red at shorter wavelengths, as expected for more evolved post-AGB objects and young planetary nebulae. The red LMC source is MSX LMC 663, which shows a peculiar SED and the highest effective temperature of the C-rich sample. It has not actually crossed into the color range defined by the sequence of M stars, and the fact that it has crossed the boundary line illustrates that one could easily draw the boundary slightly differently. A few other C-rich objects have also strayed toward the sequence of M stars.

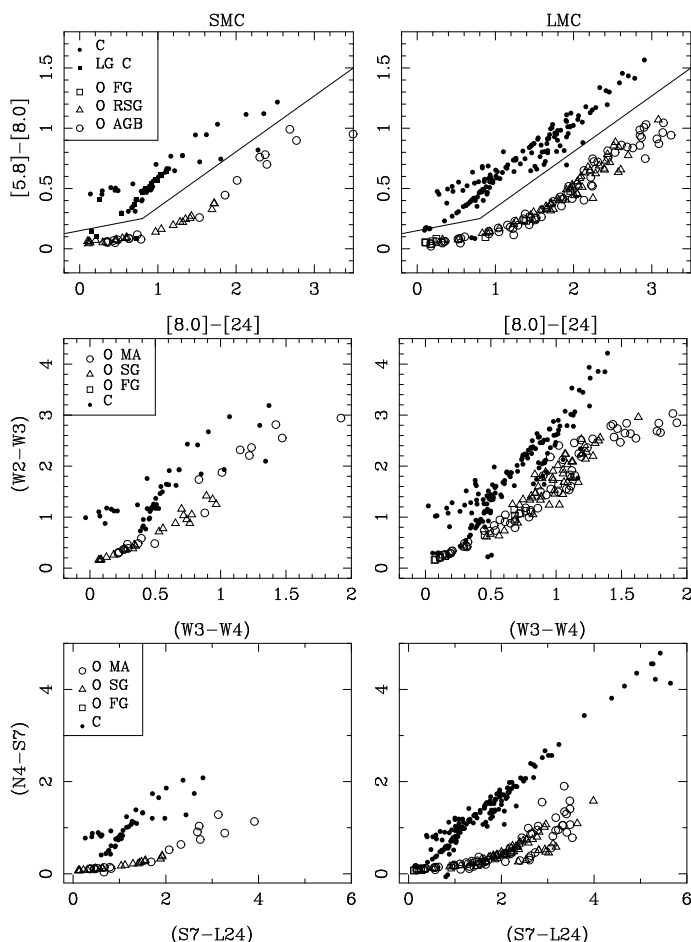


Fig. 1. Color-color diagrams for the SMC (left-hand panels) and LMC (right-hand panels). Top panels: the combination of IRAC and MIPS colors from *Spitzer*. Middle panels: *WISE* colors. Bottom panels: *Akari* colors. Symbols are explained in the legend. The lines indicate the border between C- and O-rich stars (see text).

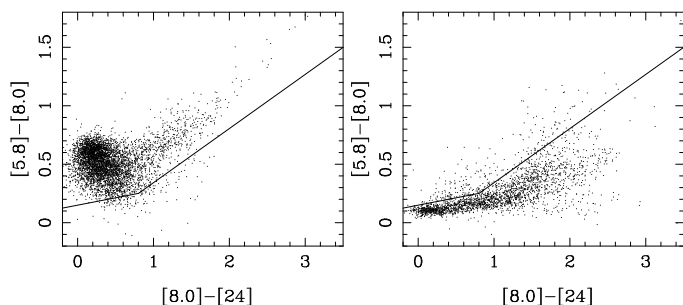


Fig. 2. Color-color diagrams for the LMC for C-rich (left-hand panel) and O-rich stars (right-hand panel), as classified by Riebel et al. (2012). The lines indicate the border between C- and O-rich from Fig. 1.

The remaining eight C stars below the boundary with M stars are all relatively blue and dust-free. Three are in the Carina dSph, and their spectra showed no evidence of amorphous carbon or SiC dust (Sloan et al. 2012). Two, HV 5680 and WBP 17, have clearly C-rich optical spectra and have infrared spectra showing little or no amorphous carbon dust (Sloan et al. 2008). The remaining three are from the SAGE sample observed by the IRS. Woods et al. (2011) classified two, PMP 337 and KDM 6486, as “C-AGB”, and they are classified by Sloan et al. (2016) as naked and nearly naked C stars (respectively). Woods et al. (2011) classified the third source, LMC-BM 11-19, simply as “star”, and

it did not appear in the C-rich sample of Sloan et al. (2016). All ten of these stars are close to naked stars, and all dust-free stars, whether they be C-rich or O-rich, will fall in the same region in most infrared color-color spaces, making some overlap inevitable for the bluest sources.

To test the robustness of how the C stars and M stars separate by color, we examined the sample of stars defined by Riebel et al. (2012). Figure 2 plots those stars with relative errors at $24\ \mu\text{m} < 5\%$ and classified by them as C-rich or O-rich. Of the 4867 C-rich stars, only 161, or 3.3%, stray into the zone of the M stars as defined above. Of the 2496 stars classified as O-rich, 2233, or 89%, fall in the O-rich zone. These high percentages testify to the discriminatory power of this CCD.

5.2. Bolometric corrections

Figure 3 shows the bolometric correction (BC) at $3.6\ \mu\text{m}$ versus $[3.6] - [8.0]$ color, and at K versus $(J - K)$ color (in the 2MASS system) for the synthetic colors determined from the best-fitting models for all sources. The bolometric magnitude M_{bol} has been calculated from $-2.5 \log L_{\text{bol}}/L_{\odot} + 4.72$ mag. The data have been fitted by polynomials, and Table 2 lists the coefficients and the rms in the fit. Relations like these make it possible to estimate bolometric magnitudes with an estimated uncertainty of about 0.1–0.3 mag, which should be sufficient for most applications. Such an estimate could also serve as a first guess in a more detailed automated modelling.

The BC for C stars at $3.6\ \mu\text{m}$ is the best defined relation and has an rms scatter below 0.1 mag. Polynomials are fitted separately to the data on either side of $[3.6] - [8.0] = 1.7$ mag, and they exclude six stars outside the plotted color range as well as three SMC stars with $[3.6] - [8.0]$ colors in the range 1.2–2.8 mag that are below the line (from left to right: CV 78, IRAS 00350 and j004452).

For the C stars, the BC for $(J - K)$ agrees well with the quadratic relation by Kerschbaum et al. (2010) in the range in common ($J - K < 4$). Our values are on the low side compared to observations by Whitelock et al. (2006) and models by Nowotny et al. (2013) and Eriksson et al. (2014). The fitting excludes 24 C stars with $(J - K) > 10$ mag as well as the outliers SAGEMCJ054546 (near $J - K \sim 1.75$ mag) and IRAS 05278 (near $J - K \sim 4.05$ mag).

For the redder carbon stars, the scatter about the fitted polynomials is substantially larger for the bolometric corrections based on $(J - K)$ compared to $[3.6] - [8.0]$, primarily because $[3.6] - [8.0]$ better samples the peak of the SED for these sources. Another contribution to the scatter at $(J - K)$ is that more evolved carbon stars can show excesses of blue radiation, which Sloan et al. (2016) attribute to scattered light escaping from shells as they begin to depart from spherical symmetry (see Section 5.3). For all of these reasons, we would recommend the use of BCs based on $(J - K)$ only for $J - K \lesssim 2$ mag. Beyond that limit, BCs based on colors from longer-wavelength filters will be more reliable.

The BCs for M stars based on $[3.6] - [8.0]$ show a well-defined relation with a scatter of about 0.2 mag. No data were excluded from the plot or the fitted polynomial.

We have fitted two polynomials to estimate the BC for M stars based on $(J - K)$, with a break at $J - K = 1.45$ mag. One M star (IRAS 05329 at $J - K \sim 7.1$) is neither plotted nor fitted. In the regime $J - K < 1.45$ mag four stars are excluded by sigma-clipping (HV 12122, HV 12070, NGC 1948 WBT 2215, SAGEMCJ050759). The break at $J - K = 1.45$ mag results from a clear dichotomy in the data, which can also be seen in the data presented by Kerschbaum et al. (2010). For bluer colors, where

most of the stars are located, a simple straight line fits well, with a dispersion less than 0.1 mag. For redder colors a third-order polynomial is fitted, but the data show much more dispersion. As for the carbon stars, the BC based on $[3.6]-[8.0]$ is much better behaved for the redder sources in the sample. Here the shift away from BCs based on $(J - K)$ should occur at $J - K \sim 1.45$ mag.

5.3. Mass-loss rates

Figure 4 plots MLR as a function of $[3.6]-[8.0]$ color generated from synthetic photometry of the fitted models. It closely resembles the corresponding figure from G09. Generally, redder colors are associated with larger MLRs, as expected. The relations are tight, with no clear dependence on metallicity (assuming that the expansion velocity and gas-to-dust ratio do not depend on metallicity).

Sloan et al. (2008) fitted a line to the logarithm of the MLR as a function of color for carbon stars. They used a spectroscopically derived color ($[6.4]-[9.3]$), which closely follows the photometric $[5.8]-[8]$ color (Sloan et al. 2016). However, the older sample did not include targets observed later in the *Spitzer* mission, which added more sources at the red and blue ends of the color range. For the carbon stars, the additional sources do not follow a single linear relation. Matsuura et al. (2009) used a three-parameter function based on the inverse of the color, which adds the necessary curvature. For the carbon stars,

$$\log \dot{M} = -4.080 - \frac{6.531}{([3.6] - [8.0]) + 0.941}. \quad (1)$$

The typical uncertainty in $\log(\text{MLR})$ is about 0.22 dex. The three data points with $[3.6]-[8.0] \sim 6.5$ mag and $\log \dot{M} > -4$ are excluded, because they have probably evolved off of the C-rich sequence defined by the rest of the sample. Two of these sources appear in the sample of Magellanic carbon-rich objects of Sloan et al. (2014), primarily because their IRS spectra were redder than any of the carbon stars considered by Sloan et al. (2016). The spectra showed no other obvious spectral features associated with post-AGB objects, such as forbidden lines, fullerenes, or polycyclic aromatic hydrocarbons (PAHs). The third source is one of the EROs from the sample by Gruendl et al. (2008), ERO 0518117.

As a group, the observed photometry of these sources suggests that they have begun to evolve off of the AGB, by showing both reduced variability and bluer colors at shorter wavelengths. C stars generally show a tight relation between most infrared colors, so that in most CCDs, they fall along an easily recognisable sequence. However, some of the reddest sources depart from that sequence. For example, several of the EROs have a bluer color at $[3.6]-[4.5]$ than expected from $[5.8]-[8.0]$ (Fig. 13 from Sloan et al. 2016). These sources may be deviating from spherical symmetry, allowing some light from the central star to escape via scattering in the poles of the extended envelope. One should keep in mind that our models assume spherical symmetry. Sloan et al. (2016, Fig. 14) also found that the variability of C stars increases to a $[5.8]-[8.0]$ color of ~ 1.5 mag, but past that color it decreases. One would expect decreased variability as a star sheds the last of its envelope and departs the AGB.

For the M stars,

$$\log \dot{M} = -4.708 - \frac{2.488}{([3.6] - [8.0]) + 0.545}. \quad (2)$$

The typical uncertainty is about 0.49 dex in $\log \dot{M}$, which is larger than for the C stars, due mostly to the apparent split in

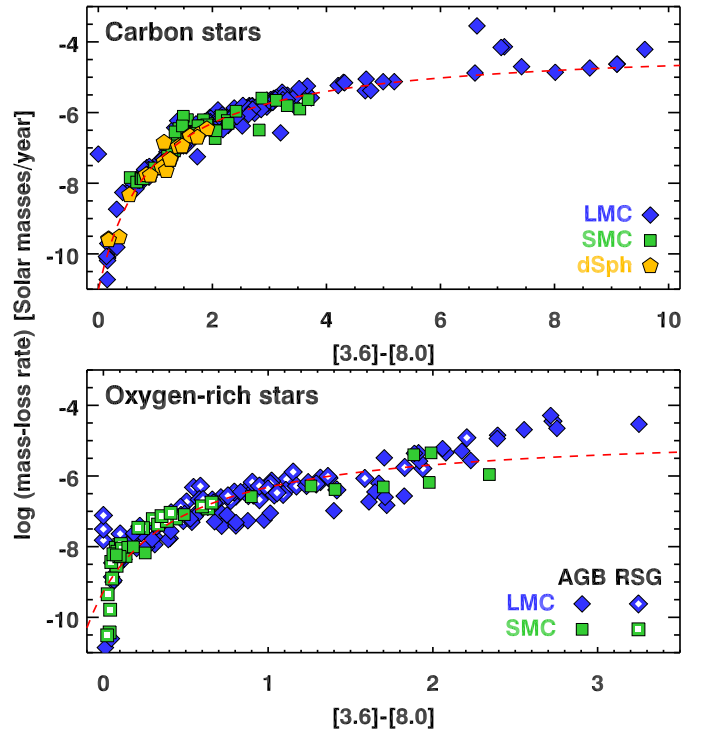


Fig. 4. Mass-loss rate versus color for C stars (top panel), and M stars (bottom panel). The fitted relations are shown as dashed orange curves and are given by equations (1) and (2). The carbon stars include sources from the LMC, SMC, and dwarf spheroidal galaxies.

the relation for AGB stars and red supergiants, with the supergiants usually showing higher MLRs. This relation is not valid at the bluest colors, $[3.6]-[8] \lesssim 0.1$ mag, because the actual MLRs drop to zero much more quickly than the fitted relation indicates.

The major difference with G09 is that the current C-rich models use the optical constants for AMC from Zubko et al. (1996), while G09 used the constants from Rouleau & Martin (1991).

6. Discussion

6.1. Comparison to other works

6.1.1. Groenewegen et al. (2009)

First we compare the MLRs derived by G09 to the present paper, which includes more photometry for the SED, uses different model atmospheres, and uses improved code for radiative transfer. In addition, the absorption and scattering coefficients have been calculated differently and with different optical constants, with a change in amorphous carbon for the C stars and a change from astronomical silicates derived from observations to silicates measured in the laboratory for M stars.

The ratio of the MLRs for 76 non-foreground (FG) M stars (in the sense of old/new) has a median value of 1.17, with 90% of the ratios in the range 0.6 to 2.7. The M stars show no obvious systematic effects, and the scatter suggests a random fitting error of a factor of 2 in the MLR.

The difference between the current models and those of G09 is much more dramatic for the carbon stars, as Figure 5 shows for the 101 sources in common between the two samples. This difference arises primarily from the shift from the optical constants for amorphous carbon from Rouleau & Martin (1991) to the ACAR sample from Zubko et al. (1996). The mean ratio is

Table 2. Bolometric corrections fitted to the data.

Condition	a_0	a_1	a_2	a_3	a_4	rms
C stars $0.0 < [3.6] - [8.0] < 1.7$	3.290	-0.843	+1.99307	-0.604618		0.063
C stars $1.7 < [3.6] - [8.0] < 5.5$	3.386	+1.565	-0.58910	+0.043892		0.073
M stars $0.0 < [3.6] - [8.0] < 3.0$	2.866	+0.419				0.21
C stars $0.9 < (J - K) < 10$	0.919	+2.482	-0.91577	+0.111553	-0.004608	0.36
M stars $0.9 < (J - K) \leq 1.45$	1.453	+1.084				0.096
M stars $1.45 < (J - K) < 6.0$	2.354	+0.453	-0.13580			0.31

Notes. Bolometric corrections to K and $[3.6]$ are computed as $BC = \sum_i a_i [\text{color}]^i$.

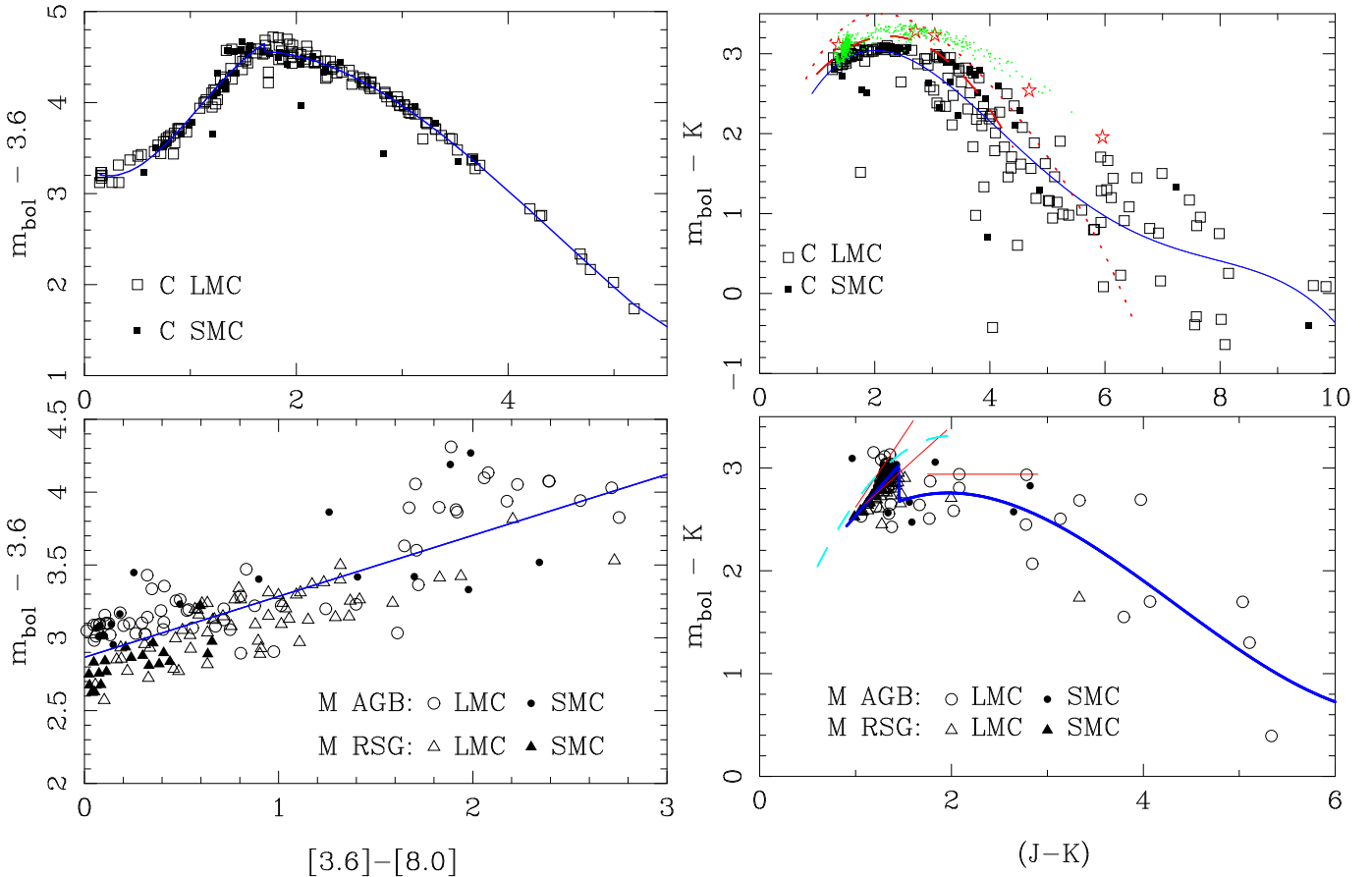


Fig. 3. Bolometric correction at $3.6 \mu\text{m}$ versus $[3.6] - [8.0]$ color (left) and K versus $J - K$ color (right) for C stars (top panels) and M stars (bottom panels). The solid dark-blue lines are polynomial fits to the data (see Table 2). See Section 5.2 for an explanation of sources not fitted or plotted. For C stars in the top right panel, red stars indicate models by Nowotny et al. (2013), green dots indicate models by Eriksson (2014), the dotted red line indicates the fit by Kerschbaum et al. (2010), and the dashed red line indicates the fit by Whitelock et al. (2006). For M stars in the lower-right panel, the straight red lines indicate relations "A", "B", and "C" from Kerschbaum et al. (2010), valid in the range $1.0 < J - K < 1.6$, $1.1 < J - K < 1.95$, and $1.75 < J - K < 2.9$ mag, respectively. The dashed light blue line indicates the fit by WBF.

8.99, the median is 7.58, and the standard deviation is 5.82. 80% of the sample have a ratio of MLRs between 5.2 and 11.4. The bottom panel of Figure 5 shows that the change in MLR due to the change in optical constants decreases with higher MLR, down to a ratio of 5.0 for the highest mass-loss bin.

A direct comparison of the extinction coefficient of the amorphous carbon grains used in the present work and by G09 (they assumed small grains and ignored scattering) shows that the ratio of opacities is about 9.5 at $1 \mu\text{m}$ and 5.4 at $2 \mu\text{m}$, consistent with the trend seen in Figure 5.

These results reveal the impact of the chosen optical constants for amorphous carbon. The constants from Zubko et al. (1996) produce slightly better fits to the observed spectra, but no compelling reason exists for choosing one set of constants

over another. The consequences of this decision are substantial. Boyer et al. (2012) and Matsuura et al. (2013) both estimated the total dust input from AGB stars in the SMC and LMC, but their estimates differed by factors of ~ 8 in the LMC and ~ 11 in the SMC. In both cases, the estimates by Matsuura et al. were higher, because they used the models by G09 to calibrate the MLRs of their photometric sample, and those models were based on the optical constants from Rouleau & Martin (1991). Boyer et al., on the other hand, used the GRAMS models (Srinivasan et al. 2011), which are based on the ACAR constants from Zubko et al. (1996).

Dust grains with more regular lattice structures should be more efficient absorbers and emitters, because they can function as better antennae. If we can apply that principle to the dust con-

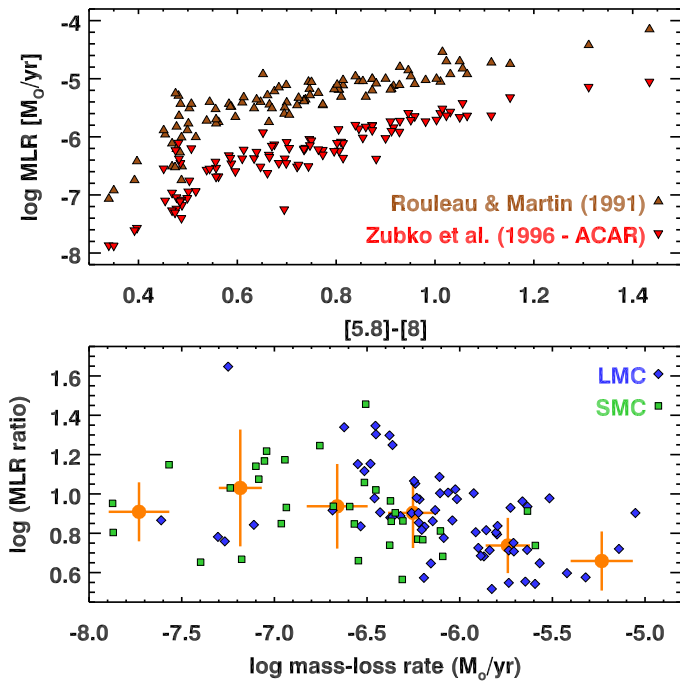


Fig. 5. Comparison of the mass-loss rates for carbon stars between the present work and G09. The current work uses optical constants for amorphous carbon from Zubko et al. (1996), while G09 used constants from Rouleau & Martin (1991). Top: A direct comparison for the common sources shows that the new models have much lower MLRs. Bottom: The ratios of the MLRs tend to be ~ 9 , although the difference between the models drops for the highest MLRs. The gold data points in the bottom panel are the median values for the log of the MLR ratio in each 0.5-dex bin, plotted against the mean log MLR; the error bars are the formal standard deviations.

stants, it follows that more graphitic carbon-rich dust will have higher opacities, and thus require less dust mass to explain a given amount of emission and absorption. More amorphous dust would require more mass, and that is consistent with the constants from Rouleau & Martin (1991), the models by G09, and the estimated total dust inputs in the SMC and LMC by Matsuura et al. (2013). On a microscopic level, graphitic grains can be described as purely aromatic sheets of carbon, while more amorphous grains would consist of mixtures of aromatic and aliphatic carbon. The aliphatic/aromatic ratio is thus the key descriptor of the dust. It would be particularly helpful for future laboratory work to explore this ratio in their samples, because we still do not have a way to distinguish what best fits the carbon stars we have observed. And as noted already, this lack of knowledge leads to significant uncertainty in total dust production by carbon stars in nearby galaxies.

6.1.2. Riebel et al. (2012)

We can also compare our results to those of Riebel et al. (2012), who derived MLRs for a sample of $\sim 30\,000$ AGB stars and RSGs in the LMC by fitting up to 12 photometric bands with the GRAMS models. We matched our source list to their LMC targets using a search radius of $1''$ and only keeping stars for which they list an error in the MLR of less than 30%. Figure 6 plots the ratio of our dust MLRs (found by dividing the MLR by 200) and theirs. For 130 C stars in common the median of this ratio is 0.46, with 90% of the stars within a factor of 2.7 of this.

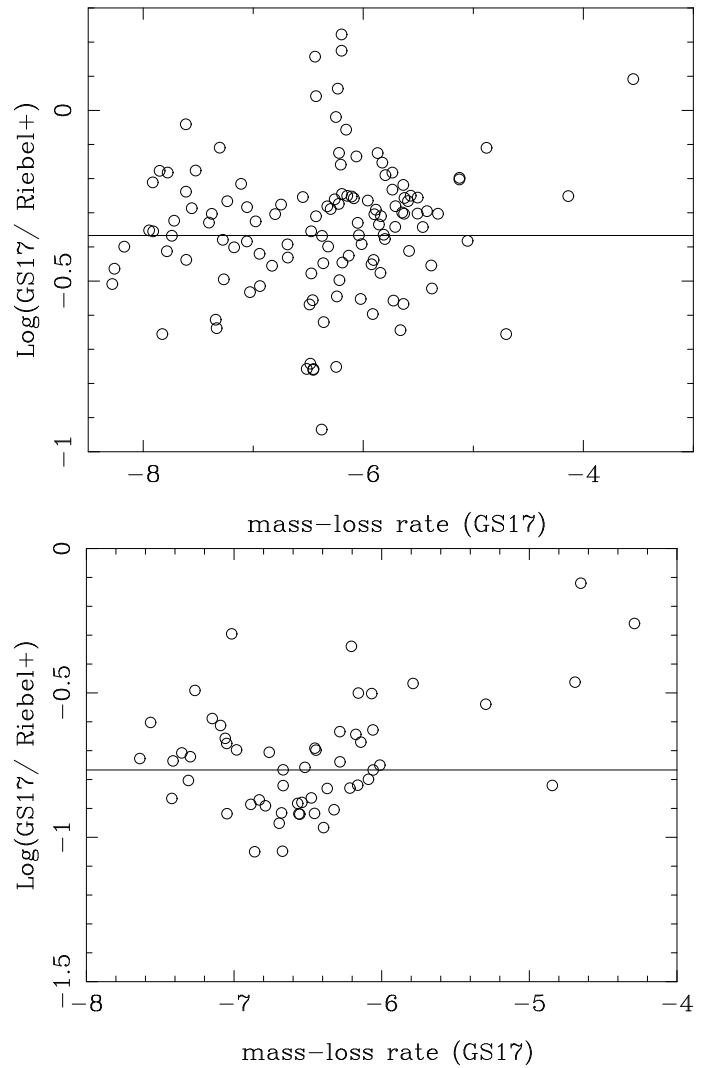


Fig. 6. Ratio of dust MLRs found in the present paper and by Riebel et al. (2012). In the top panel the C stars, in the bottom panel the O-rich stars. The lines indicate the mean ratios of, 0.46, and 0.17, respectively.

For 63 M stars (excluding FG objects) the median ratio is 0.17 with 94% within a factor of 3 of this value.

The difference in MLRs could arise from different inner radii in case of the C stars (see next section) while for the O stars it could be due to the difference in using astronomical silicates versus opacities based on optical constants measured in the laboratory (see Sections 6.1.4 and 6.1.5).

6.1.3. Srinivasan et al. (2011)

Srinivasan et al. (2011) compared their results to G09 and found that their MLRs were a factor 1.7 lower (median value). They related this difference to their use of the optical constants from Zubko et al. (1996), while G09 used the constants from Rouleau & Martin (1991). However, as noted in the previous section, the same change in optical constants reduces the MLRs by a factor of between 5 and 10 for the stars in common between the present work and G09. Thus the differences in methodology must also affect the estimated MLRs.

Table 3 lists the four stars used to calibrate the GRAMS models. They are the C stars TRM 88 and OGLE LMC-LPV-28579 (our identifier is ogle051306), and the M stars

HV 5715 and SSTISAGE1C J052206.92-715017.6 (our identifier is sagemcj052206). The table lists the derived luminosities and dust MLRs in the various papers, with the error or range in the parameters when available.

Sargent et al. (2010) and Srinivasan et al. (2010) describe the detailed radiative transfer modelling of the SED and IRS spectrum of the two M stars and C stars, respectively. The same numerical code, optical constants, grain-size distribution, etc., derived in these papers were then used in the generation and validation of the GRAMS model grid (Sargent et al. 2011, Srinivasan et al. 2011), and its application (Riebel et al. 2012, Jones et al. 2012, Srinivasan et al. 2016). Other papers have modelled the SED and/or IRS spectrum using independent methods (e.g. van Loon et al. 1999, G09, Jones et al. 2014).

It is important to note that the estimates for luminosity and MLR by Srinivasan et al. (2011, 2016), Sargent et al. (2011) and Riebel et al. (2012) are based on the same GRAMS model grid. These efforts differed in the details of how the photometric data were gathered and the models were fitted, but they all used models from the same grid. Their estimated luminosities and dust MLRs agree well, although, as discussed below, the work of Jones et al. (2012), which also used the GRAMS model grid, differed more significantly.

Section 6.1.2 quoted median ratios for our dust MLR to those by Riebel et al. of 0.46 for C stars and 0.17 for O stars. Within the errors these ratios are consistent with the values for the individual objects (0.42 and 1.65, respectively, for the C stars TRM 88 and ogle051306, and 0.16 and 0.21 for the two O stars).

However, the present work determines a dust MLR for TRM 88 ~ 8 times lower than G09. This difference cannot be due entirely to the different optical constants. Other differences in the approach by us, G09, and Riebel et al. (2012) must also play a role.

A likely suspect is that the GRAMS models allow for larger temperatures at the inner radius. The GRAMS models are run for a fixed grid of inner radii ($R_{\text{in}} = 1.5, 3, 4.5, 7, 12 R_{\star}$ for the C-star grid, and 3, 7, 11, and 15 R_{\star} for O-star grid), but only models with corresponding temperatures below 1800 K and 1400 K (respectively) are kept. The present work does not accept condensation temperatures higher than 1200 K. Srinivasan et al. (2011) provide R_{in} or T_c for our calibration C stars. For TRM 88, we find an inner radius of 15.6 R_{\star} , while Srinivasan et al. find a lower value, 12 R_{\star} , which is consistent with the ratio of dust MLR of 0.42 between the present work and the GRAMS grid. For OGLE 051306 we find 14.1 R_{\star} , while Srinivasan et al. (2010) find 4.4 R_{\star} , a difference due to the temperature at the inner radius, 970 versus 1300 K. If we had adopted that temperature, our MLR would drop by factor of 3.2, and the ratio of our dust MLR compared to Riebel et al. (2012) would decrease from 1.65 to 0.5, or close to the median value.

6.1.4. Jones et al. (2012)

For the O-rich stars HV 5715 and sagemcj052206, Sargent et al. (2010) fitted the SED and IRS spectra, and their results agree well with the GRAMS-based results of Sargent et al. (2011) and Riebel et al. (2012) (see Table 3). The fitting method of Jones et al. (2012), however, led to a much higher estimate of dust MLRs. They also used the GRAMS model grid, but the details of their method differed¹⁶.

¹⁶ They used an extra data point in the SED corresponding to the IRAS 12 μm band and determined from the IRS data, used larger error bars in the χ^2 fitting in order to account for variability, resulting in more

An examination of the 69 M stars in common between Jones et al. (2012) and Riebel et al. (2012) leads to a median ratio in the MLRs of 1.6 (Jones et al. / Riebel et al.), which is not large, but only 35% of the stars lie within a factor of 3 of the median. Nineteen stars have MLR ratios which differ from the median by a factor of 10 or more, and five differ by a factor of 75 or more. Thus the scatter when considering individual objects is significantly higher, even if the statistical difference for the overall sample is small. As noted above, for 63 M stars in common between Riebel et al. (2012) and the present work, the median ratio (this work / Riebel et al.) in the MLRs is 0.17, with no object with an MLR ratio more than a factor of ten from the median. That difference presents the opposite problem: reasonable consistency among source-to-source, but a greater shift between the model results overall.

6.1.5. Jones et al. (2014)

Jones et al. (2014) investigated a sample of evolved stars in the LMC by fitting photometry and IRS spectra to a grid of models calculated with the code *MODUST* (Bouwman et al. 2000). Table 3 shows that for HV 5715 and sagemcj052206, they find much lower dust MLR than Jones et al. (2012), and this result is generally true for the larger sample. The two samples contain 26 stars in common, and the median ratio of the 2014 results to 2012 is 0.13, again with a large scatter; for 30% of the stars the difference exceeds a factor of 5. The major difference between the two works is the adopted opacities: Jones et al. (2012) relied on the GRAMS models which use the “astronomical silicates” from Ossenkopf et al. (1992), while Jones et al. (2014) derive the opacities from optical constants measured in the laboratory, as in the present work.

The differences between the dust MLR from Jones et al. (2014) and the present work are relatively small and uniform. For 18 stars in common, the median ratio is 1.65, with all stars within a factor of 2.6 of this value. Because both papers used identical optical constants for amorphous silicates and aluminium oxide, the differences are likely due to the differences in the opacity for iron and the derived (present paper) or adopted (Jones et al. 2014) iron fraction. Differences in the radiative transfer and fitting procedure are likely to have had a smaller effect. We typically find larger iron fractions than adopted by Jones et al. (2014) and hence lower MLRs.

We have calculated the extinction coefficient for warm oxygen-deficient silicates from the astronomical silicates from Ossenkopf et al. (1992) for single-sized grains of 0.15 μm and compared those to the grains that best fit HV 5715 and sagemcj052206 in the present work. The grains in the present work are larger, and the ratio of opacities at 1 and 2 μm are 1.5–2.6 and 2–6, respectively, consistent with the differences in MLRs between the present work and most of the works based on the M-star GRAMS grid.

6.2. Mass-loss and stellar evolution

G09 compared the MLR vs. luminosity diagram with predictions from stellar evolutionary models by Vassiliadis & Wood (1993, hereafter VW) and those using recipes developed by Wagenhuber & Groenewegen (1998) with a Reimers mass-loss law (with multiplicative scaling parameter $\eta = 5$ on the AGB). The

GRAMS models providing “good” fits to the data. They also accounted for inclination angle of the LMC disk which leads to some differences in luminosity and MLR (Jones et al., 2012, private communication).

Table 3. Comparison of derived dust MLRs and luminosities for two C stars (TRM 88 and OGLE 051306) and two O stars.

Reference	L (L_{\odot})	\dot{M}_{dust} ($10^{-9} M_{\odot} \text{ yr}^{-1}$)
TRM 88		
van Loon et al. (1999)	13300	6.0
G09	7160	16.1
Srinivasan et al. (2011)	11700	3.4
Riebel et al. (2012)	9120 ± 650	4.92 ± 0.58
present paper	9403	2.1
OGLE 051306		
Srinivasan et al. (2010)	4810, 6580	2.5 (2.4-2.9)
Srinivasan et al. (2011)	6170	2.4
Riebel et al. (2012)	7080 ± 700	2.12 ± 0.42
present paper	4740	3.2
HV 5715		
Sargent et al. (2010)	$36\,000 \pm 4000$	2.3 (1.1-4.1)
Sargent et al. (2011)	33 000	1.5
Riebel et al. (2012)	$33\,700 \pm 5960$	1.56 ± 0.43
Jones et al. (2012)	28 800	19.6
Jones et al. (2014)	$19\,230 \pm 4300$	0.63 ± 0.14
present work	28 200	0.25
sagemcj052206		
Sargent et al. (2010)	5100 ± 500	2.0 (1.1-3.1)
Sargent et al. (2011)	4900	2.1
Riebel et al. (2012)	4820 ± 670	2.11 ± 0.44
Jones et al. (2012)	4740	19.6
Jones et al. (2014)	3160 ± 710	0.68 ± 0.19
present work	4120	0.45

comparison largely favored the VW models, vindicating their adopted mass-loss recipe, which is essentially the minimum of the single scattering limit $\dot{M} = 2.02 \cdot 10^{-8} L/v_{\text{exp}}$, and an empirical relation between $\log \dot{M}$ and P . The fundamental-mode period, P , is calculated from a period-mass-radius relation (see VW for details).

Figure 7 shows the relation between MLR and luminosity, with the VW model tracks for LMC metallicity overplotted (the crosses connected with the dotted lines). From the individual evolutionary tracks, a model is plotted every 5000 years. The density of points therefore represents the time spent at a certain position in the diagram. It also explains the “excursions” which are due to the finite probability of catching a star during a thermal pulse or the luminosity dip that follows. Models are plotted for initial masses of 1.5, 2.5, 5.0 and 7.9 M_{\odot} , which evolve at increasing luminosity.

The distribution of MLRs for the O-rich AGB stars (in the bottom panel) is similar to that described by G09. They are prominent at lower luminosities, which correspond to lower masses where C stars are less likely to form or will form later during their evolution on the AGB. Oxygen-rich AGB stars are largely absent at intermediate luminosities, which correspond to masses dominated by C stars, and they are prominent at higher masses, where hot-bottom burning inhibits the formation of C stars. Essentially no stars exceed the single-scattering limit. The MLRs of the RSGs scatter around the relation for Galactic RSGs derived by Verhoelst et al. (2009), $\log \dot{M} = -16.4 + 1.89 \log L/L_{\odot}$. The spread is ~ 2 dex, which

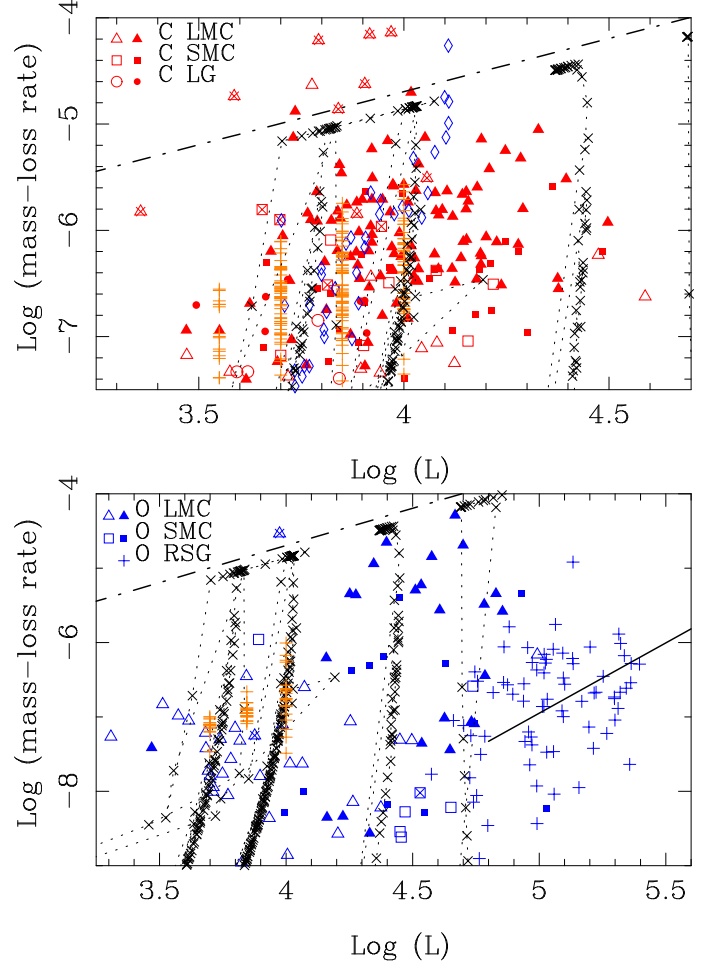


Fig. 7. Total MLR versus luminosity for C stars (top panel, red colors) and M stars (bottom panel, blue colors). Objects with Mira-like pulsation amplitudes are plotted with filled symbols; objects with smaller amplitudes with open symbols. An overplotted cross indicates no information on pulsation properties. Orange plus signs in the top panel indicate models by Eriksson et al. (2014) scaled to our adopted dust-to-gas ratio and expansion velocity (see text). Blue diamonds in the top panel indicate a sample of Galactic C Miras (see text). RSGs are plotted as plus signs independent of host galaxy and pulsation amplitude. Orange plus signs in the bottom panel indicate models by Bladh et al. (2015) scaled to our adopted dust-to-gas ratio and expansion velocity (see text). The VW models for LMC metallicity are plotted as crosses connected by the dotted lines for initial masses of 1.5, 2.5, 5.0 and 7.9 M_{\odot} , but not every track is visible in every panel. Each cross represents a time interval of 5000 years. The dot-dashed line shows the single scattering limit for a velocity of 10 km s^{-1} . The solid line is the relation found by Verhoelst et al. (2009) for Galactic RSGs.

is larger than the ~ 1 -1.5 dex scatter in the relation for Galactic RSGs.

The orange plus signs represent the recent dynamical models by Bladh et al. (2015) for M stars with masses of 1 M_{\odot} and solar metallicities. The models are available for 5000, 7000, and 10000 L_{\odot} and cover a range in effective temperatures, piston-velocity amplitudes and seed-particle densities.¹⁷ The plotted MLR is their value scaled to our adopted dust-to-gas ratio and expansion velocity. The differences are significant. The median values in the 56 models of dust-to-gas ratio (Ψ) and v_{exp} are 5.8

¹⁷ The models with seed-particle density 10^{-16} were not considered, as they do not fit the data considered by Bladh et al. very well (Bladh 2017, private communication).

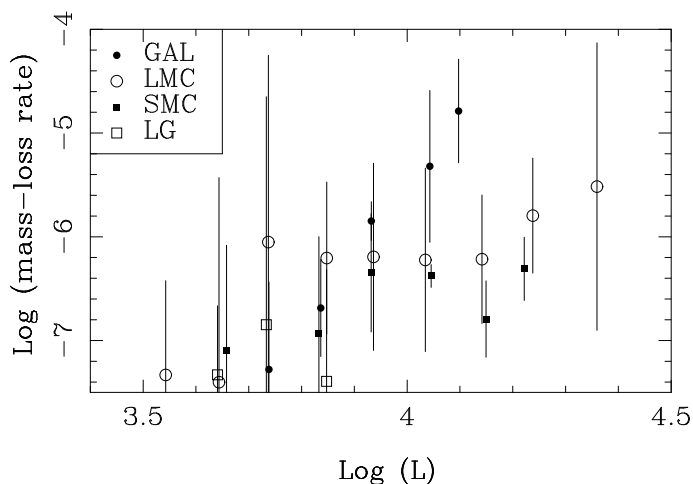


Fig. 8. Binned version of Fig. 7 for C stars.

$\cdot 10^{-4}$ and 10.4 km s^{-1} , respectively. The difference in Ψ is considerable, and their *calculated* MLRs are a median 1.1 dex above the scaled values plotted in Figure 7. A comparison to our determinations is difficult because of the difference in metallicity and mass, but the agreement is within an order of magnitude, which is encouraging given the fact that the driving of winds in M stars is a difficult problem (Woitke 2006, Höfner 2008).

The top panel of Figure 7 shows the results for the C stars. The orange plus signs are the results of the dynamical models at solar metallicity by Eriksson et al. (2014). From the 540 models they calculated we show the 193 models which result in a out-flow (not all models do), and then those with an expansion velocity larger than 5 km s^{-1} . The plotted MLR is their value scaled to our adopted dust-to-gas ratio and expansion velocity. This difference is significant. The median values for the 193 models of dust-to-gas ratio (Ψ) and v_{exp} are 0.0014 and 23.4 km s^{-1} , respectively, which differ considerably from our values. Their *calculated* MLRs lie a median 0.91 dex above the scaled values plotted in Figure 7, and reach and exceed the single-scattering limit (see below).

The different models at a given luminosity are related to differences in the other input parameters like effective temperature, overabundance of carbon, or velocity of the piston at the inner boundary of their models.

Figure 7 also includes Galactic stars (plotted as blue diamonds). The fitting for the Galactic targets was done using different software and dust opacities, which we can expect to lead to differences in derived MLRs (see Sec. 6.1). This sample includes three groups.

Groenewegen et al. (1998) modelled the SEDs and spectra of 42 Galactic carbon-rich Miras. In this case, the spectra were from the Low-Resolution Spectrometer (LRS) aboard the *Infrared Astronomical Satellite* (IRAS). Miras were chosen so that the period-luminosity relation could be used to estimate their distances, which are always a challenge for evolved stars in the Galaxy. As part of a different (unpublished) investigation, six stars in that sample covering a range of MLRs were fitted with MoD to derive the differences in MLRs, using updated photometry and where possible, spectra from the Short-Wavelength Spectrometer (SWS) aboard the *Infrared Space Observatory* (ISO). The third group comes from Groenewegen et al. (2016) who modelled some very red Galactic objects with MoD using the same method as in the present paper. That sample included three additional stars overlapping Groenewegen et al. (1998), and two

other stars. Thus the Galactic sample consists of 44 stars: 33 taken directly from the models by Groenewegen et al. (1998), nine from that sample based on updated models, and two additional stars.

The median ratio of the MLRs (old/new) is 3.8, and this is largely due to the change in optical constants (Groenewegen et al. 1998 also used the constants from Rouleau & Martin 1991). We have scaled the 33 old models by this median ratio. We have also scaled the MLRs of these stars to an expansion velocity of 10 km s^{-1} , as adopted in the rest of the sample. The stars follow a close relation which is due to the underlying adopted period-luminosity relation.

Compared to G09, the qualitative description of the comparison has changed. G09 found that only three C stars were slightly above the single-scattering limit, which they considered to be consistent with expectations.¹⁸ In the current picture, a significant number of C stars are above the single-scattering limit by up to a factor of 10. This in itself does not necessarily pose a significant issue. First, the MLRs have large uncertainties (and β , too, due to the assumed gas-to-dust ratio of 200 and expansion velocity of 10 km s^{-1}). Second, dynamical models show that $\beta > 1$ can be reached in realistic models. From a subset of 900 dynamical model atmospheres for carbon stars for solar metallicities from Mattsson et al. (2010), we find that the 98th percentile on β is 3.0. In the more recent models by Eriksson et al. (2014), the 98th percentile on β is 1.5. From dynamical model atmospheres for subsolar metallicities by Wachter et al. (2008) one might expect the value for β to be a factor 2.6 lower in the LMC, i.e. near 0.5-1.

If confirmed, our models show that the artificial cut-off in the VW models at $\beta = 1$ may be too conservative. A cut-off (if any) at a larger β would result in shorter AGB lifetimes.

Figure 8 presents the results differently, with the MLRs of the C stars binned and averaged for the SMC, LMC, dSph galaxies, and our Galaxy separately. The VW evolutionary tracks suggest that for a given mass, the luminosity evolves by about 0.1 dex on the AGB (Fig. 7), and as a consequence we chose this as the bin size in $\log L$. The MLRs in a luminosity bin are median averaged in $\log \dot{M}$ and are plotted in Fig. 8 at the average luminosity of the stars in that bin if a bin includes three or more objects. The error bar indicates the spread in the bins (as 1.5 times the median absolute deviation).

The MLR increases globally with luminosity, as also shown by the models by Eriksson et al. (2014). Any dependence on metallicity remains difficult to assess. The issue of accurate distances (hence luminosities) remains a limiting factor for any Galactic sample. The models in the present work point to a larger dust MLR in the LMC than in the SMC for a given luminosity, but this could also arise from the difference in the underlying populations (see below) and/or differences in expansion velocity.

Groenewegen et al. (2016) determined for the first time the expansion velocity of four C stars in the LMC by detecting the CO J=2-1 transition using the Atacama Large-Millimeter Array (ALMA). All four of these stars are in the present sample: IRAS 05506, IRAS 05125, ERO 0529379, and ERO 0518117. They compared these objects to the closest available analogs in the Galaxy and found that the expansion velocity in the LMC appears to be smaller than in the Galaxy. The key caveat, though,

¹⁸ The single-scattering limit applies when $\beta = 1$, where $\beta \equiv (\dot{M}v_{\text{exp}})/(L/c)$, the ratio of the matter-momentum flux to the photon-momentum flux.

is that the samples are small, and it is difficult to find suitable comparison objects in the two galaxies.

Figure 7 shows clearly that between the LMC and SMC, the stars with the heaviest mass loss are located in the LMC. This result does not appear to result from a bias in the spectroscopic sample observed by the IRS. Plotting color-magnitude diagrams (CMDs) of photometric samples in the mid-IR reveals more intrinsically red AGB stars in the LMC compared to the SMC (Fig. 5 from Ventura et al. 2016, and references therein). Comparison to models shows that the largest degree of obscuration in the LMC and SMC occurs for stars with an initial mass of 2–3 M_{\odot} and about 1.5 M_{\odot} , respectively, a difference which Ventura et al. (2016) attribute to differences in the star formation histories of the two galaxies. Such differences between the populations in the LMC and SMC make it difficult to draw any firm conclusions about how the MLR depends on metallicity.

6.3. A super-AGB star candidate

G09 suggested that MSX SMC 055 (or IRAS 00483–7347) is a good candidate for a super-AGB (SAGB) star, based on its high luminosity ($M_{\text{bol}} = -8.0$), its very long pulsation period (1749 days) and large pulsation amplitude (1.6 mag peak-to-peak in I). Its pulsational properties distinguish it from a luminous RSG. Here we present improved estimates for its parameters.

Groenewegen & Jurkovic (2017) derived a relation between period, luminosity, mass, temperature, and metallicity based on the 5–11 M_{\odot} initial-mass Cepheid models by Bono et al. (2000). For the parameters $P = 1810 \pm 50$ days, $L = 85350 \pm 8500 L_{\odot}$, $T_{\text{eff}} = 2500 \pm 100$ K, and $Z = 0.004 \pm 0.001$ (errors are adopted), we derive a current pulsation mass of $8.5 \pm 1.6 M_{\odot}$ with the total error in mass dominated by the error in effective temperature. The simpler period-mass-radius relation for fundamental-mode Mira pulsators from Wood (1990) gives a similar value of $9.2 \pm 1.8 M_{\odot}$.

The current MLR is estimated to be $4.5 \cdot 10^{-6} M_{\odot} \text{ yr}^{-1}$, assuming a conservative gas-to-dust ratio of 200. Roman-Duval et al. (2014) estimate a value in the ISM in the SMC of 1200^{+1600}_{-420} which implies the MLR could be larger by a factor of a few. Lifetimes in the thermal-pulsing phase are short in SAGB stars (10^4 – 5 years; e.g. the review by Doherty et al. 2017), but these lifetimes in combination with a MLR that could exceed $10^{-5} M_{\odot} \text{ yr}^{-1}$ indicate that the initial mass of MSX SMC 055 could very well be up to 1 M_{\odot} larger than its current mass.

García-Hernández et al. (2009) observed this and other massive AGB star candidates in the MCs in the optical at high spectral resolution. MSX SMC 055 is very rich in rubidium, Rb, with $[\text{Rb}/\text{Z}] \gtrsim +1.7$, which confirms the activation of the ^{22}Ne neutron source at the s -process site and its massive AGB or SAGB nature. Indeed, by comparing these observations to models, they independently suggested an initial mass of at least 6–7 M_{\odot} for this star.

MSX SMC 055 remains the most viable SAGB star candidate in the SMC and LMC.

6.4. The potential of JWST

The James Webb Space Telescope (JWST), due for launch in 2019, provides impressive filter sets on its two imaging instruments, NIRCAM and MIRI, which will enable broadband photometric studies of the evolved stellar population in galaxies out to distances of a few Mpc. At least two published papers have already investigated which filter combinations look to be most

useful for distinguishing and characterising different classes of objects.

Kraemer et al. (2017) examined the sample of SMC objects observed by the IRS, using the spectra to confirm the classifications. They found that the 5.6, 7.7, and 21 μm filters best separated C-rich from O-rich stars, while the 5.6, 10, and 21 μm filters best separated young stellar objects (YSOs) from planetary nebulae (PNe). Jones et al. (2017a) performed a similar study using over 1000 sources with IRS spectra in the LMC. They discussed how to discriminate O- and C-rich AGB and post-AGB stars, RSG, HII regions, PNe and YSOs. Both Kraemer et al. and Jones et al. based their CMDs and CCDs on synthetic photometry using the IRS spectra. Therefore, they were limited in showing diagrams based on MIRI filters. In Appendix ?? we present synthetic photometry for the sample of almost 400 evolved stars in about 75 filters, including the 29 medium and wide-band filters available with the NIRCAM and MIRI instruments.

Figure 9 gives two examples. The first is a CMD resembling the near-infrared and IRAC [3.6] versus J –[3.6] diagram shown by G09 (SMC objects have been placed at the distance of the LMC). In this diagram, the dustiest AGB stars show a relatively small spread in F360W magnitude and the reddest objects are predominantly C-rich. The second example is a CCD resembling the [5.8]–[8.0] versus [8.0]–[24] diagram shown in Fig. 1 which separates O-rich and C-rich very well. Replacing the F1800W filter by F2100W or F2550W yields similar plots, but for a given integration time and signal-to-noise F1800W is a magnitude more sensitive than F2100W and almost 3 magnitudes more sensitive than F2550W (Jones et al. 2017a). Thus for AGB stars, we recommend the 5.6, 7.7, and 18 μm filters to discriminate O-rich from C-rich stars.

7. Summary and conclusions

We have fitted the SEDs and IRS spectra of almost 400 evolved stars in the SMC and LMC with a dust radiative-transfer model to determine luminosities and (dust) mass-loss rates. The mass-loss rates depend strongly on the adopted opacities (that is, the optical constants, and to a lesser extent the grain shape).

A comparison to results in the literature shows that for M stars the choice of optical constants based on laboratory measurements leads to lower MLRs than those derived from observations (so called, astronomical silicates) as employed in the widely used GRAMS models. When using laboratory-determined optical constants, the iron content that is assumed or derived becomes important and introduces a factor of 2 uncertainty.

For C stars the choice between the widely used optical constants by Rouleau & Martin (1991) and Zubko et al. (1996) introduces a difference in MLR of a factor of ~ 5 or more. Comparison with the literature suggests that differences in the allowed inner radius in the radiative transfer modelling may also introduce a factor of two uncertainty in the derived MLR.

All of these uncertainties impact the estimates of the total gas and dust return of evolved stars in the MCs (see the references in Section 5.3). The differences in opacities are the greater problem, and the solution lies in a better determination of what circumstellar grains actually look like. While this paper does not offer any solutions to the problem, we hope that we have helped to better frame the problem and its consequences on our understanding of the role played by AGB stars in galactic evolution.

Also of interest are the particular cases of the half-dozen sources with the largest optical depths. They are not the most luminous sources. Groenewegen et al. (2016) and Sloan et al.

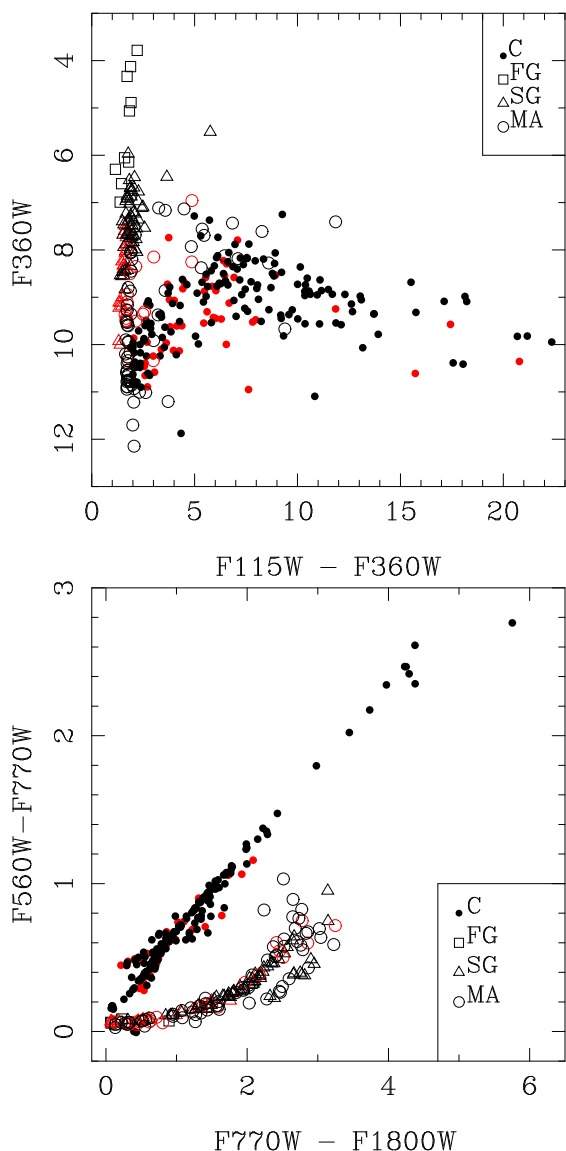


Fig. 9. Colour-Magnitude and Colour-Colour diagrams for the LMC (with the SMC stars, plotted in red, shifted to the distance of the LMC) based on synthetic JWST NIRCAM/MIRI magnitudes.

(2016) discussed their evolutionary status. Evolutionary models using the COLIBRI formalism described by Marigo et al. (2013) (see additional detail by Groenewegen et al. 2016) agree with Ventura et al. (2016) that these stars began their lives with initial masses of $2\text{--}3 M_{\odot}$, but have had their envelope masses reduced to $\lesssim 1 M_{\odot}$ through the mass-loss process. The low envelope mass is necessary to explain their long pulsation periods (often longer than 1000 days). Not all of the reddest stars have had their pulsation properties determined, which would clearly be an important contribution. Sloan et al. (2016) noted that the reddest sources showed decreased variability and evidence that radiation from the central star may be escaping the otherwise optically thick dust shell. Both behaviors are consistent with evolution off of the AGB. The unusual blue colors suggest that these stars may also be departing from spherical symmetry, in which case our radiative-transfer models could be underestimating their luminosity. These may be the sources at the very end of their AGB lifetimes, and we need better observational constraints on their geometry and outflows.

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Appendix A: The sample

Tables A.1 and A.2 list the samples of C-rich and O-rich stars, with basic information: some common names (as listed by SIMBAD), R.A. and declination in decimal degrees, the identifier used in figures and tables below (where we almost always kept the target name used in the original observation), the adopted pulsation period, the (semi-)amplitude and in which filter. For the oxygen-rich stars a classifier is added (FG=Foreground, SG=Supergiant, MA=M-type AGB-star). The C-stars are listed in order of R.A., but with the stars in the dSph galaxies listed last. For the O-rich stars the foreground objects are listed before the SGs and the AGB stars, and then by R.A. Various criteria have been used to distinguish between foreground, supergiant and O-rich AGB stars; see G09 for details. Compared to G09 only one additional FG object was added HD 269924, which is a K5 star with a significant proper motion. The distinction between SG and MA is sometimes not clear-cut, but our conclusions do not depend on the misclassification of a few objects.

Figure A.1 shows one diagnostic that was used, the period-luminosity diagram, with additional information from the pulsation amplitude and colour.

To quantify the impact of misclassifications, we compared our classifications to those from Jones et al. (2012). Of the 46 stars they classified as O-AGB, we classified 1 as SG, and 2 as C-rich. Of the 68 stars they classified as RSGs, we classified 7 as MA. We also compared our classifications to those from Ruffle et al. (2015), Woods et al. (2011), and Jones et al. (2017b). Of the 18 stars we classified as O-AGB, Ruffle et al. classified 2 as SG. Of the 21 stars we classified as RSGs, they classified 3 as MA. Of the 39 stars we classified as O-AGB, Woods et al. (2011) classified 0 as SG. Of the 13 stars we classified as RSGs, they classified 0 as MA. Of the 63 stars we classified as O-AGB, Jones et al. (2017b) classified 3 as SG. Of the 57 stars we classified as RSGs, they classified 1 as MA. The differences arise mainly because we did not strictly enforce the classic AGB luminosity limit of $M_{\text{bol}} = -7.1$ mag. This comparison shows that the probability of misclassification is $\sim 5\text{--}10\%$.

Appendix B: Mass-loss rates, luminosities, and fits to the SEDs

Tables B.1 and B.2 list the parameters of the models which best fit the observed data. These include the identifier, information on the atmospheric model used (effective temperature, $\log g$, and for the C stars, C/O ratio), grain size and dust type, luminosity, dust optical depth in the V -band, mass-loss rate, whether τ was fitted (1) or fixed (0), T_c , whether T_c was fitted or fixed, the slope of the density law, whether p was fitted or fixed, outer radius (in units of inner radius), and the reduced χ^2 .

The reduced chi-square value is given for reference only. There is a large range in values, and sometimes the values are far larger than unity. This is in part related to the construction of the SED and the available photometry (and error) which can be very different across sources, and the role of variability.

Figures ?? and ?? show the best-fitting models, and give a subjective indication of the quality of the fits. The top panel shows the observed SED and IRS spectrum and the fitted model on an absolute scale, while the bottom panel shows the IRS spectrum and the model (the blue line), scaled to a quasi-continuum point based on the average flux in the $6.35\text{--}6.55\ \mu\text{m}$ region. Horizontal lines near the bottom indicate wavelength regions excluded from the fit.

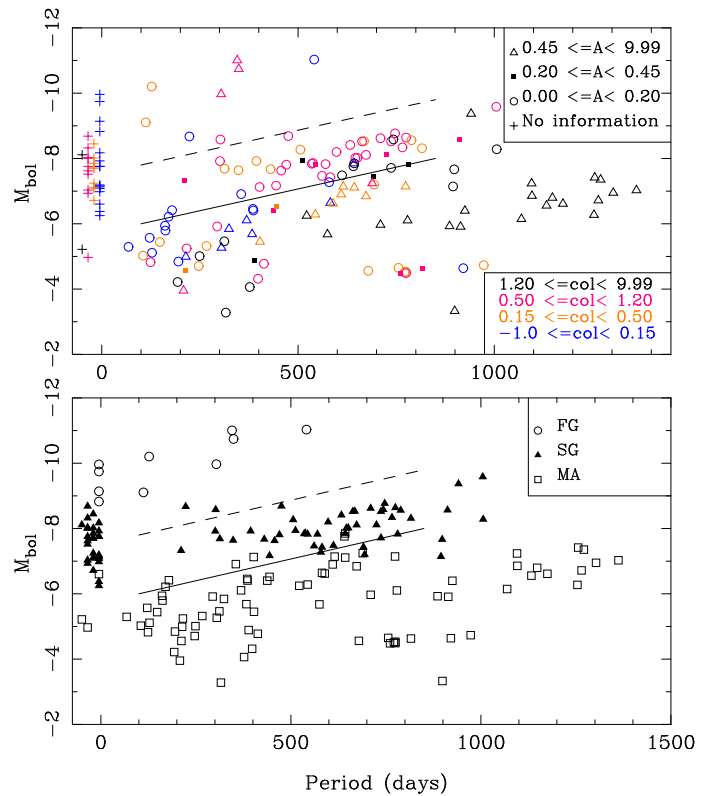


Fig. A.1. Bolometric magnitude versus pulsation period for the O-rich stars. Stars without periods are plotted as plus signs at negative periods. The solid line indicates the lower luminosity limit for RSGs by WBF, and the dashed line is 1.8 mag brighter. *Top panel.* The legend indicates the meaning of the symbols in terms of the I -band semi-amplitudes (A), and $[3.6]\text{--}[8.0]$ colours. *Bottom panel.* As top panel, but the objects are identified as foreground objects (open circles), RSG (filled triangles), and AGB stars (open squares).

Table A.1. Carbon star sample.

Names	R.A.	Declination	Identifier	Period	Amp (Filter)	Ref. ^a	Remarks
GM 780, MACHO 213.15051.6	8.905250	-73.165583	gm780	611	0.75 (<i>I</i>)	1	
MSX SMC 029	9.192958	-73.526417	msxsmc029				
MSX SMC 091	9.236292	-72.421528	msxsmc091	405	0.57 (<i>K</i>)	2	
IRAS 00350-7436	9.248792	-74.330639	iras00350				
MSX SMC 062, OGLE J004240.89-725705.1	10.670417	-72.951583	msxsmc062	548	0.86 (<i>I</i>)	1	
MSX SMC 054, MACHO 213.15504.265	10.774699	-73.361268	msxsmc054	390	0.27 (<i>I</i>)	1	
2MASS J00432649-7326433	10.860361	-73.445350	j004326	327	0.11 (<i>I</i>)	1	
MSX SMC 044, OGLE J004339.58-731457.1	10.914875	-73.249333	msxsmc044	441	0.60 (<i>I</i>)	1	
2MASS J00445256-7318258	11.219005	-73.307186	j004452	158	0.06 (<i>I</i>)	1	
MSX SMC 105, OGLE J004502.14-725223.8	11.258917	-72.873417	msxsmc105	652	0.93 (<i>I</i>)	1	
MSX SMC 036, OGLE J004553.92-732340.7	11.474750	-73.394750	msxsmc036	555	0.85 (<i>I</i>)	1	
MSX SMC 014	11.568042	-74.187111	msxsmc014	361	1.05 (<i>I</i>)	1	
MSX SMC 060, OGLE 004640.46-731646.9	11.668417	-73.279778	msxsmc060	431	0.41 (<i>I</i>)	1	
MSX SMC 200, smc102.5_195	11.711583	-71.794250	msxsmc200	433	0.36 (<i>I</i>)	1	
MSX SMC 033, OGLE J004705.55-732132.5	11.773000	-73.359167	msxsmc033	532	0.88 (<i>I</i>)	1	
SSTISAGEMA J004720.02-724035.1	11.833320	-72.676390	j004720	144	0.05 (<i>I</i>)	1	
MSX SMC 66, OGLE J004852.51-730856.5	12.218750	-73.149111	msxsmc066	523	0.46 (<i>I</i>)	1	
2MASS J00485947-7335387	12.247937	-73.594118	irasf00471	687	0.97 (<i>I</i>)	1	
CV 78, MACHO 212.15907.1	12.265958	-73.088833	cv78	435	0.75 (<i>I</i>)	1	
RAW 594	12.535420	-72.838940	raw594	140	0.06 (<i>I</i>)	1	
MSX SMC 163, MACHO 208.16031.578	12.753083	-72.421806	msxsmc163	672	0.87 (<i>I</i>)	1	
MSX SMC 142, OGLE J005140.46-725728.5	12.918625	-72.958028	msxsmc142	293	0.76 (<i>I</i>)	1	
MSX SMC 125	12.958690	-72.847080	msxsmc125	458	0.84 (<i>I</i>)	1	
MSX SMC 162, OGLE J005240.16-724727.3	13.167375	-72.791000	msxsmc162	535	0.51 (<i>I</i>)	1	
MSX SMC 202, smc102.1_11605	13.292208	-72.198528	msxsmc202	486	0.32 (<i>I</i>)	1	
MSX SMC 159, OGLE 005422.28-724329.7	13.592830	-72.724940	msxsmc159				
LEGC 105, OGLE J005446.85-731337.6	13.695184	-73.227182	legc105	349	0.62 (<i>I</i>)	1	
OGLE 005450.73-730607.2	13.711458	-73.102028	iso00548	430	0.90 (<i>I</i>)	1	
OGLE 005454.09-730318.0	13.725417	-73.055028	iso00549	546	0.56 (<i>I</i>)	1	
RAW 960, OGLE J005554.61-731136.3	13.977620	-73.193470	raw960	315	0.62 (<i>I</i>)	1	
MSX SMC 209, MACHO 207.16376.687	14.068292	-72.278139	msxsmc209	510	0.80 (<i>I</i>)	1	
OGLE SMC-SC7 204803	14.073042	-72.451194	s3mc204803	194	0.07 (<i>I</i>)	1	
IRAS 00554-7351, [GB98] S16	14.266458	-73.587389	iras00554	851	0.83 (<i>I</i>)	1	
MSX SMC 198, OGLE J005710.97-723059.7	14.295750	-72.516639	msxsmc198	512	0.85 (<i>I</i>)	1	
MSX SMC 155	14.325625	-72.709778	msxsmc155				
2MASS J00572054-7312460	14.335583	-73.212778	iso00573	352	0.60 (<i>I</i>)	1	
MSX SMC 093, smc107.2_23	14.847333	-73.933611	msxsmc093	463	0.30 (<i>I</i>)	1	
OGLE 010154.53-725822.1	15.477417	-72.972861	iso01019	337	0.51 (<i>I</i>)	1	
2MASS J01045315-7204039	16.221485	-72.067774	j010453				
MSX SMC 232, OGLE J010603.28-722231.9	16.513750	-72.375611	msxsmc232	460	0.64 (<i>I</i>)	1	
NGC 419 LE 16, smc110.2_6965	17.004750	-72.888139	ngc419le16	424	0.25 (<i>I</i>)	1	
NGC 419 IR1, OGLE J010812.92-725243.7	17.054000	-72.878890	ngc419ir1	456	0.43 (<i>I</i>)	1	
NGC 419 LE 35	17.072880	-72.883720	ngc419le35	173	0.08 (<i>I</i>)	1	
NGC 419 MIR 1	17.073000	-72.885889	ngc419mir1	738	0.75 (<i>K</i>)	3	
NGC 419 LE 27, smc110.2_6915	17.086080	-72.881140	ngc419le27	305	0.08 (<i>I</i>)	1	
NGC 419 LE 18, smc110.2_6943	17.103958	-72.882472	ngc419le18	371	0.07 (<i>I</i>)	1	
IRAS 04286-6937, MSX LMC 1007	67.125750	-69.513944	iras04286	662	0.56 (<i>K</i>)	4	
2MASS J04325737-6926331, MSX LMC 1008	68.239083	-69.442528	iras04331	673	0.50 (<i>W2</i>)	5	
2MASS J04334368-7009504, MSX LMC 1077	68.432042	-70.164028	iras04340	441	1.08 (<i>I</i>)	1	
2MASS J04352409-6656493, MSX LMC 1017	68.850417	-66.947028	iras04353	582	0.75 (<i>K</i>)	2	
2MASS J04364447-7242010, MSX LMC 1067	69.185333	-72.700278	iras04375	246	0.50 (<i>W2</i>)	5	
IRAS 04374-6831, MSX LMC 1042	69.344667	-68.417583	iras04374	639	0.71 (<i>K</i>)	4	
2MASS J04425732-7012257, MSX LMC 1075	70.738875	-70.207167	iras04433	486	0.87 (<i>I</i>)	1	
2MASS J04462712-6847469	71.613042	-68.796361	sagemcj044627	389	0.91 (<i>I</i>)	1	
MSX LMC 1120, lmc141.5_9241	71.817042	-68.407111	msxlmc1120	639	0.83 (<i>I</i>)	1	
IRAS 04496-6958, MSX LMC 1130	72.327000	-69.887361	iras04496	721	0.21 (<i>I</i>)	1	
MSX LMC 1128	72.668917	-68.971972	msxlmc1128	442	0.68 (<i>I</i>)	1	
MSX LMC 1308, lmc135.7_3454	72.795667	-69.337389	msxlmc1308	535	0.57 (<i>I</i>)	1	
MSX LMC 1205, lmc134.7_17633	72.814500	-68.694528	msxlmc1205	569	0.94 (<i>I</i>)	1	
IRAS 04518-6852, MSX LMC 1201	72.919177	-68.792953	iras04518	786	0.89 (<i>W2</i>)	5	

Table A.1. Carbon star sample: continued.

Names	R.A.	Declination	Identifier	Period	Amp (Filter)	Ref. ^a	Remarks
MSX LMC 1213	73.084042	-68.725028	msxlmc1213	478	0.72 (<i>K</i>)	2	
[KDM2001] 764	73.135500	-67.049833	kdm764	453	0.10 (<i>I</i>)	1	
2MASS J04532871-6603343	73.369667	-66.059555	sagemcj045328	399	0.30 (<i>R</i>)	6	
IRAS 04535-6616, MSX LMC 1111	73.434333	-66.196139	sagemcj045344	764	0.67 (<i>W2</i>)	5	
IRASF 04538-6820, MSX LMC 1198	73.443250	-68.270240	iras04538	669	0.61 (<i>W2</i>)	5	
IRAS 04537-6922, MSX LMC 1191	73.506708	-65.081139	iras04537	505	0.84 (<i>R</i>)	7	
MSX LMC 1209, lmc134.2_9194	73.828625	-68.775167	msxlmc1209	571	0.79 (<i>I</i>)	1	
IRAS 04557-6952	73.912417	-67.819639	iras04557	765	0.68 (<i>K</i>)	4	
MSX LMC 1298, lmc134.1_40407	74.133958	-68.880833	msxlmc1298	673	1.02 (<i>I</i>)	1	
2MASS J04584626-6820429	74.691776	-68.343849	iras04589	765	0.67 (<i>W2</i>)	5	
[KDM2001] 1238	74.729292	-69.188500	kdm1238	133	0.06 (<i>I</i>)	1	
2MASS J05003226-7209023, MSX LMC 178	75.134459	-72.150639	iras05013	550	0.73 (<i>K</i>)	2	
MSX LMC 1282, lmc124.7_14426	75.253625	-67.589889	msxlmc1282	637	1.05 (<i>I</i>)	1	
IRAS 05009-6616, MSX LMC 1278	75.268417	-66.211194	iras05009	658	0.82 (<i>K</i>)	4	
SSTISAGE1C J050231.47-680535.9	75.631170	-68.093220	ERO0502315				
[KDM2001] 1656, MACHO 55.3736.12	75.819292	-65.829167	kdm1656	249	0.07 (<i>R</i>)	6	
[KDM2001] 1691	75.903917	-68.560694	kdm1691	529	0.21 (<i>I</i>)	1	
LMC-BM 11-19	75.927458	-67.988667	lmc-bm11-19	98	0.01 (<i>I</i>)	1	
LMC-BM 12-14, [KDM2001] 1722	75.972542	-70.463222	lmc-bm12-14	220	0.12 (<i>I</i>)	1	
IRAS 05042-6827	76.023300	-68.394520	ERO0504056				
NGC 1818 WBT64	76.032242	-66.418289	ngc1818wbt64	166	0.06 (<i>R</i>)	7	
OGLE LMC-LPV-16169	76.263375	-69.407361	sagemcj050503	247	0.08 (<i>I</i>)	1	
IRAS 05053-6901, MSX LMC 84	76.270124	-68.963437	iras05053	944	0.74 (<i>W2</i>)	5	
LMC-BM 13-2, [KDM2001] 1924	76.482000	-67.369444	lmc13_2	898	0.28 (<i>I</i>)	1	
2MASS J05060754-7141482	76.531417	-71.696750	sagemcj050607	342	0.67 (<i>R</i>)	7	
[KDM2001] 1961	76.552500	-64.927111	kdm1961	482	0.04 (<i>R</i>)	7	
[KDM2001] 1966	76.579083	-64.936167	kdm1966	176	0.06 (<i>R</i>)	7	
2MASS 05062012-6454585	76.583875	-64.916278	sagemcj050620	189	0.12 (<i>R</i>)	7	
2MASS J05062960-6855348	76.623333	-68.926333	sagemcj050629	156	0.04 (<i>I</i>)	1	
IRAS 05070-7020, MSX LMC 200	76.646292	-70.280611	iras05070	560	0.50 (<i>K</i>)	2	
SHV 0507252-690238	76.789167	-68.980389	shv0507252	525	0.41 (<i>I</i>)	1	
2MASS J05075293-6812464	76.970542	-68.212917	sagemcj050752	302	1.06 (<i>I</i>)	1	
MSX LMC 92	77.106522	-68.899963	msxlmc92	536	0.89 (<i>I</i>)	1	
OGLE LMC-LPV-20709	77.109917	-68.520833	sagemcj050826	418	0.64 (<i>I</i>)	1	
[KDM2001] 2187	77.151833	-69.720972	kdm2187	820	0.25 (<i>I</i>)	1	
MSX LMC 95, lmc112.7_9825	77.499958	-69.936028	msxlmc95	608	1.01 (<i>I</i>)	1	
MSX LMC 87, lmc112.6_11178	77.581750	-69.830944	msxlmc87	622	1.00 (<i>I</i>)	1	
sage1cj051028	77.618134	-68.742065	sage1cj051028	466	0.90 (<i>I</i>)	1	
IRAS 05112-6755, MSX LMC 44, TRM 4	77.793625	-67.869583	iras05112	830	0.93 (<i>K</i>)	9	
IRAS 05113-6739, TRM 24	77.807833	-67.604472	iras05113	698	1.10 (<i>I</i>)	1	
MSX LMC 219	77.831415	-68.707676	msxlmc219	706	0.67 (<i>K</i>)	2	
TRM 72, MSX LMC 29, MACHO 56.5052.258	77.911000	-66.852722	trm72	533	1.08 (<i>I</i>)	1	
IRAS 05125-7035, MSX LMC 196	78.003208	-70.540000	iras05125	1115	0.61 (<i>K</i>)	2	
MSX LMC 220, OGLE 051232.15-691540.6	78.133583	-69.261222	msxlmc220	632	0.54 (<i>I</i>)	1	
IRAS 05132-6941, MSX LMC 223	78.212750	-69.630611	iras05132	666	0.82 (<i>K</i>)	2	
IRAS 05133-6937	78.257471	-69.564111	iras05133				
OGLE J051306.52-690946.4	78.276750	-69.162833	ogle051306	359	0.84 (<i>I</i>)	1	
MSX LMC 218, lmc110.2_244	78.318333	-68.736083	msxlmc218	654	0.76 (<i>I</i>)	1	
HV 5680	78.624411	-68.909459	hv5680	104	0.02 (<i>I</i>)	1	
MSX LMC 349	79.362266	-68.916258	msxlmc349	587	0.75 (<i>K</i>)	2	
SSTISAGE1C J051803.23-684950.7	79.513710	-68.830720	sagemcj051803	352	0.50 (<i>I</i>)	1	
[KDM2001] 3196	79.533125	-71.864916	kdm3196	118	0.02 (<i>I</i>)	1	
IRAS 05187-7033	79.548780	-70.507500	ERO0518117				
2MASS J05183266-6925253	79.636125	-69.423694	sagemcj051832	173	0.09 (<i>I</i>)	1	
IRAS 05191-6936	79.701450	-69.559660	ERO0518484				
IRAS 05190-6748, MSX LMC 307, TRM 20	79.734417	-67.751194	iras05190	945	0.78 (<i>K</i>)	9	
OGLE LMC-LPV-40384	79.785375	-69.387278	sagemcj051908	189	0.08 (<i>I</i>)	1	
2MASS J05191049-6933453	79.793750	-69.562583	2massj051910	475	0.10 (<i>I</i>)	1	
TRM 88, MSX LMC 310, MACHO 58.6508.122	80.080750	-66.596611	trm88	549	0.76 (<i>R</i>)	7	
MSX LMC 439	80.200869	-70.203495	msxlmc439				R CrB
MSX LMC 341	80.251542	-69.348667	msxlmc341	572	0.77 (<i>K</i>)	2	

Table A.1. Carbon star sample: continued.

Names	R.A.	Declination	Identifier	Period	Amp (Filter)	Ref. ^a	Remarks
HV 942, MACHO 6.6696.60	80.449850	-70.165840	hv942				R CrB
MSX LMC 527	80.582313	-65.721920	msxlmc527				
OGLE J052242.09-691526.2	80.674958	-69.257222	ogle052242	418	0.79 (I)	1	
MSX LMC 663, OGLE 052244.13-693828.3	80.683292	-69.641111	msxlmc663	1338	0.02 (I)	1	
MSX LMC 494	80.787833	-69.296347	msxlmc494	439	0.67 (I)	1	
2MASS J05233832-6653246, MSX LMC 513	80.909660	-66.890270	iras05236	754	0.97 (K)	2	
SSTM1SAGE1 J052405.23-681802.4	81.022208	-68.300694	sagemcj052405	328	0.61 (I)	1	
MSX LMC 441	81.160917	-70.399194	msxlmc441	671	0.77 (K)	2	
MSX LMC 428	81.182042	-71.790694	iras05254	685	0.53 (W2)	5	
OGLE J052445.53-691605.6	81.189208	-69.268139	ogle052445	403	0.78 (I)	1	
MSX LMC 443	81.273667	-70.169611	msxlmc443	535	0.66 (K)	2	
MSX LMC 438, lmc164.7_40522	81.331292	-71.067417	msxlmc438	561	0.58 (I)	1	
IRAS 05260-7010	81.419530	-70.140850	ERO0525406				
MSX LMC 474	81.466049	-68.776199	msxlmc474	632	0.76 (I)	1	
WBP 17, OGLE J052620.01-694137.5	81.582792	-69.693694	wbp17	316	0.47 (I)	1	
MSX LMC 774	81.596208	-69.188944	msxlmc774	670	0.78 (K)	2	
MSX LMC 634, lmc161.3_58817	81.648708	-69.139639	msxlmc634	490	0.68 (I)	1	
WBP 29	81.670624	-69.386505	wbp29	247	0.58 (I)	1	
MSX LMC 601, OGLE J052650.96-693136.8	81.711750	-69.526889	msxlmc601	560	1.22 (I)	1	
WBP 42, OGLE J052704.87-693816.4	81.769708	-69.637833	wbp42	396	0.48 (I)	1	
WBP 51	81.827210	-69.606720	wbp51	390	0.14 (I)	1	
IRAS 05278-6942, MSX LMC 635	81.850458	-69.662472	iras05278	1001	1.28 (K)	2	
SHV 0528350-701014	82.024625	-70.131555	shv0528350	474	0.35 (I)	1	
MSX LMC 754, MACHO 7.7779.1137	82.047833	-70.566278	msxlmc754	461	0.79 (I)	1	
[KDM2001] 4257	82.107583	-69.779833	ogle052825	134	0.03 (I)	1	
WBP 104	82.109167	-69.245278	wbp104	245	0.45 (I)	10	S-star (WBP)
NGC 1978 IR1	82.167375	-66.231861	ngc1978ir1	450	0.77 (R)	6	
NGC 1978 IR4	82.185417	-66.234444	ngc1978ir4	473	0.25 (R)	6	
IRAS 05295-7121, MSX LMC 692	82.194208	-71.320139	iras05295	639	0.78 (I)	1	
NGC 1978 MIR 1	82.196253	-66.237190	ngc1978mir1	376	0.60 (K)	3	
MSX LMC 679, IRAS 05292-6950	82.202542	-69.800361	msxlmc679	485	0.66 (K)	2	
GRRV 38, RGC 54	82.281587	-66.970846	grrv38	494	0.48 (R)	7	
IRAS 05305-7251, MSX LMC 723	82.407860	-72.831360	ERO0529379	680	0.48 (W2)	5	
IRAS 05300-6651, MSX LMC 560, TRM 79	82.516208	-66.823389	iras05300	708	0.82 (K)	9	
IRAS 05306-7032, MSX LMC 652	82.526010	-70.511410	iras05306	806	0.52 (K)	2	
IRAS 05315-7145	82.683780	-71.716840	iras05315				
[KDM2001] 4554	82.687443	-68.358087	kdm4554	421	0.82 (I)	1	
MSX LMC 841	82.804625	-66.161417	msxlmc841	672	0.63 (K)	2	
MSX LMC 768, OGLE 053141.04-693919.7	82.920375	-69.655500	msxlmc768	630	0.92 (I)	1	
[KDM2001] 4665, MACHO 35.8352.3	82.995584	-72.743361	kdm4665	205	0.08 (R)	7	
MSX LMC 782, lmc168.2_44882	83.013792	-69.291778	msxlmc782	484	0.93 (I)	1	
[KDM2001] 4718	83.110542	-73.168583	kdm4718	310	0.13 (R)	7	
[KDM2001] 4774	83.229208	-67.613111	kdm4774	147	0.06 (R)	7	
MSX LMC 783, lmc168.2_12726	83.231125	-69.340722	msxlmc783	515	0.79 (I)	1	
MSX LMC 775, lmc166.2_19640	83.234083	-68.213528	msxlmc775	284	0.35 (I)	1	
MSX LMC 736	83.278464	-70.509414	msxlmc736	683	0.56 (W2)	5	
2MASS J05331859-6600401	83.327458	-66.011167	sagemcj053318	440	0.72 (R)	7	
IRAS 05348-7024, MSX LMC 733	83.566588	-70.381279	iras05348	798	1.04 (K)	2	
2MASS J05344142-6926307	83.672580	-69.441860	sagemcj053441	516	0.43 (I)	1	
MSX LMC 743	83.723875	-70.490194	msxlmc743	550	0.67 (K)	2	
MSX LMC 787	83.734208	-69.154583	msxlmc787	644	0.70 (K)	2	
MSX LMC 950, OGLE J053503.72-695245.3	83.764750	-69.879278	msxlmc950	557	0.89 (I)	1	
MSX LMC 796, lmc169.3_47356	83.833333	-69.812722	msxlmc796	178	0.07 (I)	1	
MSX LMC 749, OGLE J053527.04-695227.8	83.861917	-69.874417	msxlmc749	545	0.86 (I)	1	
2MASS J05353972-6519564, MSX LMC 862	83.915500	-65.332333	iras05355	513	0.71 (R)	7	
IRAS 05360-6648, MSX LMC 872, TRM 77	84.005125	-66.777667	iras05360	527	0.64 (K)	2	
2MASS J05362413-7241324, MSX LMC 721	84.100542	-72.692361	iras05373	642	0.67 (K)	2	
MSX LMC 967, OGLE J053636.92-694722.3	84.153170	-69.789560	msxlmc967	532	0.86 (I)	1	
[KDM2001] 5345, MACHO 66.9419.10	84.598333	-66.150111	kdm5345	217	0.06 (R)	7	
OGLE J053930.16-695755.8	84.874958	-69.965500	ogle053930	400	0.64 (I)	1	
MSX LMC 971	84.966000	-70.021389	msxlmc971	656	0.87 (K)	2	

Table A.1. Carbon star sample: continued.

Names	R.A.	Declination	Identifier	Period	Amp (Filter)	Ref. ^a	Remarks
MSX LMC 1400	85.085708	-66.245611	msxlmc1400	666	0.40 (W2)	5	
MSX LMC 937, IRAS 05410-6954	85.150250	-69.880500	msxlmc937	663	0.65 (I)	1	
MSX LMC 974, lmc176.2_54243	85.242417	-69.886833	msxlmc974	516	0.95 (I)	1	
IRAS 05416-6906	85.336375	-69.078805	iras05416	887	0.92 (W2)	5	
MSX LMC 1795	85.591250	-69.049750	msxlmc1795	154	0.63 (I)	1	R CrB
[KDM2001] 5841	85.870000	-69.712167	kdm5841	207	0.04 (I)	1	
MSX LMC 1384, OGLE J054336.19-701035.2	85.900083	-70.176417	msxlmc1384	554	0.99 (I)	1	
MSX LMC 1383, IRAS 05446-6945	86.056992	-69.738434	msxlmc1383	490	0.88 (K)	2	
SSTM1SAGE1 J054437.86-673657.9	86.157792	-67.616000	sagemcj054437	367	0.79 (R)	7	
sagemcj054546	86.443077	-67.544258	sagemcj054546	511	0.06 (R)	7	
[KDM2001] 6247	86.988875	-68.249167	kdm6247	446	0.02 (R)	7	
NGC 2121 LE6	87.070042	-71.477583	ngc2121le6	388	0.52 (I)	1	
IRAS 05495-7034	87.250000	-70.556278	iras05495				
MSX LMC 1492, lmc187.3_25	87.287000	-71.535250	msxlmc1492	567	0.61 (I)	1	
IRAS 05506-7053, MSX LMC 1453	87.485500	-70.886583	iras05506	1026	0.67 (K)	2	
MSX LMC 1488, IRAS 05508-7146	87.528167	-71.767389	msxlmc1488	608	0.62 (K)	2	
IRAS 05509-6956, MSX LMC 1469	87.608770	-69.934250	ERO0550261	1052	0.69 (W2)	5	
[KDM2001] 6486	87.652750	-68.481167	kdm6486	642	0.05 (I)	1	
2MASS J05504991-7123356, MSX LMC 1487	87.707958	-71.393222	iras05515	668	0.61 (K)	2	
[PMP2006b] 337	88.212750	-69.477667	pmp337	153	0.07 (I)	1	
IRAS 05568-6753, MSX LMC 1592	89.161500	-67.892889	iras05568	1209	1.03 (W2)	5	
MSX LMC 1652, IRAS 06025-6712	90.629375	-67.213028	msxlmc1652	957	0.70 (W2)	5	
IRAS 06028-6722, MSX LMC 1651	90.687917	-67.378667	iras06028	849	0.70 (W2)	5	
2MASS J06101067-7046033, MSX LMC 1638	92.544458	-70.767583	iras06108	516	0.44 (W2)	5	
Sculptor MAG 29	14.973667	-33.641889	SclMAG29	554	0.45 (K)	11	
Sculptor ALW 3	14.995583	-33.476444	SclALW3	189	0.21 (K)	11	
Fornax BW 2	39.525791	-34.522056	ForBW2	235	0.21 (V)	12	
Fornax BTH 13-23	39.710646	-34.675565	ForBTH13-23	350	0.51 (K)	13	
Fornax BTH 12-4	39.801370	-34.545800	ForBTH12-4	470	0.48 (K)	13	
Fornax BTH 3-129	39.923333	-34.599083	ForBTH3-129	400	0.58 (K)	13	
Fornax DK 18	39.975875	-34.643583	ForDK18	174	0.41 (V)	12	
Fornax DK 52	40.027750	-34.389500	ForDK52	341	0.36 (V)	12	
Fornax DI 2	40.039458	-34.107139	ForDI2				
Fornax DI 20	40.042500	-34.556083	ForDI20	320	0.13 (K)	13	
Fornax BW 69	40.074125	-34.459944	ForBW69	276	0.40 (V)	12	
Fornax BW 75	40.130150	-34.478949	ForBW75	276	0.40 (V)	12	
Fornax BW 83	40.264833	-34.801500	ForBW83	278	0.38 (V)	12	
Carina ALW 2	100.306375	-50.906944	CarALW2	182	0.09 (V)	12	
Carina ALW 6	100.422708	-50.968916	CarALW6	284	0.33 (V)	12	
Carina ALW 10	100.543125	-50.940000	CarALW10	194	0.19 (V)	12	
Leo I MFT C	152.092712	+12.299208	LeoIMFTC	523	0.52 (K)	14	
Leo I MFT A	152.122000	+12.314342	LeoIMFTA	336	0.40 (K)	14	
Leo I MFT E	152.251500	+12.316709	LeoIMFTE	283	0.58 (K)	14	

Notes. ^(a) 1= OGLE, 2= Groenewegen et al. (2017), VMC K-band data combined with literature data, 3= Kamath et al. (2010); Amplitude estimated from their figures, 4= Whitelock et al. (2003), 5= ALLWISE + NEOWISE + SAGE + SAGE-VAR, 6= MACHO, 7= EROS, 9= redetermined combining Whitelock et al. (2003) and Wood (1998), 10= Wood, Bessell & Paltoglou (1985), 11= Menzies et al. (2011); Semi amplitude read-off their figures, 12= Catalina Sky Survey (Drake et al. 2014), 13= Whitelock et al. (2009), 14= Menzies et al (2010); Semi amplitude read-off their figures.

Table A.2. M star sample.

Names	R.A.	Declination	Identifier	Period	Amp (F)	Ref. ^a	Remarks
WOH G 17, MSX LMC 1150	69.848708	-73.184111	wohg17	127	0.13 (V)	12	FG
MSX LMC 1212	73.384667	-69.021500	msxlmc1212				FG
RS Men, IRAS 05169-7350, MSX LMC 412	78.921917	-73.787139	rsmen	304	0.53 (K)	16	FG
[W60] D29, MSX LMC 819	82.997208	-66.644056	w60d29				FG
HD 269788, MSX LMC 778	83.723625	-68.777639	hd269788				FG
MSX LMC 946	84.584292	-69.625639	msxlmc946	112	0.14 (I)	15	FG
HD 269924	84.705500	-69.451778	hd269924				FG
MSX LMC 1677, IRAS 06013-6505	90.365833	-65.089750	msxlmc1677	345	2.39 (V)	15	FG
HD 271832, MSX LMC 1687, IRAS 06045-6722	91.106208	-67.388444	hd271832	541	0.09 (V)	15	FG
MSX LMC 1686, VV Dor, HV 12249	91.699125	-66.803472	msxlmc1686	349	3.01 (V)	15	FG
MSX SMC 067, HV 11262	11.903667	-73.078917	msxsmc067				SG
[M2002] SMC 10889	12.112583	-73.203417	smc010889				SG
[M2002] SMC 11709	12.193000	-73.472417	smc011709				SG
PMMR24, MACHO 212.15903.1	12.215904	-73.377739	pmmr24	430	0.15 (V)	15	SG
MSX SMC 096	12.526667	-73.469750	msxsmc096				SG
MSX SMC 109	12.873625	-73.178944	msxsmc109				SG
MSX SMC 168, HV 1652	13.861458	-72.598931	msxsmc168				SG
2MASS J00561387-7227324	14.057833	-72.459028	s3mc203963				SG
2MASS J00561455-7227425	14.060625	-72.461806	s3mc204111				SG
NGC 330 ARP 17	14.079250	-72.468972	s3mc205104				SG
[M2002] SMC 46662	14.895872	-72.068463	smc046662	394	0.12 (V)	15	SG
[M2002] SMC 52334	15.475667	-71.871889	smc052334				SG
PMMR 132	15.516875	-72.436389	pmmr132				SG
[M2002] SMC 55188	15.760263	-72.031403	smc055188	544	0.32 (I)	1	SG
PMMR 141	15.767833	-72.570305	pmmr141				SG
[M2002] SMC 55681	15.804138	-72.157312	smc55681				SG
PMMR 145	15.814084	-72.670111	pmmr145				SG
HV 11464	16.039543	-72.837717	hv11464				SG
[M2002] SMC 60447	16.221182	-72.796967	masseysmc60447				SG
HV 2084	17.409256	-73.333940	msxsmc149	737	0.48 (V)	15	SG
[M2002] SMC 83593	22.641504	-73.311579	smc083593	506	0.47 (V)	15	SG
2MASS J04471864-6942205	71.827708	-69.705722	sagemcj044718				SG
HV 2236, MSX LMC 1132	72.343583	-69.409556	hv2236	301	0.18 (V)	18	SG
HV 11423	15.229798	-71.631369	hv11423	668	0.34 (V)	15	SG
GV 60, WOH S 60, iras 04537-6922	73.378667	-69.297139	gv60	535	0.21 (V)	15	SG
MSX LMC 1189, IRAS 04553-6933	73.762792	-69.486861	msxlmc1189	512	0.23 (I)	15	SG
WOH G 64, MSX LMC 1182, IRAS 04553-6825	73.793667	-68.341611	wohg64	941	0.45 (I)	1	SG
MSX LMC 1204	73.816833	-69.320000	msxlmc1204	663	0.32 (V)	15	SG
MSX LMC 1330	73.840208	-69.787972	msxlmc1330	646	0.30 (V)	15	SG
MSX LMC 1318, MACHO 17.2473.8	73.889750	-69.416472	msxlmc1318	561	0.12 (I)	1	SG
HV 2255, MSX LMC 1328	74.430458	-70.147306	hv2255	912	0.17 (K)	19	SG
MSX LMC 1271, HD 268850	75.589458	-66.110639	msxlmc1271				SG
HV 888, MSX LMC 43, IRAS 05042-6720	76.058875	-67.270639	hv888	1005	0.57 (V)	15	SG
MSX LMC 141, HV 894	76.389583	-70.563028	msxlmc141	673	0.33 (V)	15	SG
HV 916, MSX LMC 264, IRAS 05148-6730	78.707167	-67.455472	hv916	781	0.12 (K)	4	SG
[M2002] LMC 116895, HV 5760	79.972065	-69.459315	lmc116895				SG
[M2002] LMC 119219	80.098395	-69.557450	lmc119219	895	0.41 (V)	15	SG
WOH S 264, IRAS 05247-6941 MSX LMC 461	81.080458	-69.647000	wohs264	1006	0.14 (B)	6	SG
[M2002] LMC 134383, HV 957	81.436891	-69.080244	lmc134383	457	0.24 (V)	15	SG
NGC 1948 WBT 2215, [W60] D4	81.504500	-66.271972	ngc1948wbt2215	223	0.34 (V)	18	SG
MSX LMC 549	81.547292	-66.203083	msxlmc549	633	0.38 (B)	6	SG
MSX LMC 575	81.592417	-66.357917	msxlmc575	816	0.06 (V)	15	SG
MSX LMC 589, [W60] A2	81.644958	-68.861111	msxlmc589				SG
HV 963, MSX LMC 567	81.893083	-66.891667	hv963	570	0.68 (V)	15	SG
HV 2551	81.910834	-69.478917	hv2551	348	0.13 (V)	15	SG
HV 2561, MSX LMC 593	82.120250	-68.118833	hv2561	710	0.31 (V)	15	SG
HV 5870, MSX LMC 609	82.264500	-69.112806	hv5870	691	0.09 (K)	2	SG
[W60] A27, MSX LMC 597	82.425875	-68.954806	w60a27	775	0.26 (V)	15	SG
HV 5879 MACHO 82.8044.1115	82.478125	-69.071028	hv5879	313	0.09 (V)	15	SG
SP77 46-50	82.519125	-68.791361	sp77_46-50				SG
MSX LMC 810	82.586125	-66.883833	msxlmc810				SG

Table A.2. M star sample: continued.

Names	R.A.	Declination	Identifier	Period	Amp (F)	Ref. ^a	Remarks
MSX LMC 587, HV 12998 IRAS 05313-6920	82.767417	-69.317500	msxlmc587	725	0.34 (<i>I</i>)	15	SG
[W60] D22, MSX LMC 818	82.794333	-66.592111	w60d22	598	0.20 (<i>V</i>)	15	SG
MSX LMC 839	82.903375	-66.502111	msxlmc839	747	0.42 (<i>V</i>)	15	SG
2MASS J05321865-6731459	83.077708	-67.529417	sagemcj053218	579	0.23 (<i>V</i>)	18	SG
2MASS J05321933-6731205	83.080542	-67.522389	ngc2011sageirs1				SG
HV 996, IRAS 05327-6757, TRM 5	83.148375	-67.919139	hv996	743	0.06 (<i>K</i>)	19	SG
MSX LMC 815, HV 1001	83.808708	-67.732167	msxlmc815	643	0.55 (<i>V</i>)	15	SG
HV 2700, TRM 62, MSX LMC 878	83.828792	-67.038778	hv2700	211	0.11 (<i>K</i>)	19	SG
MSX LMC 791, MACHO 82.8891.8	83.852167	-69.067611	msxlmc791	444	0.22 (<i>B</i>)	6	SG
MSX LMC 870, IRAS 05354-6657, TRM 68	83.868000	-66.934000	msxlmc870	737	0.12 (<i>V</i>)	15	SG
MSX LMC 891	83.980083	-69.166500	msxlmc891	475	0.02 (<i>V</i>)	15	SG
MH 6, MSX LMC 899, Z Dor, HV 2740	84.566708	-69.169778	mh6				SG
[W60] A72, MSX LMC 886, IRAS 05389-6922	84.641542	-69.342139	w60a72				SG
[W60] A78, MSX LMC 961	84.884708	-69.580556	w60a78	789	0.25 (<i>V</i>)	15	SG
[W60] A81, MSX LMC 901	85.101833	-69.354694	w60a81				SG
MSX LMC 897, HV 5993	85.182292	-69.366139	msxlmc897	302	0.08 (<i>I</i>)	15	SG
MSX LMC 939	85.202083	-69.560000	msxlmc939	612	0.06 (<i>V</i>)	15	SG
[M2002] LMC 175464	85.230431	-69.390368	lmc175464	538	0.26 (<i>V</i>)	15	SG
HV 1017	85.246625	-69.310028	hv1017	898	0.33 (<i>V</i>)	15	SG
[M2002] LMC 175746	85.278677	-69.287433	lmc175746	582	0.24 (<i>V</i>)	15	SG
HV 2778, MSX LMC 943	85.294417	-69.634444	hv2778	651	0.23 (<i>V</i>)	15	SG
W61 6-24	85.489250	-69.205056	w61_6-24	694	0.29 (<i>V</i>)	18	SG
[M2002] LMC 177150	85.502990	-69.193603	lmc177150				SG
NGC 2100 ROB B4	85.516250	-69.218722	ngc2100robb4				SG
2MASS J05420616-6913077	85.528167	-69.208667	2massj054206				SG
W61 6-57	85.541500	-69.224667	w61_6-57				SG
[M2002] LMC 177997, HV 2798	85.647833	-69.146750	lmc177997	470	0.20 (<i>V</i>)	15	SG
HV 2834, MSX LMC 1429	86.057208	-66.279028	hv2834	766	0.31 (<i>V</i>)	18	SG
HV 11223	8.006697	-73.376326	hv11223	386	0.12 (<i>I</i>)	1	MA
HV 1366	10.707712	-72.919808	hv1366	305	0.86 (<i>I</i>)	1	MA
MSX SMC 024, HV 1375, smc128.3_15	10.717625	-73.847694	msxsmc024	402	0.14 (<i>I</i>)	1	MA
2MASS J00444973-7313581	11.185928	-73.235450	j004444				MA
MSX SMC 018, OGLE 004631.61-732846.0	11.631625	-73.479556	msxsmc018	925	1.39 (<i>I</i>)	1	MA
BFM 1, MACHO 208.15800.6	11.830167	-72.667889	bfm1	403	1.03 (<i>I</i>)	1	MA
OGLE J005007.19-733124.7, IRAS 00483-7347	12.529958	-73.523639	msxsmc055	1810	0.81 (<i>I</i>)	1	MA
MSX SMC 134	12.684917	-72.627471	msxsmc134	249	0.04 (<i>I</i>)	1	MA
HV 11303	13.036834	-71.606648	hv11303	582	0.25 (<i>K</i>)	19	MA
BMB-B 75, OGLE J005212.93-730852.6	13.053917	-73.148087	bmbb75	779	1.20 (<i>I</i>)	1	MA
HV 11329	13.414125	-72.877556	hv11329	385	0.12 (<i>I</i>)	1	MA
HV 12122, smc108.6_10328	13.825174	-72.092190	msxsmc000	544	1.43 (<i>I</i>)	1	MA
HV 838, MACHO 211.16305.4	13.909208	-73.194722	hv838	643	1.09 (<i>I</i>)	1	MA
HV 11366, MACHO 207.16433.1	14.228215	-72.235683	hv11366	179	0.07 (<i>I</i>)	1	MA
HV 12149	14.709027	-72.309858	hv12149	774	1.27 (<i>I</i>)	1	MA
MSX SMC 181, HV 11417	15.200708	-72.850556	msxsmc181	1096	1.70 (<i>I</i>)	1	MA
HV 1963	16.110906	-72.577842	hv1963	355	0.08 (<i>K</i>)	17	MA
IRAS F01066-7332	17.043033	-73.264597	irasF01066	886	1.33 (<i>I</i>)	1	MA
HV 12956	17.259375	-71.402833	hv12956	522	1.34 (<i>I</i>)	1	MA
OGLE LMC-LPV-749	69.338167	-70.579083	ngc1651sageirs1	247	0.04 (<i>I</i>)	1	MA
IRAS 04407-7000, MSX LMC 1072	70.118667	-69.920417	iras04407	1148	1.84 (<i>I</i>)	1	MA
IRAS 04498-6842, MSX LMC 1117	72.422792	-68.630944	iras04498	1256	1.72 (<i>I</i>)	1	MA
IRAS 04509-6922, MSX LMC 1192	72.668583	-69.292194	iras04509	1271	1.56 (<i>I</i>)	1	MA
2MASS J04512858-6955500	72.869285	-69.930561	sagemcj045128	899	0.71 (<i>I</i>)	1	MA
IRAS 04516-6902, MSX LMC 1190	72.870792	-68.963889	iras04516	1095	1.45 (<i>I</i>)	1	MA
2MASS J04530941-6817109	73.289208	-68.286361	sagemcj045309	921	0.10 (<i>I</i>)	1	MA
IRAS 04545-7000, MSX LMC 1171	73.541875	-69.932833	iras04545	1254	0.85 (<i>K</i>)	9	MA
2MASS J04562323-6927489	74.096833	-69.463583	sagemcj045623				MA
IRAS 05003-6712, MSX LMC 1280	75.079125	-67.132778	iras05003	914	1.47 (<i>I</i>)	1	MA
MSX LMC 61, MACHO 25.3951.67	76.120542	-67.689972	msxlmc61	575	1.41 (<i>I</i>)	1	MA
HV 2310, SHV 0506368-681557	76.615287	-68.201028	hv2310	589	1.05 (<i>I</i>)	1	MA
2MASS J05075937-6839257	76.997375	-68.657167	sagemcj050759	377	0.03 (<i>I</i>)	1	MA
BMB-BW 180	77.360833	-69.115666	bmbbw180	68	0.02 (<i>I</i>)	1	MA

Table A.2. M star sample: continued.

Names	R.A.	Declination	Identifier	Period	Amp (F)	Ref. ^a	Remarks
2MASS J05105908-6856137	77.746208	-68.937139	sagemcj051059	294	0.07 (I)	1	MA
2MASS J05121357-6839228	78.056542	-68.656333	sagemcj051213	413	0.05 (I)	1	MA
IRAS 05128-6455, MSX LMC 283	78.269042	-64.861194	iras05128	710	0.54 (K)	19	MA
2MASS J05133993-6638526	78.416375	-66.647944	sagemcj051339	756	0.11 (I)	1	MA
NGC 1866 ROB B136, MACHO 59.5436.11	78.422542	-65.474500	ngc1866robb136	122	0.07 (R)	7	MA
2MASS J05141234-6850579	78.551458	-68.849444	sagemcj051412	771	0.16 (I)	1	MA
2MASS J05152646-6751268	78.860250	-67.857472	sagemcj051526	195	0.05 (I)	1	MA
2MASS J05161243-7049302	79.051833	-70.825055	sagemcj051612	775	0.10 (I)	1	MA
2MASS J04512899-6857500, MSX LMC 1190	79.446667	-68.311833	sagemcj051747	1826	0.12 (I)	1	MA
HV 5715, MACHO 49.6132.10	79.546167	-67.446861	hv5715	438	0.31 (R)	6	MA
2MASS J05201425-7029309	80.059375	-70.491944	sagemcj052014	679	0.09 (I)	1	MA
2MASS J05205184-6934076	80.216042	-69.568777	sagemcj052051	775	0.16 (I)	1	MA
2MASS J05210166-6914174	80.256917	-69.238167	sagemcj052101	216	0.06 (I)	1	MA
SSTISAGE1C J052206.92-715017.6	80.528875	-71.838278	sagemcj052206	398	0.03 (I)	1	MA
SHV 0523185-693932	80.729042	-69.614416	shv0523185	208	0.48 (I)	1	MA
HV 12793, MSX LMC 529, TRM 108	80.931708	-65.699889	hv12793	641	0.07 (K)	19	MA
IRAS 05246-7137, MSX LMC 423	80.974708	-71.578861	iras05246				MA
HV 5810, TX Dor	81.029263	-69.393523	hv5810	369	0.79 (I)	1	MA
OGLE J052620.01-694137.5	81.583834	-69.650639	ogle052620	816	0.21 (I)	1	MA
WBP 77, SHV 0528300-693445	82.027980	-69.541080	wbp77	212	0.37 (I)	1	MA
HV 2572, MSX LMC 1781, SHV 0528586-69	82.152917	-69.334444	hv2572	615	0.93 (I)	1	MA
MSX LMC 642, IRAS 05294-7104	82.200708	-71.041361	msxlmc642	1133	1.71 (I)	1	MA
HV 2575, MACHO 4.7943.9, GRV0529-6747	82.249917	-67.750361	hv2575	383	0.67 (R)	7	MA
HV 2578, SHV 0529291-695022	82.263162	-69.801919	hv2578	643	0.84 (I)	1	MA
IRAS 05298-6957, MSX LMC 653	82.352600	-69.920468	iras05298	1265	0.98 (K)	19	MA
SHV 0530472-690607	82.614708	-69.066194	shv0530472	214	0.71 (I)	1	MA
2MASS J05312844-7010271	82.868542	-70.174222	sagemcj053128	389	0.27 (I)	1	MA
2MASS J05320670-7010248	83.027917	-70.173556	sagemcj053206	128	0.04 (I)	1	MA
MSX LMC 807, TRM 58	83.154833	-67.115667	msxlmc807	1069	0.70 (K)	2	MA
IRAS 05329-6708, MSX LMC 811, TRM 60	83.213875	-67.114444	iras05329	1303	0.80 (K)	9	MA
HV 12620, SHV 0533355-704322	83.249607	-70.689886	hv12620	324	0.72 (I)	1	MA
2MASS J05334325-7059209	83.430208	-70.989166	sagemcj053343b	161	0.02 (I)	1	MA
2MASS J05334396-7059017	83.433208	-70.983833	sagemcj053343a	148	0.17 (I)	1	MA
2MASS J05354806-7031464	83.950250	-70.529583	sagemcj053548	973	0.12 (I)	1	MA
OGLE LMC-LPV-74445	84.231667	-68.190167	sagemcj053655	761	0.20 (I)	1	MA
IRAS 05402-6956, MSX LMC 936	84.937000	-69.921667	iras05402	1362	1.70 (I)	1	MA
WOH G 449	84.939208	-66.969278	wohg449	124	0.14 (R)	7	MA
MSX LMC 947	85.258167	-70.719694	msxlmc947	689	1.39 (I)	1	MA
2MASS J05411457-7132359	85.310750	-71.543305	sagemcj054114	193	0.05 (R)	7	MA
WOH G 494, MACHO 76.10090.12	85.627250	-69.815944	wohg494	170	0.06 (I)	1	MA
2MASS J05425437-7008075	85.726542	-70.135417	sagemcj054254	267	0.10 (I)	1	MA
2MASS J05431413-7038351	85.808875	-70.643083	sagemcj054314	162	0.05 (I)	1	MA
OGLE LMC-LPV-82411	86.025125	-68.631555	sagemcj054406	444	0.23 (I)	1	MA
2MASS J05444011-6911491	86.167167	-69.196972	sagemcj054440	316	0.03 (I)	1	MA
HV 12667, SHV 0549503-704331	87.305625	-70.711278	hv12667	673	1.26 (R)	7	MA
HV 12070	88.116031	-69.236126	hv12070	610	1.75 (R)	6	MA
2MASS J05534915-7105269	88.454792	-71.090833	iras05545	312	0.02 (I)	1	MA
IRAS 05558-7000, MSX LMC 1524	88.837625	-70.000833	iras05558	1175	1.79 (I)	1	MA
2MASS J06005362-6800389	90.223417	-68.010833	sagemcj060053	105	0.11 (R)	6	MA

Notes. ^(a) 1= OGLE, 2= Groenewegen et al. (2017), VMC K-band data combined with literature data, 3= Kamath et al. (2010); Amplitude estimated from their figures, 4= Whitelock et al. (2003), 5= ALLWISE + NEOWISE + SAGE + SAGE-VAR, 6= MACHO, 7= EROS, 9= period redetermined combining Whitelock et al. (2003) and Wood (1998), 10= Wood, Bessell & Paltoglou (1985), 11= Menzies et al. (2011); Semi amplitude read-off their figures, 12= Catalina Sky Survey (Drake et al. 2014), 13= Whitelock et al. (2009), 14= Menzies et al (2010); Semi amplitude read-off their figures, 15= ASAS-3 (Pojmanski 2002), 16= Whitelock et al. (1994), 17= period redetermined by combining Catchpole & Feast (1981), and WBF, 18= OMC (Mas-Hesse et al. 2003), 19= various literature K-band data.

Table B.1. Fit results of the C star sample.

Identifier	$T_{\text{eff}} / \log g / (\text{C/O})$ (K/-/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
gm780	3100/+000/0140	a0.15 zubko100 Pitm10 Hofm0	20019	1.849e+00	1.09e-07	1	1200	0	2.00	0	17	153
msxsmc029	3600/+000/0140	a0.10 zubko100 Pitm0 Hofm0	4984	1.950e+01	1.26e-06	1	676	1	1.53	1	4	53
msxsmc091	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6975	3.345e+00	1.16e-07	1	1200	0	2.00	0	8	350
iras00350	4000/+000/0140	a0.15 zubko100 Pitm0 Hofm10	56665	2.585e+00	1.84e-07	1	1037	1	1.41	1	9.9	83
msxsmc062	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	16243	5.523e+00	4.90e-07	1	997	1	2.00	0	8	1149
msxsmc054	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	6632	1.071e+01	8.10e-07	1	1016	1	2.24	1	8	551
j004326	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4644	9.571e-01	2.50e-08	1	1200	0	2.00	0	10	228
msxsmc044	3000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	16310	3.220e+00	1.76e-07	1	1200	0	2.00	0	0.037	1945
j004452	2600/+000/0140	a0.15 zubko100 Pitm0 Hofm0	9195	2.697e+00	3.21e-07	1	590	1	1.52	1	10	43
msxsmc105	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7900	6.711e+00	5.94e-07	1	871	1	2.00	0	8	181
msxsmc036	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4634	7.851e+00	4.94e-07	1	902	1	2.00	0	8	707
msxsmc014	3000/+000/0140	a0.15 zubko100 Pitm0 Hofm0	9922	3.608e+01	2.22e-06	1	1200	0	2.13	1	8	435
msxsmc060	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	16513	9.044e+00	3.11e-07	1	1200	0	1.60	1	8	249
msxsmc200	3400/+000/0140	a0.15 zubko100 Pitm0 Hofm0	6763	6.000e+00	2.70e-07	1	1200	0	2.21	1	8	394
msxsmc033	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	18992	7.168e+00	6.32e-07	1	1200	0	2.38	1	0.037	502
j004720	3500/+000/0140	a0.15 zubko100 Pitm50 Hofm0	16541	2.084e-01	1.45e-08	1	1200	0	2.00	0	17	239
msxsmc066	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	17718	7.222e+00	7.87e-07	1	1200	0	2.66	1	8	672
irasf00471	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	30455	8.648e+00	6.26e-07	1	1200	0	1.91	1	8	411
cv78	4000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10007	8.958e-01	4.00e-08	1	1200	0	2.00	0	22	20102
raw594	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4257	6.472e-01	1.63e-08	1	1200	0	2.00	0	10	208
msxsmc163	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	11881	6.543e+00	4.27e-07	1	1083	1	2.00	0	8	132
msxsmc142	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4552	2.830e+00	7.95e-08	1	1238	1	2.00	0	0.018	261
msxsmc125	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	14932	3.130e+00	1.61e-07	1	1200	0	2.00	0	5	593
msxsmc162	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	13166	2.417e+00	1.14e-07	1	1200	0	2.00	0	4	1901
msxsmc202	3100/+000/0140	a0.15 zubko100 Pitm0 Hofm0	14328	1.968e+00	9.08e-08	1	1200	0	2.00	0	0.25	592
msxsmc159	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6512	1.085e+01	3.06e-07	1	1200	0	1.76	1	8	358
legc105	3100/+000/0140	a0.15 zubko100 Pitm0 Hofm0	7739	2.564e+00	8.84e-08	1	1200	0	2.00	0	14	717
iso00548	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	11573	5.091e+00	3.53e-07	1	1200	0	2.37	1	12	237
iso00549	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9226	7.886e+00	4.49e-07	1	1105	1	2.00	0	8	728
raw960	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6587	8.716e-01	2.70e-08	1	1200	0	2.00	0	26	368
msxsmc209	2900/+000/0140	a0.15 zubko100 Pitm5 Hofm0	15302	7.203e+00	4.23e-07	1	1173	1	2.00	0	8	1380
s3mc204803	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7394	3.348e-01	1.08e-08	0	1200	0	2.00	0	13	163
iras00554	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	23066	1.418e+01	2.56e-06	1	829	1	2.00	0	8	2430
msxsmc198	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7996	5.591e+00	2.08e-07	1	1249	1	2.00	0	8	638
msxsmc155	3400/+000/0140	a0.15 zubko100 Pitm0 Hofm0	8814	1.985e+01	1.09e-06	1	1200	0	2.13	1	8	894
iso00573	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6535	1.777e+00	5.78e-08	1	1200	0	2.00	0	15	289
msxsmc093	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7976	2.291e+00	8.24e-08	1	1200	0	2.00	0	23	340
iso01019	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6161	4.968e+00	2.84e-07	1	1200	0	2.54	1	12	245
j010453	2900/+000/0140	a0.15 zubko100 Pitm0 Hofm0	4514	2.951e+01	1.57e-06	1	997	1	2.00	0	8	121
msxsmc232	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6629	6.875e+00	2.55e-07	1	1200	0	2.00	0	8	498
ngc419le16	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5010	2.321e+00	6.66e-08	1	1200	0	2.00	0	16	439
ngc419ir1	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	11990	6.016e+00	4.19e-07	1	1200	0	2.40	1	8	721
ngc419le35	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7050	4.350e-01	1.36e-08	0	1200	0	2.00	0	17	46
ngc419mir1	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	8083	4.707e+01	2.32e-06	1	1200	0	1.87	1	8	257
ngc419le27	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6846	4.350e-01	1.35e-08	0	1200	0	2.00	0	17	70
ngc419le18	3200/+000/0140	a0.15 zubko100 Pitm0 Hofm0	5616	4.736e-01	1.34e-08	1	1200	0	2.00	0	19	1027
iras04286	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12136	1.327e+01	4.34e-07	1	1200	0	1.61	1	8	630
iras04331	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm20	8380	2.180e+01	3.12e-06	1	826	1	2.00	0	8	256
iras04340	4750/+000/xxxx	a0.15 zubko100 Pitm10 Hofm0	6409	8.110e+00	5.06e-07	1	1100	0	2.01	1	0.037	109
iras04353	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	6902	1.638e+01	1.52e-06	1	869	1	1.87	1	8	837
iras04375	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	7257	1.454e+01	1.73e-06	1	794	1	1.96	1	8	269
iras04374	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12159	1.661e+01	1.39e-06	1	1004	1	2.00	0	8	567
iras04433	2600/+000/0140	a0.30 zubko100 Pitm10 Hofm0	7719	5.620e+00	4.71e-07	1	1200	0	2.12	1	8	244
sagemcj044627	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	5325	2.993e+00	9.33e-08	1	1200	0	2.00	0	8	374
msxlmc1120	3100/+000/0140	a0.30 zubko100 Pitm5 Hofm0	15377	5.584e+00	6.07e-07	1	1006	1	1.74	1	8	2170
iras04496	2600/+000/0140	a0.15 zubko100 Pitm0 Hofm0	38738	4.527e+00	2.38e-07	1	1200	0	1.66	1	0.40	494
msxlmc1128	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8170	2.353e+00	8.79e-08	1	1200	0	2.00	0	0.037	1922
msxlmc1308	2600/+000/0140	a0.15 zubko100 Pitm0 Hofm0	15044	6.652e+00	3.47e-07	1	1200	0	2.00	0	8	438
msxlmc1205	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	19003	9.856e+00	7.37e-07	1	1153	1	2.00	0	8	389
iras04518	2700/+000/0140	a0.15 zubko100 Pitm5 Hofm20	5376	5.683e+01	7.50e-06	1	787	1	2.00	0	8	831

Table B.1. Fit results of the C star sample: continued.

Identifier	$T_{\text{eff}} / \log g / (C/O)$ (K/-/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
msxlmc1213	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	8367	1.965e+01	9.13e-07	1	1258	1	2.00	0	8	404
kdm764	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8198	7.064e-01	2.45e-08	1	1200	0	2.00	0	13	276
sagemcj045328	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5220	1.460e+00	4.20e-08	1	1200	0	2.00	0	10	222
sagemcj045344	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm20	8349	3.764e+01	5.84e-06	1	809	1	2.00	0	8	258
iras04538	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12738	1.674e+01	2.35e-06	1	838	1	2.00	0	8	823
iras04537	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm0	13324	3.664e+00	3.25e-07	1	1154	1	1.95	1	8	584
msxlmc1209	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	6884	1.112e+01	6.45e-07	1	1037	1	2.00	0	8	289
iras04557	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	15097	1.748e+01	2.55e-06	1	825	1	1.89	1	8	276
msxlmc1298	3300/+000/0140	a0.30 zubko100 Pitm5 Hofm0	31412	7.311e+00	1.19e-06	1	1200	0	2.06	1	8	1131
iras04589	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm15	6968	7.533e-01	4.15e-06	1	1200	0	1.89	1	8	83
kdm1238	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6668	2.216e+01	6.73e-09	1	1200	0	2.00	0	13	135
iras05013	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	8305	2.146e+01	1.10e-06	1	1200	0	2.00	0	8	407
msxlmc1282	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	14173	1.411e+01	1.59e-06	1	913	1	2.00	0	8	524
iras05009	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12405	1.828e+01	1.57e-06	1	1002	1	2.00	0	8	919
ERO0502315	3200/+000/0140	a0.15 zubko100 Pitm10 Hofm0	8030	2.986e+02	2.38e-05	1	1200	0	1.91	1	8	87
kdm1656	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	14727	5.976e-01	2.76e-08	1	1200	0	2.00	0	13	158
kdm1691	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12882	6.891e-01	3.00e-08	1	1200	0	2.00	0	13	203
lmc-bm11-19	2700/+000/0140	a0.15 zubko100 Pitm0 Hofm0	5476	6.042e-03	1.53e-10	0	1200	0	2.00	0	13	1859
lmc-bm12-14	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10679	4.818e-01	1.91e-08	1	1200	0	2.00	0	0.074	70
ERO0504056	3000/+000/0140	a0.15 zubko100 Pitm10 Hofm0	5968	3.125e+02	2.34e-05	1	1200	0	1.96	1	8	383
ngc1818wbt64	3300/+000/0140	a0.15 zubko100 Pitm20 Hofm0	5502	2.858e-01	1.67e-08	1	957	1	2.00	0	8	98
sagemcj050503	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10272	5.197e-03	1.96e-10	0	1200	0	2.00	0	10	485
iras05053	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm15	11262	9.006e+01	7.48e-06	1	1200	0	2.00	1	8	119
lmc-bm13_2	3200/+000/0140	a0.15 zubko100 Pitm20 Hofm0	2957	2.551e+00	6.70e-08	1	1200	0	2.00	0	0.037	1172
sagemcj050607	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4126	1.560e+00	3.96e-08	1	1200	0	2.00	0	10	631
kdm1961	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4860	3.015e-03	7.82e-11	0	1200	0	2.00	0	13	103
kdm1966	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5590	3.015e-03	8.39e-11	0	1200	0	2.00	0	13	149
sagemcj050620	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9926	4.370e-01	1.64e-08	1	1200	0	2.00	0	10	78
sagemcj050629	3000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3537	5.105e-01	1.13e-08	1	1200	0	2.00	0	13	133
iras05070	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm5	9989	2.727e+01	2.70e-06	1	810	1	1.70	1	8	488
shv0507252	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	12038	1.988e+00	8.76e-08	1	1200	0	2.00	0	8	929
sagemcj050752	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	2950	4.756e+00	1.15e-07	1	1200	0	2.00	0	4	420
msxlmc92	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	13782	7.685e+00	5.51e-07	1	1062	1	2.00	0	8	400
sagemcj050826	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10226	3.380e+00	1.48e-07	1	1200	0	2.00	0	37.0	1383
kdm2187	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3381	3.150e-01	6.97e-09	1	1200	0	2.00	0	13	240
msxlmc95	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	14209	5.978e+00	8.20e-07	1	821	1	2.00	0	8	503
msxlmc87	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	15443	6.683e+00	5.76e-07	1	894	1	1.76	1	8	352
sage1cj051028	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	5268	9.623e+00	3.37e-07	1	1200	0	2.00	0	9	660
iras05112	3900/+000/0140	a0.10 zubko100 Pitm5 Hofm10	16145	2.179e+01	3.79e-06	1	824	1	2.04	1	8	1155
iras05113	3900/+000/0140	a0.10 zubko100 Pitm5 Hofm5	9401	1.733e+01	2.70e-06	1	782	1	2.12	1	8	149
msxlmc219	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	11913	1.748e+01	2.26e-06	1	867	1	2.00	0	8	531
trm72	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	13152	7.314e+00	1.35e-06	1	822	1	2.29	1	8	1038
iras05125	2800/+000/0140	a0.15 zubko100 Pitm5 Hofm15	15453	4.384e+01	7.23e-06	1	873	1	2.00	0	8	132
msxlmc220	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	23710	6.848e+00	3.53e-07	1	1200	0	1.73	1	8	554
iras05132	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9756	2.344e+01	9.47e-07	1	1200	0	1.77	1	8	375
iras05133	2800/+000/0140	a0.15 zubko100 Pitm10 Hofm15	6196	4.457e+02	6.14e-05	1	1200	0	2.25	1	5	145
ogle051306	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4740	8.192e+00	6.34e-07	1	962	1	2.37	1	2	944
msxlmc218	3000/+000/0140	a0.30 zubko100 Pitm5 Hofm0	17281	4.892e+00	3.06e-07	1	1271	1	1.73	1	8	231
hv5680	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6682	6.254e-04	1.87e-11	0	1200	0	2.00	0	22	100
msxlmc349	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm15	7773	2.269e+01	9.66e-07	1	1200	0	1.81	1	8	300
sagemcj051803	3000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4918	2.045e+00	5.81e-08	1	1200	0	2.00	0	0.074	315
kdm3196	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9532	2.230e-03	8.10e-11	0	1200	0	2.00	0	13	87
ERO0518117	3400/-020/0140	a0.10 zubko100 Pitm0 Hofm0	9310	7.919e+01	7.29e-05	1	399	1	2.44	1	0.60	99
sagemcj051832	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5235	5.147e-01	1.41e-08	1	1200	0	2.00	0	10	334
ERO0518484	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6921	2.205e+02	1.38e-05	1	1200	0	1.88	1	8	109
iras05190	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm10	13882	3.757e+01	2.18e-06	1	1200	0	1.79	1	8	451
sagemcj051908	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7642	3.756e-01	1.23e-08	1	1200	0	2.00	0	13	204
2massj051910	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8716	6.973e-01	2.46e-08	1	1200	0	2.00	0	13	164
trm88	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9403	5.504e+00	4.22e-07	1	970	1	2.00	0	8	4288
msxlmc439	3300/+000/0140	a0.15 zubko100 Pitm0 Hofm0	7679	3.026e+01	1.43e-06	1	1200	0	2.00	0	5	288
msxlmc341	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm10	5827	1.862e+01	1.45e-06	1	941	1	2.00	0	8	213

Table B.1. Fit results of the C star sample: continued.

Identifier	$T_{\text{eff}} / \log g / (\text{C/O})$ (K/-/)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
h942	4000/+000/0140	a0.15 zubko100 Pitm0 Hofm0	2282	1.882e+01	1.50e-06	1	766	1	2.00	0	3	69
msxlmc527	3300/+000/0140	a0.15 zubko100 Pitm0 Hofm0	11383	2.523e+01	3.11e-06	1	854	1	2.00	0	5	190
ogle052242	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7408	5.142e+00	5.64e-07	1	941	1	2.41	1	8	364
msxlmc663	7750/+250/xxxx	a0.10 zubko100 Pitm0 Hofm0	13284	3.087e+00	5.63e-08	1	1473	1	1.48	1	25	109
msxlmc494	3000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9593	4.877e+00	2.06e-07	1	1200	0	2.00	0	8	631
iras05236	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm0	13103	5.547e+00	4.37e-07	1	1200	0	1.87	1	8	1301
sagemcj052405	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3552	4.308e+00	1.14e-07	1	1200	0	2.00	0	8	411
msxlmc441	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	7917	2.510e+01	1.95e-06	1	1016	1	2.00	0	4	190
iras05254	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	8354	1.557e+01	1.96e-06	1	787	1	1.92	1	8	713
ogle052445	3100/+000/0140	a0.15 zubko100 Pitm10 Hofm0	7411	2.826e+00	1.05e-07	1	1200	0	2.00	0	9	351
msxlmc443	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm10	9264	1.724e+01	1.49e-06	1	988	1	2.00	0	8	581
msxlmc438	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	15861	8.805e+00	8.66e-07	1	968	1	2.00	0	8	1961
ERO0525406	2900/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3857	2.954e+02	1.83e-05	1	1200	0	2.03	1	8	61
msxlmc474	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	11978	1.133e+01	1.53e-06	1	830	1	2.00	0	8	166
wbp17	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7368	5.000e-03	1.54e-10	0	1200	0	2.00	0	16	300
msxlmc774	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	7678	1.450e+01	1.84e-06	1	791	1	2.00	0	8	145
msxlmc634	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9348	6.509e+00	6.99e-07	1	950	1	2.32	1	8	206
wbp29	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5101	1.970e-01	5.23e-09	1	1200	0	2.00	0	12	220
msxlmc601	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10417	8.902e+00	7.15e-07	1	988	1	2.00	0	8	603
wbp42	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5784	1.802e+00	5.40e-08	1	1200	0	2.00	0	5	204
wbp51	2800/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6715	7.936e-01	2.44e-08	1	1200	0	2.00	0	21	118
iras05278	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm10	24856	8.005e+00	3.05e-06	1	741	1	1.84	1	8	173
shv0528350	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8752	1.237e+00	4.56e-08	1	1200	0	2.00	0	10	424
msxlmc754	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8233	6.528e+00	2.92e-07	1	1200	0	2.10	1	8	538
ogle052825	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7953	3.505e-01	1.22e-08	1	1200	0	2.00	0	13	177
wbp104	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4195	7.715e-02	1.84e-09	1	1200	0	2.00	0	8	82
ngc1978ir1	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8772	7.410e+00	3.72e-07	1	1200	0	2.18	1	13	705
ngc1978ir4	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	14134	5.424e-01	2.45e-08	1	1200	0	2.00	0	21	217
iras05295	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9851	1.601e+01	5.67e-07	1	1200	0	1.74	1	8	545
ngc1978mir1	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm10	7800	6.378e+00	3.51e-07	1	1200	0	1.73	1	8	379
msxlmc679	3100/+000/0140	a0.15 zubko100 Pitm10 Hofm10	5932	1.177e+01	1.26e-06	1	818	1	2.00	0	8	619
grrv38	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	11041	1.847e+00	7.75e-08	1	1200	0	2.00	0	23	190
ERO0529379	3100/+000/0140	a0.15 zubko100 Pitm20 Hofm10	5434	1.723e+02	1.32e-05	1	1200	0	2.05	1	8	94
iras05300	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8869	1.575e+01	1.96e-06	1	796	1	2.00	0	8	747
iras05306	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	9129	3.636e+01	6.98e-06	1	760	1	2.15	1	4	209
iras05315	4750/+050/xxxx	a0.10 zubko100 Pitm10 Hofm20	8253	7.048e+01	6.98e-05	1	372	1	1.90	1	0.20	102
kdm4554	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10575	5.038e+00	3.72e-07	1	1200	0	2.54	1	10	805
msxlmc841	2700/+000/0140	a0.30 zubko100 Pitm5 Hofm0	10608	4.760e+00	5.50e-07	1	1055	1	2.05	1	8	72
msxlmc768	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	19501	1.314e+01	1.60e-06	1	937	1	2.00	0	8	485
kdm4665	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6922	2.696e-03	8.35e-11	0	1200	0	2.00	0	13	89
msxlmc782	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm10	8203	9.715e+00	6.41e-07	1	1050	1	2.00	0	8	149
kdm4718	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10815	1.424e-01	5.48e-09	0	1200	0	2.00	0	13	207
kdm4774	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7964	5.193e-01	1.82e-08	1	1200	0	2.00	0	13	77
msxlmc783	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9470	7.636e+00	6.02e-07	1	972	1	2.00	0	8	403
msxlmc775	3200/+000/0140	a0.15 zubko100 Pitm0 Hofm0	29760	5.386e+00	5.86e-07	1	1200	0	2.43	1	0.037	1034
msxlmc736	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	9439	4.817e+01	2.61e-06	1	1200	0	1.85	1	8	434
sagemcj053318	4000/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4213	6.026e+00	2.05e-07	1	1200	0	2.00	0	8	302
iras05348	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm5	14349	3.024e+01	1.88e-06	1	1200	0	1.89	1	8	183
sagemcj053441	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8311	6.844e+00	3.65e-07	1	1200	0	2.28	1	8	1064
msxlmc743	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	10240	1.961e+01	1.84e-06	1	966	1	2.00	0	0.30	914
msxlmc787	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm15	6998	1.276e+01	1.30e-06	1	873	1	2.00	0	8	171
msxlmc950	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm0	7656	9.287e+00	6.24e-07	1	991	1	2.00	0	8	605
msxlmc796	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7850	1.409e+00	4.96e-08	1	1200	0	2.00	0	10	174
msxlmc749	3100/+000/0140	a0.30 zubko100 Pitm5 Hofm0	11879	5.665e+00	5.99e-07	1	1149	1	2.08	1	8	762
iras05355	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm0	10651	4.366e+00	3.36e-07	1	1215	1	2.00	0	4	323
iras05360	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	6149	2.066e+01	1.22e-06	1	1003	1	1.84	1	8	119
iras05373	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6653	2.259e+01	1.24e-06	1	1115	1	2.00	0	8	198
msxlmc967	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	15407	7.790e+00	4.79e-07	1	1200	0	2.09	1	8	144
kdm5345	3600/+000/0140	a0.15 zubko100 Pitm20 Hofm0	3767	1.547e+00	4.65e-08	0	1200	0	2.00	0	13	319
ogle053930	3100/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6474	4.954e+00	1.79e-07	1	1200	0	2.00	0	0.037	804
msxlmc971	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	6132	1.516e+01	2.31e-06	1	720	1	2.06	1	4	217

Table B.1. Fit results of the C star sample: continued.

Identifier	$T_{\text{eff}} / \log g / (\text{C/O})$ (K/-/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
msxlmc1400	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	9330	1.743e+01	4.18e-07	1	1200	0	1.53	1	8	191
msxlmc937	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	16840	1.176e+01	7.78e-07	1	1051	1	1.75	1	8	346
msxlmc974	3100/+000/0140	a0.30 zubko100 Pitm5 Hofm0	10851	5.080e+00	4.33e-07	1	1200	0	2.03	1	8	208
iras05416	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	10863	7.582e+01	4.21e-06	1	1200	0	1.76	1	8	694
msxlmc1795	2600/+000/0140	a0.15 zubko100 Pitm0 Hofm0	5065	1.644e+01	8.89e-07	1	987	1	2.00	0	3	316
kdm5841	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3330	6.730e-01	1.49e-08	1	1200	0	2.00	0	10	115
msxlmc1384	2600/+000/0140	a0.30 zubko100 Pitm5 Hofm0	10815	7.395e+00	3.30e-07	1	1284	1	1.67	1	8	1639
msxlmc1383	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm20	7043	2.486e+01	3.47e-06	1	767	1	1.95	1	5	193
sagemcj054437	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8864	3.882e+00	1.58e-07	1	1200	0	2.00	0	8	479
sagemcj054546	4750/+000/xxxx	a0.15 zubko100 Pitm0 Hofm0	1127	4.382e+00	2.67e-07	1	615	1	1.64	1	4	68
kdm6247	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4657	2.921e-03	7.42e-11	0	1200	0	2.00	0	10	68
ngc2121le6	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8039	1.516e+00	5.29e-08	1	1200	0	2.00	0	10	440
iras05495	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	11509	7.771e+01	2.84e-04	1	270	1	2.50	1	0.10	96
msxlmc1492	3100/+000/0140	a0.15 zubko100 Pitm0 Hofm0	23808	4.717e+00	2.82e-07	1	1236	1	2.00	0	0.10	452
iras05506	2800/+000/0140	a0.15 zubko100 Pitm5 Hofm10	17677	2.448e+01	5.63e-06	1	759	1	2.00	0	8	267
msxlmc1488	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	13949	1.594e+01	7.83e-07	1	1173	1	1.79	1	8	444
ERO0550261	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm10	10412	1.162e+02	1.99e-05	1	800	0	1.92	1	5	259
kdm6486	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4334	2.682e-03	6.47e-11	0	1200	0	2.00	0	10	151
iras05515	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm10	10687	3.512e+01	2.37e-06	1	1200	0	2.03	1	8	714
pmp337	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	10212	2.208e-03	8.46e-11	0	1200	0	2.00	0	13	241
iras05568	2700/+000/0140	a0.15 zubko100 Pitm5 Hofm10	21262	4.897e+01	8.87e-06	1	836	1	1.88	1	6	951
msxlmc1652	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm15	19249	2.003e+01	4.78e-06	1	724	1	1.90	1	8	321
iras06028	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm10	14191	3.786e+01	2.32e-06	1	1200	0	1.85	1	0.80	190
iras06108	2600/+000/0140	a0.15 zubko100 Pitm10 Hofm15	8358	1.857e+01	7.72e-07	1	1200	0	1.79	1	8	258
ScIMAG29	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8116	2.914e+00	1.08e-07	1	1200	0	2.00	0	8	908
ScIALW3	3600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5090	1.641e-01	4.65e-09	1	1200	0	2.00	0	8	77
ForBW2	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6172	2.756e+00	1.42e-07	1	1200	0	2.48	1	8	7
ForBTH13-23	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4604	7.711e+00	2.37e-07	1	1200	0	2.00	0	8	182
ForBTH12-4	3600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	8021	5.094e+00	2.18e-07	1	1200	0	2.00	0	8	353
ForBTH3-129	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	5212	1.015e+01	3.44e-07	1	1200	0	2.00	0	8	355
ForDK18	3500/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6963	1.169e+00	4.04e-08	1	1200	0	2.00	0	8	371
ForDK52	3500/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4216	1.024e+00	2.74e-08	1	1200	0	2.00	0	8	421
ForDI2	3700/+000/0140	a0.15 zubko100 Pitm5 Hofm0	2230	1.107e+00	2.25e-08	1	1200	0	2.00	0	8	938
ForDI20	3200/+000/0140	a0.15 zubko100 Pitm5 Hofm0	6547	5.612e-01	1.72e-08	1	1200	0	2.00	0	8	821
ForBW69	3500/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3917	1.747e+00	4.66e-08	1	1200	0	2.00	0	8	378
ForBW75	3400/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4840	6.056e-01	1.66e-08	1	1200	0	2.00	0	8	313
ForBW83	3500/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4162	1.705e+00	4.67e-08	1	1200	0	2.00	0	8	400
CarALW2	3200/+000/0140	a0.15 zubko100 Pitm0 Hofm0	5671	1.000e-02	2.63e-10	0	1200	0	2.00	0	8	108
CarALW6	2600/+000/0140	a0.15 zubko100 Pitm0 Hofm0	7464	1.000e-02	2.98e-10	0	1200	0	2.00	0	8	279
CarALW10	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	4450	1.000e-02	2.47e-10	0	1200	0	2.00	0	8	48
LeoIMFTC	2600/+000/0140	a0.15 zubko100 Pitm5 Hofm0	7837	5.553e+00	2.15e-07	1	1200	0	2.00	0	8	272
LeoIMFTA	3200/+000/0140	a0.15 zubko100 Pitm0 Hofm0	4588	4.010e+00	1.12e-07	1	1200	0	2.00	0	8	315
LeoIMFTE	3300/+000/0140	a0.15 zubko100 Pitm5 Hofm0	3118	7.601e+00	1.98e-07	1	1200	0	2.00	0	8	400

Notes. Column 1 lists the identifier. Column 2 lists the information on the model atmosphere that is used as T_{eff} (in K) / $(\log g \cdot 100) / ((\text{C/O}) - 100)$. Column 3 indicates the grain size and type: The number after the a indicates the grain size in μm . Then follows the proportion of AMC (zubko) : SiC (Pitm) : MgS (Hofm) = 100 : x : y. Column 4 lists the luminosity. Column 5 lists the dust optical depth at $0.5 \mu\text{m}$, and Column 6 lists the total mass-loss rate (assuming an expansion velocity of 10 km s^{-1} , and a dust-to-gas ratio of 0.005). Column 7 indicates if the optical depth was fitted ($f=1$, or fixed $f=0$). Column 8 lists the temperature at the inner dust radius, and Column 9 indicates if this temperature was fitted ($f=1$, or fixed $f=0$). Column 10 lists the slope of the density law, and Column 11 indicates if this temperature was fitted ($f=1$, or fixed $f=0$). Column 12 lists the outer radius in units of the inner dust radius. Column 13 lists the reduced χ^2 of the fit.

Table B.2. Fit results of the M star sample.

Identifier	$T_{\text{eff}}/\log g$ (K/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
wohg17	3300/+0.5	a0.10 Oliv70 AlOx30 Fe30	932967	1.201e-01	2.84e-07	1	1000	0	2.00	0	13	504
msxlmc1212	3900/+0.5	a0.20 Oliv40 AlOx60 Fe1	262501	1.000e-04	1.14e-10	0	1000	0	2.00	0	13	98
rsmen	2500/+0.0	a0.10 Oliv60 AlOx40 Fe30	752101	2.044e-01	4.37e-07	1	1000	0	2.00	0	13	492
w60d29	3800/+0.5	a0.20 Oliv90 AlOx10 Fe30	350174	1.000e-04	8.50e-11	0	1000	0	2.00	0	13	218
hd269788	4250/+0.0	a0.20 Oliv40 AlOx60 Fe3	611699	3.000e-03	8.67e-09	0	760	1	2.00	0	13	4010
msxlmc946	3200/+0.5	a0.10 Oliv50 AlOx50 Fe30	339561	4.252e-02	6.53e-08	1	1000	0	2.00	0	13	51
hd269924	3600/+0.0	a0.10 Oliv40 AlOx60 Fe3	745922	1.000e-03	3.69e-09	0	1000	0	2.00	0	13	4892
msxlmc1677	2700/+0.0	a0.10 Oliv90 AlOx10 Fe30	1952457	6.687e-01	2.05e-06	1	1000	0	2.00	0	13	1315
hd271832	3400/+0.0	a0.50 Oliv80 AlOx20 Fe3	1997701	1.391e-03	4.90e-09	1	1000	0	2.00	0	13	2553
msxlmc1686	2500/+0.0	a0.20 Oliv70 AlOx30 Fe30	1532676	2.973e-01	4.86e-07	1	1000	0	2.00	0	13	270
msxsmc067	3500/+0.0	a0.10 Oliv50 AlOx50 Fe30	143486	1.067e-02	1.12e-08	1	1000	0	2.00	0	13	196
smc010889	3700/+0.5	a0.10 Oliv70 AlOx30 Fe30	184822	5.192e-02	6.01e-08	1	1000	0	2.00	0	10	697
smc011709	3800/+0.5	a0.20 Oliv40 AlOx60 Fe30	114473	1.000e-02	9.16e-09	0	825	1	2.00	0	10	47
pmmr24	3800/+0.5	a0.50 Oliv60 AlOx40 Fe30	90740	9.816e-02	6.28e-08	1	1000	0	2.00	0	10	52
msxsmc096	3700/+0.5	a0.50 Oliv60 AlOx40 Fe30	107095	4.938e-02	3.35e-08	1	1000	0	2.00	0	13	76
msxsmc109	3800/+0.5	a0.10 Oliv90 AlOx10 Fe30	122980	1.344e-01	1.21e-07	1	1000	0	2.00	0	13	245
msxsmc168	3800/+0.5	a0.10 Oliv90 AlOx10 Fe30	93615	5.390e-02	4.21e-08	1	1000	0	2.00	0	13	320
s3mc203963	3900/+0.5	a0.20 Oliv40 AlOx60 Fe1	24445	1.289e-03	4.49e-10	0	1000	0	2.00	0	13	160
s3mc204111	4000/+0.0	a0.20 Oliv50 AlOx50 Fe30	57989	3.000e-03	1.25e-09	0	1000	0	2.00	0	13	7
s3mc205104	4000/+0.0	a0.20 Oliv40 AlOx60 Fe1	27422	1.000e-04	3.74e-11	0	1000	0	2.00	0	13	17
smc046662	3600/+0.5	a0.10 Oliv60 AlOx40 Fe30	113944	3.694e-02	3.42e-08	1	1000	0	2.00	0	10	269
smc052334	3700/+0.5	a0.10 Oliv60 AlOx40 Fe30	97741	1.352e-02	1.18e-08	1	1000	0	2.00	0	10	70
pmmr132	3800/+0.5	a0.20 Oliv70 AlOx30 Fe30	47998	9.110e-05	3.09e-11	0	1000	0	2.00	0	13	442
smc055188	3300/+0.5	a0.50 Oliv100 AlOx0 Fe30	104318	2.131e-01	1.38e-07	1	1000	0	2.00	0	10	218
pmmr141	3700/+0.5	a0.20 Oliv50 AlOx50 Fe30	98039	7.126e-03	3.68e-09	1	1000	0	2.00	0	13	82
smc55681	3800/+0.5	a0.10 Oliv70 AlOx30 Fe30	93022	6.387e-02	5.36e-08	1	1000	0	2.00	0	10	380
pmmr145	4000/+0.0	a0.20 Oliv100 AlOx0 Fe30	52487	5.000e-04	1.64e-10	0	1000	0	2.00	0	13	134
hv11464	3900/+0.5	a0.20 Oliv50 AlOx50 Fe30	55012	1.000e-02	7.15e-09	0	780	1	2.00	0	13	101
masseysmc60447	3800/+0.5	a0.50 Oliv50 AlOx50 Fe30	56568	1.770e-02	8.78e-09	1	1000	0	2.00	0	13	85
msxsmc149	3700/+0.5	a0.20 Oliv80 AlOx20 Fe30	198288	2.661e-01	1.76e-07	1	1000	0	2.00	0	13	416
smc083593	3600/+0.5	a0.10 Oliv80 AlOx20 Fe30	157236	7.268e-02	7.31e-08	1	1000	0	2.00	0	10	200
sagemcj044718	3600/+0.5	a0.10 Oliv60 AlOx40 Fe30	37506	3.201e-02	1.70e-08	1	1000	0	2.00	0	13	58
hv2236	3400/+0.0	a0.10 Oliv95 AlOx5 Fe10	113624	8.817e-01	8.13e-07	1	1000	0	2.00	0	13	716
hv11423	3700/+0.5	a0.10 Oliv80 AlOx20 Fe30	199246	7.809e-02	9.06e-08	1	1000	0	2.00	0	10	652
gv60	3600/+0.5	a0.20 Oliv80 AlOx20 Fe10	105755	5.856e-01	5.30e-07	1	773	1	2.00	0	13	115
msxlmc1189	3500/+0.5	a0.10 Oliv100 AlOx0 Fe30	115869	1.285e+00	1.75e-06	1	800	0	2.00	0	13	198
wohg64	3500/+0.0	a0.10 Oliv70 AlOx30 Fe10	432190	1.732e+01	3.55e-05	1	896	1	1.60	0	0.1	91695
msxlmc1204	3500/+0.0	a0.10 Oliv95 AlOx5 Fe30	198164	1.015e-01	1.85e-07	1	778	1	2.00	0	13	663
msxlmc1330	3400/+0.5	a0.10 Oliv80 AlOx20 Fe10	123820	6.978e-01	7.22e-07	1	1000	0	2.00	0	13	467
msxlmc1318	3200/+0.5	a0.50 Oliv70 AlOx30 Fe30	74948	3.013e-01	2.70e-07	1	800	0	2.00	0	13	163
hv2255	3500/+0.0	a0.10 Oliv90 AlOx10 Fe10	206364	6.201e-01	1.30e-06	1	800	0	2.00	0	13	1061
msxlmc1271	3400/+0.0	a0.20 Oliv70 AlOx30 Fe30	78591	5.075e-01	2.02e-07	1	1000	0	2.00	0	13	95
hv888	3500/+0.5	a0.50 Oliv70 AlOx30 Fe3	526751	2.736e-01	4.76e-07	1	1044	1	2.00	0	13	13598
msxlmc141	3600/+0.5	a0.10 Oliv80 AlOx20 Fe10	135417	5.272e-01	6.10e-07	1	1000	0	2.00	0	13	738
hv916	3400/+0.5	a0.20 Oliv90 AlOx10 Fe30	104646	1.555e+00	6.95e-07	1	1000	0	2.00	0	13	787
lmc116895	3800/+0.5	a0.20 Oliv80 AlOx20 Fe30	124490	1.014e-01	1.01e-07	1	758	1	2.00	0	10	138
lmc119219	3900/+0.5	a0.20 Oliv95 AlOx5 Fe30	55661	1.100e+00	4.04e-07	1	1000	0	2.00	0	10	363
wohs264	3400/+0.5	a0.20 Oliv90 AlOx10 Fe30	158954	1.249e+00	8.71e-07	1	912	1	2.00	0	13	161
lmc134383	3500/+0.5	a0.10 Oliv90 AlOx10 Fe30	87053	2.377e-01	2.79e-07	1	800	0	2.00	0	10	349
ngc1948wbt2215	3500/+0.0	a0.20 Oliv40 AlOx60 Fe30	227669	1.611e-02	2.30e-08	1	830	1	2.00	0	13	79
msxlmc549	3200/+0.5	a0.10 Oliv90 AlOx10 Fe30	178966	3.693e-01	3.51e-07	1	1000	0	2.00	0	13	565
msxlmc575	3800/+0.5	a0.20 Oliv70 AlOx30 Fe30	163654	4.616e-02	3.78e-08	1	893	1	2.00	0	13	29
msxlmc589	3900/+0.5	a0.50 Oliv70 AlOx30 Fe30	230016	2.711e-01	2.88e-07	1	1000	0	2.00	0	13	1933
hv963	3700/+0.5	a0.50 Oliv80 AlOx20 Fe30	104486	2.945e-01	3.91e-07	1	758	1	2.00	0	13	107
hv2551	3600/+0.5	a0.10 Oliv80 AlOx20 Fe30	87885	6.232e-02	4.67e-08	1	1000	0	2.00	0	13	168
hv2561	3700/+0.5	a0.20 Oliv90 AlOx10 Fe10	216781	4.956e-01	6.68e-07	1	758	1	2.00	0	13	146
hv5870	3600/+0.5	a0.10 Oliv90 AlOx10 Fe10	72629	1.054e+00	8.76e-07	1	1000	0	2.00	0	13	449
w60a27	3500/+0.5	a0.50 Oliv95 AlOx5 Fe30	220830	2.494e-01	2.43e-07	1	1000	0	2.00	0	13	565
hv5879	3700/+0.5	a0.20 Oliv80 AlOx20 Fe30	91718	5.129e-02	2.27e-08	1	1000	0	2.00	0	13	88
sp77_46-50	3700/+0.5	a0.50 Oliv60 AlOx40 Fe30	53155	3.196e-02	1.52e-08	1	1000	0	2.00	0	13	49
msxlmc810	3500/+0.5	a0.10 Oliv70 AlOx30 Fe30	164901	2.001e-01	2.10e-07	1	1000	0	2.00	0	13	256

Table B.2. Fit results of the M star sample: continued.

Identifier	$T_{\text{eff}}/\log g$ (K/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
msxlmc587	3500/+0.5	a0.50 Oliv90 AlOx10 Fe30	136128	6.572e-01	5.20e-07	1	1004	1	2.00	0	13	635
w60d22	3800/+0.5	a0.10 Oliv90 AlOx10 Fe30	147204	9.899e-02	1.62e-07	1	800	0	2.00	0	13	138
msxlmc839	3300/+0.5	a0.20 Oliv90 AlOx10 Fe10	248890	4.640e-01	5.14e-07	1	800	0	2.00	0	13	207
sagemcj053218	3900/+0.5	a0.10 Oliv40 AlOx60 Fe30	62668	4.352e-03	3.47e-09	1	1000	0	2.00	0	13	176
ngc2011sageirs1	3400/+0.0	a0.50 Oliv70 AlOx30 Fe30	86631	2.744e-01	1.63e-07	1	1048	1	2.00	0	13	93
hv996	3600/+0.5	a0.20 Oliv90 AlOx10 Fe30	209641	7.935e-01	9.71e-07	1	761	1	2.00	0	13	1610
msxlmc815	3600/+0.0	a0.10 Oliv95 AlOx5 Fe30	106709	4.519e-01	5.95e-07	1	800	0	2.00	0	13	1685
hv2700	3600/+0.5	a0.10 Oliv100 AlOx0 Fe30	65803	3.474e-01	2.13e-07	1	1000	0	2.00	0	13	64
msxlmc791	3500/+0.5	a0.10 Oliv90 AlOx10 Fe30	57028	5.232e-01	3.02e-07	1	1000	0	2.00	0	13	255
msxlmc870	3500/+0.5	a0.10 Oliv80 AlOx20 Fe30	93934	6.946e-01	5.39e-07	1	1000	0	2.00	0	13	588
msxlmc891	3400/+0.0	a0.20 Oliv80 AlOx20 Fe30	230799	7.067e-01	5.22e-07	1	971	1	2.00	0	13	279
mh6	3300/+0.5	a0.10 Oliv70 AlOx30 Fe30	97733	4.034e-01	4.28e-07	1	874	1	2.00	0	13	35
w60a72	2500/+0.0	a0.10 Oliv100 AlOx0 Fe10	136080	7.252e+00	1.21e-05	1	793	1	2.00	0	13	1009
w60a78	3600/+0.5	a0.20 Oliv50 AlOx50 Fe30	204913	1.769e-01	1.30e-07	1	1000	0	2.00	0	13	159
w60a81	3500/+0.0	a0.50 Oliv80 AlOx20 Fe30	126061	1.955e-01	2.75e-07	1	753	1	2.00	0	13	111
msxlmc897	3400/+0.0	a0.20 Oliv80 AlOx20 Fe30	208803	3.034e-01	2.15e-07	1	954	1	2.00	0	13	587
msxlmc939	3600/+0.0	a0.10 Oliv100 AlOx0 Fe30	76121	1.439e+00	1.63e-06	1	800	0	2.00	0	13	188
lmc175464	3500/+0.5	a0.10 Oliv70 AlOx30 Fe30	107680	2.045e-01	1.73e-07	1	1000	0	2.00	0	10	1224
hv1017	3600/+0.5	a0.50 Oliv90 AlOx10 Fe30	90016	7.347e-01	8.56e-07	1	788	1	2.00	0	13	103
lmc175746	3600/+0.5	a0.10 Oliv70 AlOx30 Fe30	72328	4.048e-01	2.91e-07	1	1000	0	2.00	0	13	679
hv2778	3700/+0.5	a0.10 Oliv100 AlOx0 Fe30	124584	3.855e-01	3.34e-07	1	1000	0	2.00	0	13	345
w61_6-24	3900/+0.5	a0.50 Oliv70 AlOx30 Fe30	58746	5.544e-02	3.13e-08	1	967	1	2.00	0	13	267
lmc177150	3600/+0.5	a0.20 Oliv70 AlOx30 Fe30	53682	8.597e-02	5.60e-08	1	755	1	2.00	0	10	59
ngc2100robb4	3900/+0.5	a0.20 Oliv60 AlOx40 Fe30	61000	1.339e-01	5.50e-08	1	1000	0	2.00	0	13	724
2massj054206	3400/+0.0	a0.50 Oliv70 AlOx30 Fe30	45847	2.114e-01	8.96e-08	1	1000	0	2.00	0	13	279
w61_6-57	3600/+0.5	a0.50 Oliv60 AlOx40 Fe30	50340	1.657e-01	7.66e-08	1	1000	0	2.00	0	13	65
lmc177997	3600/+0.5	a0.10 Oliv80 AlOx20 Fe30	102937	1.685e-01	1.38e-07	1	1000	0	2.00	0	10	414
hv2834	3300/+0.5	a0.10 Oliv70 AlOx30 Fe30	167638	2.135e-01	2.15e-07	1	1000	0	2.00	0	13	1717
hv11223	3500/+0.0	a0.10 Oliv70 AlOx30 Fe30	28195	1.000e-02	2.87e-09	0	1196	1	2.00	0	13	141
hv1366	3400/+0.0	a0.20 Oliv60 AlOx40 Fe30	9881	3.624e-02	5.26e-09	1	1000	0	2.00	0	13	464
msxsmc024	3200/+0.0	a0.10 Oliv60 AlOx40 Fe30	54731	4.366e-01	2.60e-07	1	1000	0	2.00	0	13	545
j004444	3600/+0.0	a0.10 Oliv100 AlOx0 Fe30	33872	2.228e-02	9.56e-09	1	1000	0	2.00	0	10	22
msxsmc018	2500/+0.0	a0.20 Oliv100 AlOx0 Fe10	28032	1.631e+01	3.99e-06	1	1041	1	2.00	0	13	426
bfm1	3200/+0.5	a0.10 Oliv40 AlOx60 Fe30	11687	3.253e-02	9.83e-09	1	1000	0	2.00	0	13	397
msxsmc055	2500/+0.0	a0.50 Oliv90 AlOx10 Fe30	85352	5.320e+00	4.51e-06	1	953	1	2.00	0	13	447
msxsmc134	3700/+0.5	a0.10 Oliv100 AlOx0 Fe30	7790	2.508e+00	1.10e-06	1	756	1	2.00	0	13	185
hv11303	3500/+0.0	a0.10 Oliv50 AlOx50 Fe30	35125	9.838e-03	5.12e-09	1	1000	0	2.00	0	13	128
bmbb75	3900/+0.5	a0.10 Oliv90 AlOx10 Fe30	21370	1.076e+00	4.89e-07	1	948	1	2.00	0	5	467
hv11329	3500/+0.0	a0.20 Oliv60 AlOx40 Fe30	29546	2.059e-02	5.30e-09	1	1000	0	2.00	0	13	97
msxsmc000	2500/+0.0	a0.10 Oliv40 AlOx60 Fe30	25196	1.535e-02	6.64e-09	1	1000	0	2.00	0	13	273
hv838	3400/+0.0	a0.20 Oliv60 AlOx40 Fe30	106791	1.000e-02	5.85e-09	0	939	1	2.00	0	13	2717
hv11366	3500/+0.0	a0.20 Oliv70 AlOx30 Fe30	28519	1.000e-02	2.42e-09	0	1000	0	2.00	0	13	224
hv12149	3200/+0.5	a0.20 Oliv95 AlOx5 Fe30	55609	2.759e-01	8.08e-08	1	1000	0	2.00	0	13	608
msxsmc181	3200/+0.5	a0.50 Oliv90 AlOx10 Fe30	42726	1.737e+00	5.22e-07	1	1220	1	2.00	0	13	889
hv1963	3400/+0.0	a0.10 Oliv50 AlOx50 Fe30	44814	1.051e-02	6.08e-09	1	1000	0	2.00	0	13	84
irasF01066	3000/+0.5	a0.20 Oliv90 AlOx10 Fe30	18121	1.313e+00	4.14e-07	1	775	1	2.00	0	10	343
hv12956	3500/+0.0	a0.10 Oliv90 AlOx10 Forst15 Fe30	24353	2.499e+00	6.58e-07	1	800	0	1.49	1	13	515
ngc1651sageirs1	3400/+0.5	a0.20 Oliv40 AlOx60 Fe30	5894	7.144e-02	8.88e-09	1	1000	0	2.00	0	13	57
iras04407	4250/+0.0	a0.20 Oliv80 AlOx20 Fe30	40466	1.136e+01	2.74e-06	1	1074	1	1.68	1	13	1006
iras04498	2800/+0.0	a0.20 Oliv80 AlOx20 Fe30	71579	4.772e+00	2.63e-06	1	851	1	2.00	0	13	325
iras04509	2700/+0.0	a0.20 Oliv95 AlOx5 Fe10	67477	9.269e+00	4.55e-06	1	902	1	2.00	0	13	790
sagemcj045128	3700/+0.5	a0.50 Oliv70 AlOx30 Fe30	1660	2.581e+00	2.71e-07	1	1000	0	2.00	0	9	393
iras04516	3200/+0.5	a0.20 Oliv90 AlOx10 Fe10	60616	1.130e+01	3.27e-06	1	1161	1	2.00	0	13	824
sagemcj045309	3400/+0.0	a0.20 Oliv40 AlOx60 Fe1	5545	1.000e-04	1.39e-11	0	1000	0	2.00	0	13	189
iras04545	2500/+0.0	a0.10 Oliv95 AlOx5 Fe10	24930	2.953e+01	2.23e-05	1	847	1	2.00	0	13	2761
sagemcj045623	4000/+0.0	a0.20 Oliv70 AlOx30 Fe30	7524	3.945e-01	5.63e-08	1	1000	0	2.00	0	13	125
iras05003	3600/+0.5	a0.10 Oliv100 AlOx0 Fe10	17860	1.049e+01	4.52e-06	1	1030	1	2.00	0	9	264
msxlmc61	3300/+0.5	a0.50 Oliv100 AlOx0 Fe30	14409	2.179e+00	6.23e-07	1	1003	1	2.00	0	13	1066
hv2310	2900/+0.0	a0.10 Oliv60 AlOx40 Fe30	34359	9.705e-02	4.43e-08	1	1000	0	2.00	0	13	30984
sagemcj050759	3900/+0.0	a0.10 Oliv70 AlOx30 Fe30	3257	1.078e+00	1.48e-07	1	1000	0	1.82	1	5	143
bmbbw180	3500/+0.5	a0.20 Oliv40 AlOx60 Fe30	10134	8.380e-03	1.39e-09	1	1000	0	2.00	0	13	137

Table B.2. Fit results of the M star sample: continued

Identifier	$T_{\text{eff}} / \log g$ (K/-)	grain size/type	L (L_{\odot})	$\tau_{0.5}$	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	f	T_c (K)	f	p	f	R_{out} ($\cdot 10^3$)	χ^2
sagemcj051059	3400/+0.0	a0.50 Oliv80 AlOx20 Fe30	17955	2.420e-01	8.72e-08	1	881	1	2.00	0	13	36
sagemcj051213	3400/+0.5	a0.10 Oliv90 AlOx10 Fe10	6294	2.034e-01	7.12e-08	1	801	1	2.00	0	13	122
iras05128	2500/+0.0	a0.20 Oliv95 AlOx5 Fe10	18869	2.490e+01	4.38e-06	1	1129	1	2.00	0	13	1281
sagemcj051339	3500/+0.0	a0.20 Oliv70 AlOx30 Fe30	5605	1.597e-01	1.72e-08	1	1000	0	2.00	0	13	65
ngc1866robb136	3500/+0.0	a0.10 Oliv40 AlOx60 Fe30	13066	3.000e-03	9.99e-10	0	1000	0	2.00	0	13	341
sagemcj051412	3500/+0.0	a0.20 Oliv80 AlOx20 Fe10	4925	1.802e-01	1.89e-08	1	1000	0	2.00	0	13	55
sagemcj051526	3400/+0.0	a0.10 Oliv60 AlOx40 Fe30	6687	3.000e-03	1.10e-09	0	760	1	2.00	0	13	316
sagemcj051612	3400/+0.0	a0.50 Oliv60 AlOx40 Fe30	5022	1.769e-01	1.59e-08	1	1200	0	2.00	0	13	16
sagemcj051747	3500/+0.0	a0.10 Oliv100 AlOx0 Fe10	2032	6.142e-01	5.43e-08	1	1157	1	2.00	0	13	53
hvj5715	3400/+0.0	a0.20 Oliv80 AlOx20 Fe50	28173	2.194e-01	4.91e-08	1	1000	0	2.00	0	13	26
sagemcj052014	3500/+0.0	a0.50 Oliv50 AlOx50 Fe30	5158	8.028e-02	1.14e-08	1	1000	0	2.00	0	13	56
sagemcj052051	3500/+0.5	a0.20 Oliv90 AlOx10 Fe30	4827	3.926e-01	3.79e-08	1	1012	1	2.00	0	13	125
sagemcj052101	3500/+0.5	a0.50 Oliv100 AlOx0 Fe10	9679	3.267e-01	7.90e-08	1	1000	0	2.00	0	13	290
sagemcj052206	3600/+0.5	a0.20 Oliv90 AlOx10 Fe10	4123	1.300e+00	8.92e-08	1	1191	1	2.00	0	13	172
shv0523185	3400/+0.5	a0.10 Oliv100 AlOx0 Fe30	2946	3.948e-01	3.86e-08	1	1099	1	2.00	0	13	29
hvj12793	3600/+0.5	a0.20 Oliv100 AlOx0 Fe10	98278	1.396e+00	6.88e-07	1	1000	0	2.00	0	13	771
iras05246	3900/+0.0	a0.10 Oliv70 AlOx60 Fe30	9430	3.114e+01	2.92e-05	1	819	1	2.26	1	13	116
hvj5810	3400/+0.0	a0.10 Oliv40 AlOx60 Fe30	21390	6.560e-03	2.73e-09	1	1000	0	2.00	0	13	21257
ogle052620	3400/+0.0	a0.10 Oliv90 AlOx10 Fe30	5499	1.543e-01	5.06e-08	1	750	0	2.00	0	13	148
wbp77	3500/+0.0	a0.10 Oliv50 AlOx50 Fe30	5141	4.938e-02	9.83e-09	1	1000	0	2.00	0	26	282
hvj2572	3200/+0.5	a0.50 Oliv80 AlOx20 Fe30	55495	1.777e-01	8.10e-08	1	1000	0	2.00	0	13	277
msxlmc642	3900/+0.5	a0.20 Oliv100 AlOx0 Fe10	32436	1.221e+01	5.07e-06	1	976	1	2.00	0	13	260
hvj2575	3200/+0.5	a0.20 Oliv40 AlOx60 Fe30	14519	3.000e-02	4.47e-09	0	1104	1	2.00	0	13	17871
hvj2578	3100/+0.5	a0.50 Oliv70 AlOx30 Fe30	54013	1.936e-01	8.62e-08	1	1000	0	2.00	0	13	5433
iras05298	3500/-0.5	a0.10 Oliv90 AlOx10 Fe10	37608	2.518e+01	1.43e-05	1	1070	1	1.93	1	9	221
shv0530472	3400/+0.0	a0.10 Oliv40 AlOx60 Fe30	7645	1.000e-04	2.49e-11	0	1000	0	2.00	0	13	1264
sagemcj053128	3600/+0.5	a0.10 Oliv90 AlOx10 Forst5 Fe30	6975	1.693e+00	3.53e-07	1	992	1	2.00	0	13	145
sagemcj053206	3400/+0.0	a0.10 Oliv40 AlOx60 Fe30	8585	2.000e-02	4.37e-09	0	1082	1	2.00	0	13	173
msxlmc807	4750/+0.0	a0.10 Oliv100 AlOx0 Fe10	22209	1.929e+01	1.15e-05	1	1091	1	2.00	0	9	222
iras05329	3500/+0.5	a0.10 Oliv100 AlOx0 Fe10	46490	4.106e+01	5.15e-05	1	1010	1	2.50	1	9	3928
hvj12620	3400/+0.0	a0.20 Oliv70 AlOx30 Fe30	16786	3.000e-02	4.61e-09	0	1067	1	2.00	0	13	938
sagemcj053343b	3500/+0.0	a0.10 Oliv40 AlOx60 Fe30	18363	1.815e-02	7.17e-09	1	1000	0	2.00	0	13	89
sagemcj053343a	3400/+0.0	a0.20 Oliv60 AlOx40 Fe30	11596	6.993e-02	2.36e-08	1	928	1	2.00	0	13	72
sagemcj053548	3400/+0.0	a0.50 Oliv70 AlOx30 Fe30	6047	9.236e-02	2.72e-08	1	750	0	2.00	0	13	109
sagemcj053655	3300/+0.5	a0.10 Oliv80 AlOx20 Fe10	4808	2.894e-01	6.12e-08	1	1096	1	2.00	0	13	211
iras05402	4500/+0.0	a0.10 Oliv95 AlOx5 Fe10	50040	1.870e+01	2.04e-05	1	985	1	2.00	0	13	436
wohg449	3700/+0.5	a0.10 Oliv100 AlOx0 Fe30	6570	1.584e-01	4.79e-08	1	840	1	2.00	0	13	78
msxlmc947	2800/+0.0	a0.50 Oliv95 AlOx5 Fe10	61075	6.219e-01	3.59e-07	1	1000	0	2.00	0	13	758
sagemcj054114	3800/+0.5	a0.50 Oliv70 AlOx30 Fe30	3751	7.385e-01	1.04e-07	1	1000	0	2.00	0	13	155
wohg494	3400/+0.0	a0.20 Oliv60 AlOx40 Fe30	23677	3.000e-02	6.04e-09	0	1048	1	2.00	0	13	239
sagemcj054254	3200/+0.5	a0.20 Oliv70 AlOx30 Fe10	10370	1.040e-01	2.37e-08	1	797	1	2.00	0	13	205
sagemcj054314	3400/+0.0	a0.10 Oliv40 AlOx60 Fe30	16022	7.475e-03	2.69e-09	1	1000	0	2.00	0	13	52
sagemcj054406	3300/+0.5	a0.50 Oliv70 AlOx30 Fe30	31361	7.671e-02	4.86e-08	1	766	1	2.00	0	13	63
sagemcj054440	3600/+0.5	a0.10 Oliv100 AlOx0 Fe10	1586	9.791e-01	1.85e-07	1	800	0	2.00	0	13	864
hvj12667	2800/+0.0	a0.20 Oliv80 AlOx20 Fe30	42232	1.883e-01	9.63e-08	1	937	1	2.00	0	13	35346
hvj12070	2700/+0.0	a0.20 Oliv70 AlOx30 Fe30	44443	1.752e-01	3.61e-08	1	1133	1	2.00	0	13	907
iras05545	3700/+0.0	a0.10 Oliv60 AlOx40 Forst10 Fe30	11824	2.401e+00	2.51e-07	1	1200	0	1.58	1	13	747
iras05558	3000/+0.5	a0.20 Oliv90 AlOx10 Fe10	34173	1.876e+01	5.97e-06	1	1000	0	2.00	0	13	181
sagemcj060053	3400/+0.5	a0.10 Oliv70 AlOx30 Fe30	7895	7.219e-02	1.60e-08	1	1000	0	2.00	0	13	40

Notes. Column 1 lists the identifier. Column 2 lists the information on the model atmosphere that is used as T_{eff} (in K) / $\log g$. Column 3 indicates the grain size and type: The number after the a indicates the grain size in μm . Then follows the proportion of olivine (MgFeSiO_4), corundum, metallic iron, and sometimes forsterite. Column 4 lists the luminosity. Column 5 lists the dust optical depth at $0.5 \mu\text{m}$, and Column 6 lists the total mass-loss rate (assuming an expansion velocity of 10 km s^{-1} , and a dust-to-gas ratio of 0.005). Column 7 indicates if the optical depth was fitted ($f=1$, or fixed $f=0$). Column 8 lists the temperature at the inner dust radius, and Column 9 indicates if this temperature was fitted ($f=1$, or fixed $f=0$). Column 10 lists the slope of the density law, and Column 11 indicates if this temperature was fitted ($f=1$, or fixed $f=0$). Column 12 lists the outer radius in units of the inner dust radius. Column 13 lists the reduced χ^2 of the fit.